

Carbonaceous nanoparticle formation in flames

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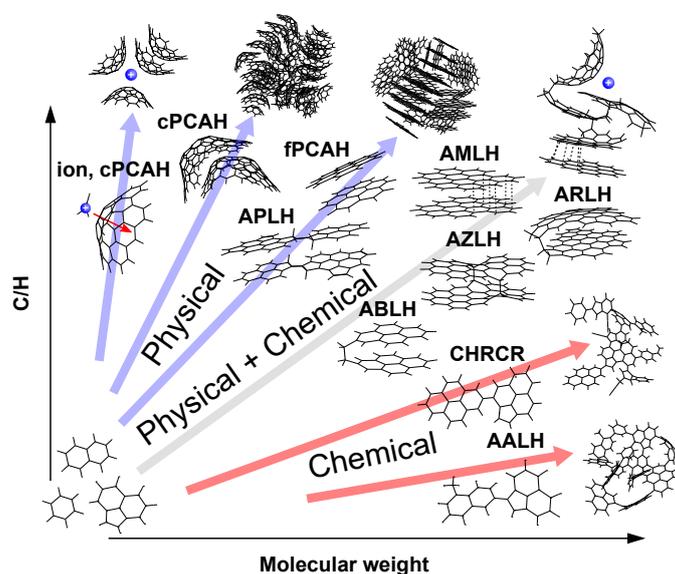
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Abstract

The route by which gas-phase molecules in hydrocarbon flames form solid carbonaceous nanoparticles is reviewed. These products of incomplete combustion are introduced as particulates and materials revealing both their useful applications and unwanted impacts as pollutants. Significant advances in experimental techniques in the last decade have allowed the gas phase precursors and the transformation from molecules to nanoparticles to be directly observed. These measurements combined with computational techniques allow for various mechanisms known to date to be compared and explored. Questions remain surrounding the various mechanisms that lead to nanoparticle formation. Mechanisms combining physical and chemical routes, so-called physically stabilised soot inception, are highlighted as a possible “middle way” with reactive aromatics activated by hydrogen of particular interest.



Highlights:

- The review is motivated by efforts to reduce harmful soot emissions and to control the nanostructure and synthesis of carbon black/nanodots.
- The formation of gas-phase precursor aromatics are reviewed identifying PCAH, aromers and clustering PAH.
- The formation of carbonaceous nanoparticles are reviewed focusing on the known chemical and physical mechanisms.
- Mechanisms combining physical and chemical mechanisms are highlighted with localised π -radicals of particular interest.

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1 Introduction

The carbonaceous products of incomplete combustion have fascinated and frustrated many. Interest in their illumination, pigments and heating gave way to dissatisfaction as they filled our cities with toxic air. This review attempts to capture this fascination and frustration by examining one of the least well understood aspects of incomplete combustion, the self-assembly of gas-phase molecules into carbonaceous nanoparticles.

This review is written for three main fields: combustion science, aerosol science and chemical engineering. Combustion science is concerned with understanding the physical and chemical processes involved in flames, of interest to many of the great scientists. Michael Faraday wrote, in his famous set of public lectures on the chemical history of a candle [138],

‘There is not a law under which any part of this universe is governed which does not come into play, and is touched upon in these phenomena. There is no better, there is no more open door by which you can enter the study of natural philosophy, than by considering the physical phenomena of a candle.’

