Reactive localized π -radicals on rim-based pentagonal rings: properties and concentration in flames

Angiras Menon¹, Jacob Martin¹, Gustavo León¹, Dingyu Hou^{2,3}, Laura Pascazio¹, Xiaoqing You^{2,3}, Markus Kraft^{1,4}

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 ¹ Department of Chemical Engineering and Biotechnology University of Cambridge Philippa Fawcett Drive Cambridge, CB3 0AS United Kingdom E-mail: mk306@cam.ac.uk
 ³ Key Laboratory for Thermal Science and

 Key Laboratory for Thermal Science and Power Engineering of Ministry of Education Tsinghua University Beijing, 100084 China ² Center for Combustion Energy Tsinghua University Beijing, 100084 China

 ⁴ School of Chemical and Biomedical Engineering Nanyang Technological University 62 Nanyang Drive Singapore 637459

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Edited by

Computational Modelling Group Department of Chemical Engineering and Biotechnology University of Cambridge Philippa Fawcett Drive Cambridge CB3 0AS United Kingdom

E-Mail: c4e@cam.ac.uk World Wide Web: http://como.ceb.cam.ac.uk/



Abstract

The impact of localized π -radicals on soot formation is explored by considering their electronic structure and computing their relative concentrations in flame conditions. Electronic structure calculations reveals that the presence of localized π -radicals on rim-based pentagonal rings is due to aromaticity. We further calculated a complete mechanism for the formation and elimination of the site from hydrogen additions and abstractions. A batch reactor with flame concentrations of H[•] and H₂ was used to determine the time-dependent concentration of localized π -radicals. Low temperatures (<1000 K) favored the fully saturated rim-based pentagonal ring. Soot nucleation temperatures (1000-1500 K) give way to unsaturated rim-based pentagons being favored. Localized π -radicals on rim-based pentagonal rings are found to be in higher concentration than the aryl-type σ -radical on the rim-based pentagon (mole fractions of $10^{-6} - 10^{-7}$) below 1500 K, consistent with recent experimental observations. Higher temperatures favor the σ -radical and the concentration of the localized π -radical on rim-based pentagons becomes negligible. A kinetic Monte Carlo treatment of multiple sites indicates that multiple localized π -radicals are possible on a single molecule. These results reveal the importance of localized π -radicals on rimbased pentagonal rings for rapid formation of soot nanoparticles in flames involving aromatic rim-linked hydrocarbons (ARLH).



Highlights

- Spin density and Clar analyses are applied to quantify the degree of localization of various PAH radicals.
- Density Functional Theory and variational transition state theory calculations are used to compute the process rate constants and for the formation of a localized π -radical on five-member ring containing PAHs.
- Kinetic simulations in a 0-dimensional reactor showed that the localized π -radical product competes with σ -radical products at temperatures up to even 1500 K, suggesting they may be important to consider for combustion mechanisms.
- Kinetic Monte Carlo simulations suggest that multiple such localized π -radical sites can exist on a single PAH, suggesting potential for chemical polymerization mechanisms.

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1 Introduction

Soot nanoparticles invade our bodies and damage almost every organ [13]. Within the atmosphere they absorb large amounts of infrared light, contributing to global heating on nearly the same scale as carbon dioxide [3, 16]. Fundamental insights into this process have remained elusive, but recent experimental techniques such as high resolution atomic force microscopy (HR-AFM) [4] and tunable photoionisation time of flight mass spectrometry (PI-TOF MS) [11] are beginning to uncover new reactive aromatic soot precursors that lead to soot formation and its potential elimination. We recently mapped the reactivity of the observed edges using electronic structure theory with reactivity indices [15]. We found localized π -radicals on rim-based pentagonal rings that are partially saturated/protonated (previously explored computationally for edge rearrangements [23]). This enables complexes that are both π -stacked and covalently bonded, forming a rimbond on the face of the aromatic species. We call these complexes aromatic rim-linked hydrocarbons (ARLH). The importance of localized π -radicals in soot formation was first introduced by Wang at the 2010 International Symposium on Combustion [22], where he considered a separate localization mechanism based on biradical systems such as acenes [12, 22].

HR-AFM of aromatic soot precursors showed the presence of these partially saturated sites as well as fully saturated rim-based pentagons [4]. This would suggest that a partial equilibrium exists between rim-based pentagonal rings and hydrogen radicals in flames, potentially leading to significant concentrations of reactive localized π -radicals. The concentration of another radical – the σ -radical – was computed by Howard in 1991 [10], where the edges of these aromatic species were considered to be in partial equilibrium with H[•] and H₂ in the flame. On average, 2–3 σ -radicals were found to be present in each \approx 670 Da aromatic species. However, no similar analysis exists for partially saturated rim-based pentagonal rings.

In this paper, we first explore the localization of π -radicals. A reaction mechanism and rates are then calculated for partially saturated rim-based pentagonal rings. Batch reactor simulations using kinetic equations and Monte Carlo methodologies are then used to explore the concentration of these reactive π -radicals in flames.

2 Methodology

Geometry optimizations and vibrational frequency calculations were performed using the hybrid density functional B3LYP and the 6-311G(d,p) basis set for all chemical species and transition states. Transition states were confirmed to have one imaginary frequency corresponding to the reaction in question. The energies of all major species and transition states were further refined using the composite CBS-QB3 method. All quantum chemistry calculations were performed using the Gaussian 16 program [5].

The rate constants of all reactions with a well-defined transition state and barrier were estimated using conventional transition state theory as implemented in the Arkane package within Reaction Mechanism Generator [6]. Partition functions were evaluated using the rigid rotor harmonic oscillator approximation and quantum tunneling corrections were applied through the Wigner correction [24]. For the barrierless hydrogen-PAH radical recombinations, two different approaches were used to estimate the rate constant. First, RRKM theory with a simple Gorin Model was used as implemented in Unimol [18]. The potential energy as a function of fragment separation was fitted to a Morse potential and the energies of the separated fragments were taken from the CBS-QB3 energies. However, since the PAH fragment in this case is large, the Gorin model is less reliable. Hence, the rate constants for the barrierless channels were also estimated using variational transition state theory (VTST) [20] as implemented in ktools within Multiwell [2]. Trial transition state geometries and vibrations were taken from potential energy surface scans of the PAH-H bond using B3LYP/6-311G(d,p). The energy and momentum maxima and grain sizes were taken from [1]. Ultimately, the VTST rate constants were used as the Gorin model appeared to greatly overestimate the recombination reaction rate constants (see Supplementary information).

Kinetic simulations were performed in a 0-D isothermal reactor using Cantera [8] at a pressure of 1 atmosphere and initial mole fractions of 10^{-5} , 0.001, and 0.1 for accoronene, H, and H₂ with the rest as N₂. These are representative of typical concentrations of these species in flames [17]. The rates for the reactions of the five-membered ring in acenaphthalene were used, as it is expected that these will be very similar to those for the five-membered ring in acecoronene. Justification is provided in the supplementary information. In addition, kinetic Monte Carlo (KMC) simulations were conducted for coronene with multiple rim-based five-membered rings to see if multiple localized π -radical sites could form, using the five-membered ring as the reactive site. The reactions, initial concentrations, and pressure were the same as for the 0-D kinetic simulation.

3 Results and discussion

3.1 Localization of π -radicals

Localization of π -radicals is driven by aromaticity. We will highlight this by considering the spin density interpreted through a Clar analysis for π -radical doublet spin states.