Indeed many doors have been opened by the study of flames, allowing for an unprecedented understanding of chemical kinetics and physical processes. However, the formation mechanism of carbonaceous particles in hydrocarbon flames has remained a perennial unsolved problem in the field, although not for lack of effort (see the many detailed reviews written over the last two decades – Richter and Howard in 2000 [420], Frenklach in 2002 [149], McEnally, Pfefferle, Atakan and Kohse-Höinghaus in 2006 [336], the book edited by Bockhorn, D’Anna, Sarofim and Wang in 2009 [39], D’Anna in 2009 [98], Wang in 2011 [511], Haynes in 2019 [194], Frenklach and Mebel [152] with some recent reviews focusing on experimental aspects by Hansen, Cool, Westmoreland and Kohse-Höinghaus in 2009 [187], Li and Fei Qi in 2010 [295], Desgroux et al. in 2013 [111], Fei Qi in 2013 [407], Niessner in 2014 [384], Kittelson and Kraft in 2014 [256], Michelsen in 2017 [349], Wang and Chung in 2019 [518] and Baldelli, Rogak et al. [18], as well as a recent glossary of soot nomenclature [351]). It has only been in the last decade, however, that experimental and computational techniques in combustion science have been able to peek behind the door to reveal insights into the earliest formation mechanisms of carbonaceous particulates in the flame.

To clarify the problem, carbonaceous particle formation is separated into four main steps and provide a schematic (see Figure 1 based on a schematic by Bockhorn from 1994 [37]):

1. Precursor formation
2. Nanoparticle formation
3. Primary particle formation
4. Aggregate formation

These steps are not strictly distinct but overlap and influence each other (for example, nanoparticles grow into primary particles). However, a distinction is made between nanoparticles and primary particles for the following reasons. Firstly, many of the smallest