Figure 1 shows the spin density isosurface as well as the value of the spin density for the most spin-rich site. The phenylmethyl radical [Fig. 1 a)] shows the most significant spin density on the methyl site. A Clar analysis would suggest that the phenyl ring contains an aromatic sextet ("six π -electrons localized in a single benzene-like ring separated from adjacent rings by formal CC single bonds" [19]) with the radical residing solely on the methyl group. Spin density is seen within the aromatic ring suggesting other minor Clar resonance structures, however, the Clar structure shown is found to dominate suggesting that the aromaticity of the ring is maximized when the π -radical is localized to the methyl site. Similarly with the fluorenyl radical [Fig. 1 b)], the major Clar structure suggests two sextets with the radical localized to the pentagonal ring, which is seen in the spin density. A Clar analysis of the cyclopentamethyl radical [Fig. 1 c)], the focus of this paper, would suggest a traveling sextet across the two six-membered rings with the radical localized on the unsaturated pentagonal ring site. The spin density suggests that some minor delocal-



Figure 1: Spin density isosurface=0.025 shown on the molecular geometry with the Clar analysis. The spin density of the most spin rich carbon site is also shown indicating the degree of localization.

ization is occurring to the β -site from the primary radical site on the aromatic edge due to minor Clar structures [15]. The fact that this site is not significantly delocalized past the β -site is seen from the lack of change in the spin density after enlarging the aromatic network [Fig. 1 d)]. Furthermore, no significant change is seen for the same π -radical site on the curved aromatic corannulene in Figure 1 e).

Figure 1 f) – j) shows the impact of delocalization on π -radicals, however, we still find that aromaticity drives the location of the delocalized π -radical. For indenyl [Fig. 1 f)] the Clar analysis provides one sextet with a radical in resonance between two sites, with spin density showing that the radical is indeed split. Protonation of a benzene ring [Fig. 1 g)] again suggests three locations for the π -radical delocalization. Phenalenyl [Fig. 1 h)], the prototypical six-membered ring delocalized π -radical, has the radical split over six sites,



Figure 2: Potential energy surfaces for the reactions on five-member rings in acenaphthalene leading to the formation of localized π -radicals on rim-based pentagonal rings at 0 K. Energies are computed at the CBS-QB3//B3LYP/6-311G(d,p) level of theory.

still driven by aromaticity. The Clar analysis shows one sextet with the radical residing on the zig-zag edge with six resonance structures suggesting significant delocalization. Enlarging the aromatic network in this case [Fig. 1 i) and j)] leads to a delocalization of the π -radical with some minor localization on zig-zag edges, which can be justified by a major Clar structure with the radical centered on these edges. Therefore, the π -radical can be either localized or delocalized depending on the aromatic topology, which can be rationalized by aromaticity rules.

3.2 Reaction mechanism for localized π -radicals on rim-based pentagonal rings

Entropic considerations suggest that hydrogen addition would be unfavored at high temperatures due to 1) the reverse reaction leading to two species, and 2) the hydrogen addition reactions having a larger pre-exponential factor, as the additions can occur from above and below the aromatic plane, whereas hydrogen abstraction requires a collision directly along the C–H bond in order to form the radical. At flame temperatures this paints a picture of rapid hydrogen addition and removal during soot formation, requiring a detailed mechanism to reveal the concentration of reactive localized π -radicals on rimbased pentagonal rings. It should be mentioned that systems with biradical character are not considered due to space restrictions [12, 22].

Figure 2 presents the potential energy surfaces for the reactions of acenaphthalene (A2R5) that could lead to the formation of the localized π -radical A2R5H, a σ -radical (A2R5-), as well as a fully hydrogenated five-membered ring (A2R52H). Starting from A2R5 as the reactant in Figure 2 a), A2R5- can be produced through hydrogen abstraction by an H radical, which proceeds with a moderate barrier of 17.7 kcal/mol. This is similar to values reported for hydrogen abstraction by H radicals on PAHs using the G3(MP2,CC) composite method [9]. Hydrogen can also attack the five-membered ring on A2R5, resulting in the localized π -radical, A2R5H. This process has a very low barrier of 1.4 kcal/mol, and releases 43 kcal/mol of energy, meaning it is expected to be preferred at low temperatures. Finally, A2R5H can undergo a hydrogen loss process, the reverse of the barrierless A2R5M and hydrogen radical recombination reaction. The reaction energy for the hydrogen loss in this case is high as expected, at 108 kcal/mol. In Figure 2 b), A2R5- can also be formed by a hydrogen loss from A2R5. Again, the reverse process of the A2R5- and hydrogen radical recombination is barrierless. This hydrogen loss also has a very high reaction energy of 115.5 kcal/mol. A2R5 can also undergo a hydrogen migration to form A2R5M, but this requires a large barrier (72.2 kcal/mol) to be overcome in order for the migration to proceed, with a small reverse barrier. Both of these processes are expected to be unfavorable at flame temperatures. In Figure 2 c), the localized π -radical A2R5H can have hydrogen abstraction by H radicals occur at both carbons along the five-membered ring peripheral free edge. One abstraction results in the formation of A2R5M, requiring a barrier of 13.2 kcal/mol, with a reaction energy of 3.4 kcal/mol. The other abstraction requires a barrier of 10.9 kcal/mol and re-produces A2R5, with a reaction energy of -61.4 kcal/mol. Between the two abstraction processes, the production of A2R5 has a slightly lower barrier and proceeds to a lower energy product, so it is expected that A2R5 will be preferentially formed over A2R5M by abstraction. Alternatively, the H radical can undergo a barrierless recombination reaction with the localized π -radical A2R5H to form the protonated A2R52H. With a reaction energy of -84.0 kcal/mol, this is expected to be the competing route with abstraction, producing A2R5. Finally, Figure 2 d) presents hydrogen abstraction by H radicals on either of the fully saturated carbon sites in A2R52H, resulting in the re-formation of A2R5H. This hydrogen abstraction has a much lower barrier than those seen for the abstractions on A2R5 or A2R5H, at just 5.8 kcal/mol. This abstraction also proceeds downhill in energy with a decrease in 20.5 kcal/mol, which is also in contrast to the A2R5 and A2R5H abstractions. This abstraction provides a return path to the localized π -radical. The rate constants for the reactions presented in the potential energy surface in Figure 2 and their reverse reactions were computed in the temperature range 300 – 3000 K and at the high pressure limit. The rate constants were then fitted to the modified Arrhenius form, with the parameters given in Table 1.

To examine the accuracy of the rate coefficients calculated above, one can compare the rate constants for the hydrogen abstraction by H radicals to those previously calculated by the authors [9], where we calculated the rate of abstraction from A2R5. The value calculated using CBS-QB3 is higher by a factor of 1.72 at 1500 K. This follows from the barrier for this abstraction predicted by CBS-QB3, being 1.8 kcal/mol lower than the previous calculations, which is within their reported uncertainty of \pm 2 kcal/mol for the M06-2X barrier heights. Additionally, Violi reported a barrier of 80 kcal/mol for

Reaction	A	п	E				
With Barrier							
$A2R5+H\rightarrow A2R5+H_2$	$1.99 \cdot 10^{8}$	1.88	16.76				
A2R5-+H ₂ \rightarrow A2R5+H	$7.08 \cdot 10^5$	2.11	4.89				
A2R5+H \rightarrow A2R5H	$1.63 \cdot 10^{9}$	1.51	0.77				
A2R5H→A2R5+H	$1.93\cdot10^{10}$	1.24	44.66				
A2R5→A2R5M	$2.65 \cdot 10^{11}$	0.70	71.85				
A2R5M→A2R5M	$3.19 \cdot 10^{11}$	0.40	6.88				
A2R5H+H \rightarrow A2R5M+H ₂	$7.29 \cdot 10^{7}$	1.48	11.84				
$A2R5M+H_2 \rightarrow A2R5H+H$	$4.85 \cdot 10^{5}$	1.89	7.49				
A2R5H+H \rightarrow A2R5+H ₂	$2.17 \cdot 10^{7}$	1.86	9.24				
A2R5+H ₂ \rightarrow A2R5H+H	$1.20 \cdot 10^{5}$	2.56	69.86				
A2R52H+H \rightarrow A2R5H+H ₂	$4.42 \cdot 10^{7}$	1.83	4.33				
$A2R5H\text{+}H_2 \text{\rightarrow} A2R52H\text{+}H$	$2.41 \cdot 10^{6}$	1.78	24.28				
Barrierless							
A2R5→A2R5-+H	$2.87 \cdot 10^{15}$	-0.32	117.47				
A2R5-+H \rightarrow A2R5	$4.90 \cdot 10^{11}$	0.21	0.00				
A2R5H→A2R5M+H	$4.61 \cdot 10^{15}$	-0.35	109.87				
A2R5M+H \rightarrow A2R5H	$1.19 \cdot 10^{13}$	0.09	0.28				
A2R52H→A2R5H+H	$1.89 \cdot 10^{16}$	-0.40	86.38				
A2R5H+H \rightarrow A2R52H	$6.95 \cdot 10^{12}$	0.10	0.35				