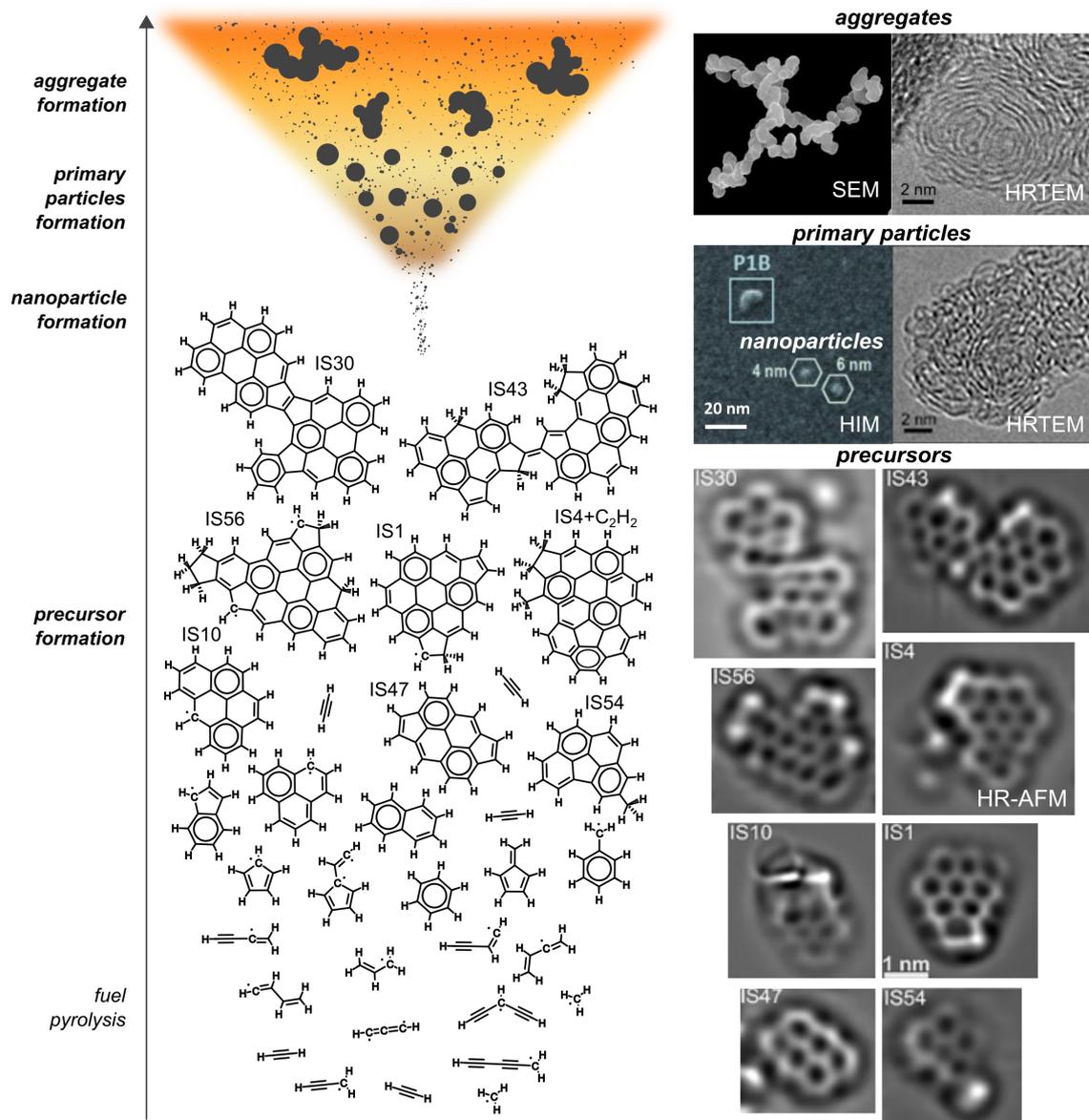


Figure 1: Schematic of carbonaceous particulate (soot or carbon black) formation in flames. Fuel pyrolysis and single ring species from Hansen et al. [187], Johansson et al. [234]. Multiring aromatic structures from Commodo et al. [88]. Nanoparticles imaged with HIM are shown from [437]. Primary particles are also shown in the HIM as well as with HRTEM [323]. Aggregates are shown with SEM for a lamp black particle (Orion carbons) as well as HRTEM of a primary particle [323].

nanoparticles have very low coagulation efficiencies and are therefore readily emitted alongside larger particles [212, 298, 399]. Secondly, evidence has recently emerged for non-spherical primary particles, indicating coagulation of nanoparticles [437]. Finally, flames can be established which are dominated by nanoparticles [112]. We have also made use of the recent extensive review of soot nomenclature [351]. However, we will

use the term carbonaceous nanoparticles for early soot particles to bridge the combustion, materials and aerosol terminology [98, 133, 141, 238, 242, 363, 374]. This follows efforts to avoid mechanistic language when discussing soot formation and allows for a discussion of variously sized or charged species on the nanoscale. Further details are provided throughout concerning the nomenclature.

For aggregate formation the terminology for carbon blacks is used (quoted from the ASTM D3053 standard with italicised term added by the authors),

‘Carbon black exhibits aciniform (*grape-like*) morphology composed of spheroidal “primary particles” strongly fused together to form discrete entities called aggregates. The primary particles are conceptual in nature, in that once the aggregate is formed the “primary particle” no longer exists, they are no longer discrete and have no physical boundaries amongst them. The aggregates are loosely held together by weaker forces forming larger entities called agglomerates.’

Soot, unlike carbon black, most commonly contains a significant hydrogen content in the primary particles [483], often also with condensed aromatics on the aggregates (called mixed soot [44]) which has implications for human health [297]. Carbon blacks are thermally treated to near complete carbonisation (loss of heteroatoms leaving a disordered carbon solid) with minimal health impacts [320]. We refer the reader to the recent excellent reviews [18, 250] on the carbonisation of soot as it takes on a shell [52], maturing into a carbon black once hydrogen is fully evolved, but we will not discuss this further.

Aerosol science is concerned with the combustion products as particulates, which are particles suspended in the air. Soot is particularly problematic as an aerosol, posing significant risk for human health and the climate [44]. Chemical engineers are then often tasked with eliminating these emissions. This requires a comprehensive and complete understanding of the process. The problem was most clearly articulated by Palmer and Cullis in 1965 [390],

‘A major breakthrough in understanding carbon formation will have been achieved when it becomes possible in at least one case to account for the entire course of nucleation and growth of carbon on the basis of a fundamental knowledge of reaction rates and mechanisms.’