Table 1: Modified Arrhenius rate parameters for the localized π -radical mechanism. The units are kcal/mol, K, cm³mol⁻¹s⁻¹ and s⁻¹.

migration of a hydrogen atom on the bay site of benzo[c]phenanthrene, resulting in the formation of a carbene site [21]. This is not too dissimilar to the migration barrier of 72.2 kcal/mol for A2R5 in this work, given that the results from [21] were computed using energies at B3LYP/6-31G(d,p) compared to CBS-QB3.

For the barrierless recombination reactions, Kislov and coworkers computed the reaction energy of the H radical–naphthyl recombination as -111.0 kcal/mol using G3(MP2,CC). This reaction is similar to the H radical–A2R5- recombination, as is our energy of -115.5 kcal/mol. The reaction energy of A2R5M and H is also similar at -107.8 kcal/mol. The A2R5H recombination reaction energy is quite different at -84.0 kcal/mol, but the H radical attacks a carbon that already has a hydrogen, which is not true for the other reactions, so this difference is expected. Harding *et al.* computed the rate of the H radical–naphthyl recombination reaction using interaction energies determined by CASPT2/cc-pVDZ and VRC-TST for the rates. In general, the rate constants calculated by Harding for the H radical–naphthyl recombination are one to two orders of magnitude higher than the recombinations here. The calculations here are less accurate, as the interaction energies are determined by DFT and not a multi-reference method. On the other hand, it was noted that for hydrogen abstraction reactions, the reaction on A2R5 is several orders of magnitude lower than for naphthyl [9], so this difference may due to the reactant molecule. Further refinement of the rates of the barrierless reactions is necessary, as these will be



Figure 3: 0-dimensional homogeneous gas-phase reactor simulations of reactions involving acecoronene (A7R5) at atmospheric pressure and typical flame compositions. The degree of saturation of the five-membered ring is shown in the figure.

the largest source of uncertainty in the kinetic mechanism.

3.3 Concentration profiles in flames

Figure 3 provides the kinetic simulations in a 0-D, homogeneous gas-phase reactor at 1 atmosphere of pressure using the 18 reactions that involve the five-membered ring detailed in Table 1. The chosen reactant PAH is acecoronene, or A7R5, representative of a slightly larger PAH. Since reactions of carbons in the six-membered ring are not considered (as the five-membered ring is of primary interest), the choice of reactant PAH is largely unimportant. The rates computed for A2R5 are also likely very similar for larger PAHs, which has been observed for hydrogen abstraction by H radicals on PAHs [9]. Computations we performed of rate constants for hydrogen abstraction, migration, and addition for A7R5 suggest this is indeed the case (see Supplementary information). The kinetic simulations were conducted for six temperatures, including a lower temperature threshold for soot formation of >1000 K, temperatures of 1250 and 1400 K where soot nucleation is found in flames [7], a typical flame temperature of 1500 K, and temperatures representative of maximum values seen in flames of 1800 and 2000 K.

Figure 3 shows clear trends in the degree of saturation of the carbons on the five-membered ring. At 1000 K, the saturated products are preferred, with the fully saturated species being the dominant product at mole fractions near 10^{-5} . In other words, most of the reactant PAH transforms to a fully saturated five-membered ring product. However, the localized

 π -radical is the second most favored product with mole fractions of around 10⁻⁶. The reactant PAH is depleted, but then starts to reform at around 1 ms when the reverse reactions start to occur. At 1250 and 1400 K, it can be observed that the major product is the reactant with an unsaturated rim-based pentagonal ring, followed by the fully saturated five-membered ring and the localized π -radical. Comparing these results with the HR-AFM structures we find a consistent frequency of rim-based pentagonal sites with a ratio of 27:12:4 for the unsaturated, saturated and partially saturated rim-based pentagonal rings [4]. The mole fraction of the saturated product is lower at these temperatures, but is still of the order of 10^{-5} to 10^{-6} for the fully saturated five-membered ring and 10^{-6} to 10^{-7} for the localized π -radical. This is a significant mole fraction and is considerably higher than the σ -radicals, suggesting that if chemical cross-linking reactions leading to larger PAHs and/or soot are to occur at these temperatures, such reactions should also consider localized π -radicals as potential reactants. At 1500 K, the mole fraction of the localized π -radical is stable at 10⁻⁷, with the mole fraction of σ -radicals being very similar and the mole fraction of the fully saturated product being only slightly higher. This suggests that even at 1500 K, the localized π -radicals could be as important as σ -radicals, even though the concentration is much lower than just the species with peripheral fivemembered rings. At the higher temperatures of 1800 and 2000 K, the unsaturated states are favored, with the reactant and σ -radicals being the dominant species as consistent with the trend. However, it can be seen that the mole fraction of σ -radicals at these temperatures is lower than what was observed for the π -radicals at lower temperatures.

Finally, a kinetic Monte Carlo scheme was developed to see if multiple localized π radicals could be present on a single PAH with multiple rim-based pentagons (Figure 4). The same flame compositions are used as in the previous simulations. The lowest temperature (1000 K) was used to consider the localized π -radicals as they are present in higher concentrations. 10000 reactant PAHs with two and three rim-based pentagonal rings were sampled in a fixed control volume so that reasonable statistics could be collected using the KMC model. In both cases two localized π -radical sites can be seen to form within 10^{-6} s. For the two-site species the concentration of both sites being localized π -radicals is just under half that for species with a single radical site. For the three-site model, similar concentrations of having one or two localized π -radical sites were found, with a quarter of that again having three radical sites. Comparing these results with the frequency of aromatic species imaged with HR-AFM [4] just prior to soot nucleation, from a total of 49 molecules with >4 rings; 28 contained at least one rim-based pentagonal ring, 12 contained two rim-based pentagonal rings and none of the imaged species contain three rim-based pentagonal rings. At least two reactive sites would be required to allow for a continuous mass accumulation into soot nanoparticles given a mechanism only involving ARLH. It should be mentioned that we also found that the localized π radical is able to form strong π -stacked complexes with the partially embedded rim-based pentagonal [15]. However, computing the concentrations of this site is outside the scope of this paper, as it requires detailed chemistry of PAH growth. The relative importance of π -radical versus σ -radical was also not explored due to the challenge of including van der Waals and possible curved PAH flexoelectric driven interactions for π -radicals in ARLH, which could significantly enhance the efficiency of reactions during collisions with flexoelectric species, which has been one of the challenges in σ -driven mechanisms [14]. Given these considerations it appears, from these preliminary results, that π -radicals on rim-based pentagonal rings have sufficient concentrations and reactivity to be important to fully explain soot formation processes.