Since this was written, scientific advances have allowed for this problem to be partially resolved – models do exist for specific cases. Simple kinetic models, considering acetylene concentrations, allowed the mass of soot emissions to be reproduced [245], but particle numbers were predicted incorrectly. Computational simulations coupled with kinetic experiments in the 1970s and 1980s allowed for models to be developed that considered different nucleation species in detailed chemistry models [228]. It was only in the late 1980s to early 1990s that combining a kinetic mechanism for PAH growth (HACA - Hydrogen Abstraction Carbon Addition) and an irreversible dimerisation of aromatic species allowed particle number to be captured [153, 329–331, 512], with one of the most popular implementations (ABF mechanism) published in 2000 [13] (differing minimally from ref. [512]). This soot model was able to reproduce many experimental observations such as the equivalence ratio threshold ($\phi > 2$) and the low (~ 1450 K) and

high temperature thresholds for soot formation (so-called "soot bell curve" or "soot island") [42, 154, 167, 172, 491]. It is important to note that irreversible dimerisation is an empirical model in that by fitting model parameters to particular experimental 'cases' reasonable nucleation rates can be attained. However, for a new combustion system it is rarely predictive.

Attempts to provide such a predictive model for nanoparticle formation have focused on developing more detailed models. Kinetic mechanisms can now be automatically generated for many reaction classes in combustion chemistry (*e.g.* RMG - reaction mechanism generator [158]) and some PAH mechanisms now allow growth of large PAH (up to coronene) [412, 467]. For larger PAH, kinetic Monte Carlo simulations allow the formation of curved aromatics [148, 156, 291, 410, 526–528, 539] as well as crosslinks [100, 286, 505]. Particle dynamics such as coagulation, growth, oxidation and fragmentation can be computed with stochastic approaches, allowing the particle size distribution to be modelled [19, 458, 548]. However, these attempts have not improved our predictive power significantly due to the lack of understanding concerning nanoparticle formation. In fact, experimental and computational work from the last decade has shown that irreversible dimerisation of pyrene at flame temperatures cannot occur [427, 489, 511], with no alternative mechanisms proving any more useful. This leads us to restate our comment from 2014 that [256],

‘None of the existing soot models have predictive power.’

Until a fundamental understanding of the mechanism (or mechanisms) of soot nanoparticle formation is found, developing a predictive models to control or eliminate carbonaceous combustion products will prove futile.

The purpose of this paper is to review the molecule-to-particle transition in detail with a focus on the precursors formed and the nanoparticle mechanisms.

Section 2 explores the detection of nanoparticles as well as the health, climate and material motivation for understanding this mechanism. Much of this extended introduction can be skipped by readers who are already familiar with the field, however the experimental results for nanoparticles will be critically discussed throughout the rest of the document and therefore Section 2.1 is recommend reading. The discussion about mixed soot in Section 2.2 is also important when discussing liquid-like mechanisms for nanoparticle formation.

Section 3 begins the main text with a review of the formation of molecular precursors. The use of sooting propensity scales are briefly discussed, highlighting the important role of aromatic species and 5-membered cycles. Formation of pericondensed aromatic hydrocarbons through traditional growth pathways is then explored with recent insights into detection of pentagonal ring-containing PAH. Larger PAH (aromers) formed through crosslinking are then discussed with a focus on the previous difficulties in their detection and their chemical structure, which has recently been exposed. The final precursors discussed are the PAH that cluster to form soot. This section on precursors therefore provides the necessary understanding of the molecular species present in the flame before nanoparticle formation begins.

Section 4 provides a systematic comparison of formation mechanisms for soot nanopar-

ticles. This section has been arranged in a similar manner to Bansal and Donnet's 1993 book 'Carbon Black' [119] but is significantly updated and partially restructured. The reasons for providing this comprehensive overview of mechanisms are recent new insights and the resurfacing of old mechanisms. It does, however, give the impression that the mechanisms are disjointed so we have therefore added a section combining physical and chemical mechanisms, which we argue best describe the partial success of the "irreversible dimerisation" models proposed in the literature.

Finally, Section 5 summarises the mechanisms and experiments, redrawing many important historical plots with the insights from the last decade. An outlook is provided for further scientific and technological directions required to resolve the formation mechanism of carbonaceous nanoparticles in the flame.

2 History and motivations

This section introduces the many nanoparticles in combustion systems and provides the motivations for understanding the formation of carbonaceous nanoparticles. The experimental finding concerning carbonaceous nanoparticles in combustion flames will be introduced, drawing on recent reviews [18, 98, 111, 349, 511]. Some motivations for this study from both a human health and climate perspective will be discussed, also drawing on recent reviews [44, 174, 198, 227, 297, 299, 352, 353, 379, 532]. Finally, recent material applications are discussed.

2.1 Detection

Particles down to a nanometre in size were initially observed via electron shadow microscopy by Wersborg et al. [524] in 1973. Laser scattering also indicated nanoparticles two years later [94]. Some of the first nanoparticles to be quantitatively detected in the flame were positively charged species with molecular weight of order $10^3 - 10^4$ Da, found in low pressure flames [209]. Small, positively charged molecules are known to form in flames through chemionisation reactions, therefore the presence of charged soot nanoparticles is not surprising [192] (at this stage they were not referred to as nanoparticles but as early soot particles). Their size was limited to below 10^5 Da [25]. Higher sensitivity nanoparticle detectors have recently found the majority of these sub 1 nm particles to be positively charged [64, 536]. However, in sooting flames the charged nanoparticle modes that are present quickly coagulate with electrons and small charged species to form neutral particles [143, 514].

In 1985, the C_{60} buckminsterfullerene molecule (see Figure 13) was discovered by laser ablation of a graphite target [277] and two years later in low pressure benzene flames [164]. Since this time their combustion synthesis has been developed into a commercial technology (NanoC) generating kilogram scale of magic number fullerenes, for example C_{60} and C_{70} , that have found applications in many fields such as organic solar voltaics and medicine [41, 168, 178, 215]. Significant controversy has surrounded the role of fullerenes in soot formation. The formation of fullerenes in flame will not specifically discussed