Figure 4: *Kinetic Monte Carlo simulation for the time evolution of rim-based pentagonal rings for two (top) and three (bottom) site species at atmospheric pressure and typical flame compositions at 1000 K. These results are the average of five runs.*

4 Conclusions

Localization of π -radicals was found to be governed by aromaticity rules developed from a Clar analysis. The partially saturated rim-based pentagonal ring was found to concentrate significant spin density on the pentagonal ring and be unchanged by extension of the aromatic ring, as opposed to π -radicals formed within the six-membered ring networks which delocalize. A reaction mechanism was developed, allowing the concentration of possible localized π -radicals to be computed within flame conditions with significant concentrations found in soot-forming temperatures. Finally, kinetic Monte Carlo showed that multiple reactive sites can be formed on a single aromatic, suggesting a chemical polymerization could be possible. This will require further computational and experimental work to establish.

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Revision History

The spin density isosurface values presented in Figure 1 were updated on July 9th, 2020, as the original values were inaccurate in how the hydrogen spin densities were treated. The updated values have resolved this problem.

A Further information on rate calculations

In order to show that the kinetic mechanism demonstrated for acenapthalene-sized species scales to larger aromatic networks, some rates were also calculated for acecoronene (A7R5), a coronene molecule with a rim-based pentagonal ring attached to a zig-zag edge. Since the CBS-QB3 calculations have too large a memory requirement for a molecule such as acecoronene, the rates were computed using energies, geometries, and vibrational frequencies all taken at the B3LYP/6-311G(d,p) level of theory. In this case, we chose hydrogen abstraction from, addition to, and migration on A7R5, representing the three main categories of hydrogen–PAH reactions studied in this work. Figure S1 presents the Arrhenius plots of these three processes for A2R5 and A7R5. Little difference is seen between the smaller and larger aromatic rates. The hydrogen addition to the R5 site is seen to decrease slightly for the larger species at low temperatures where soot does not form. Hence, it is expected that the rates calculated for A2R5 in this work should scale for larger PAHs with rim-based pentagonal rings as well.



Figure S1: Temperature dependent rate constant for acenapthelene A2R5 and coronene A7R5 for some critical reactions in the reaction mechanism.

Figure S2 compares the three barrierless reaction rate constants computed using the RRKM theory framework and the simple Gorin model with those computed using the variational transition state theory (VTST) framework. The unimolecular decomposition rates were determined using these methods, and the radical recombination rate was determined from the equilibrium constant for the overall reaction. In the Gorin model, the internal motion of the transition state is given by the vibrations and rotations of the separated fragments of the product, and the potential energy between the separated fragments needs to be provided. In this case, the free-rotor approximation was used for the rotations of the loose transition states, and the potential energy surface was fit to a Morse potential:

$$E(r) = D_e [1 - \exp[-\beta (r - r_{eq})]^2, \qquad (A.1)$$

with D_e being the bond dissociation energy, r the reaction coordinate, r_{eq} the equilibrium distance, and β the steepness of the potential energy function.

For the VTST calculations, trial transition states were taken from a relaxed potential energy surface scan at the B3LYP/6-311G(d,p) level of theory, with the coordinate being the carbon-hydrogen bond distance. Frequencies and rotations were calculated for each trial transition state at the same level of theory, as were the energies of the trial transition states relative to the reactant. The H radical and PAH fragment energies were also set to be relative to the reactant. The numerical parameters for the energy and angular momentum density of states integration were taken from [1] and are essentially the default parameters, but little variance was seen in the rate constants based on these parameters. In general, we find the Gorin model overpredicts the rate constants compared with the more accurate VTST method, possibly because one of the fragments of the product (the PAH radical) is very large and similar to the reactant PAH. We expect the VTST method to give a reasonable first estimate for these rates. However, it is also known that the relative energies of the trial transition states are important, as are other potential reaction coordinates, meaning multireference methods for the interaction energies and more advanced frameworks [such as variable reaction coordinate-transition state theory (VRC-TST)] are likely necessary to give a more accurate estimate of the rate constants of these barrierless reactions.



Figure S2: Temperature dependent rate constant for the three barrierless reactions computed using the Gorin model and variational TST (VTST).

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