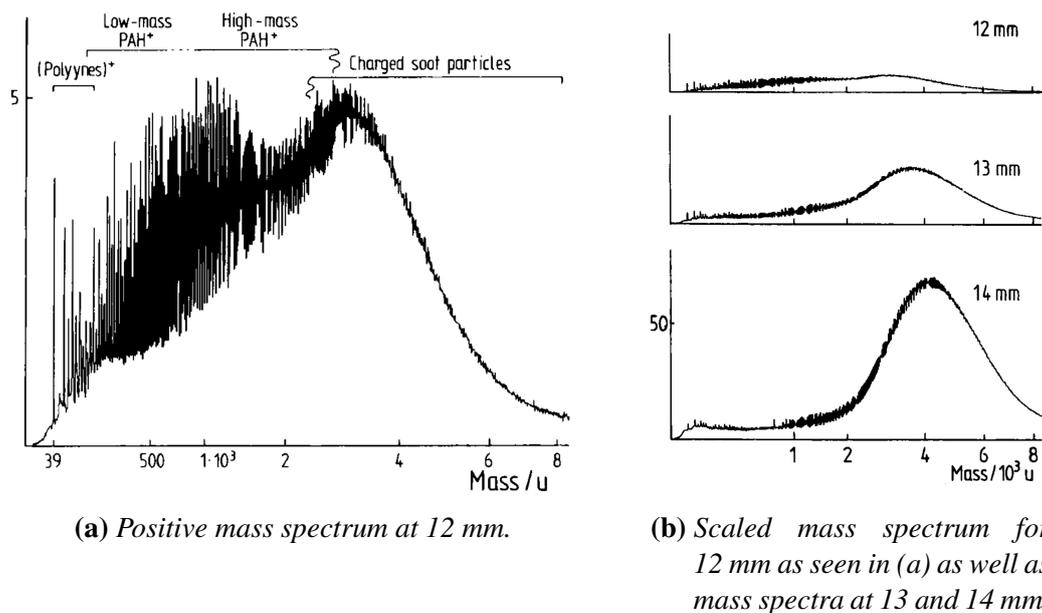
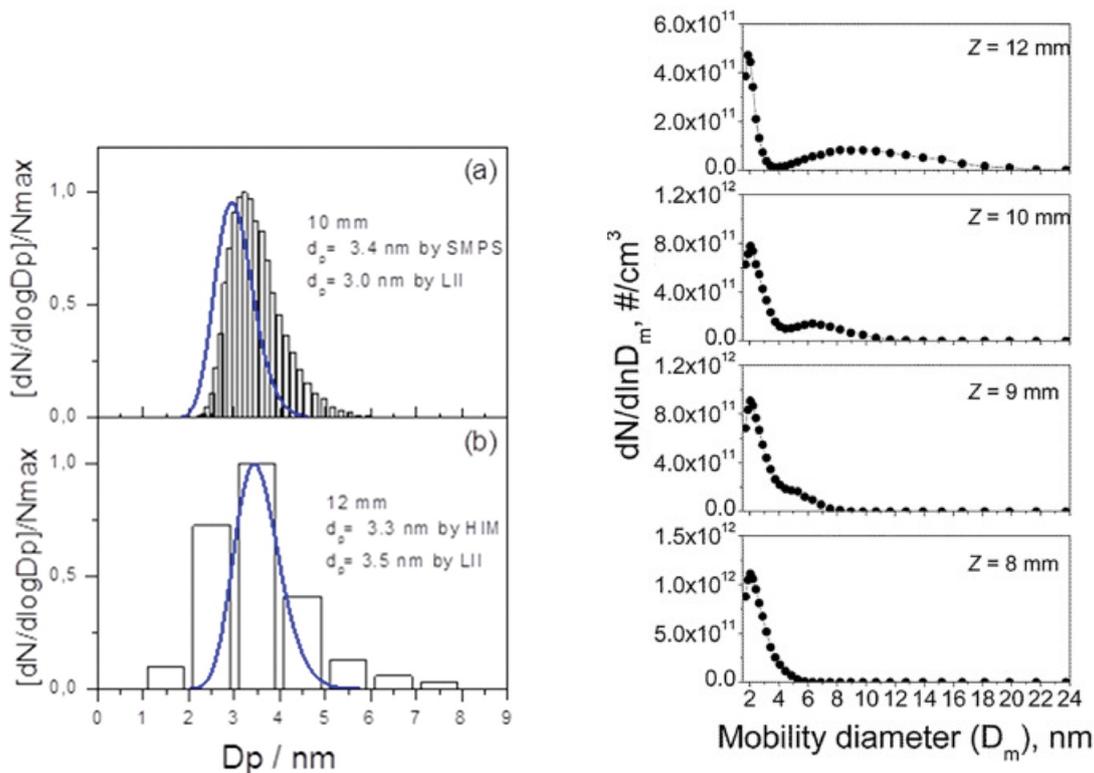


Figure 2: Positive ion mass spectrometry of an C_2H_2/O_2 low pressure flame $p = 2.7$ kPa at various heights above the burner [25]. Used with permission from John Wiley and Sons ©.

(see the reviews [208, 366, 422]) but will focus on their role in the formation of larger carbonaceous nanoparticles. Graphene or giant aromatic molecules can also be formed in some particular operating conditions of low pressure acetylene flames [208]. Microwave heating has also been shown to allow graphene synthesis in flames at atmospheric conditions [378, 459]. Flame synthesis of graphene in the gas phase has yet to be developed into a mature technology.

By the 1990s laser scattering and electron microscopy had established that larger (~ 2 nm) incipient nanoparticles were present in all sooting flames [95, 117, 125]. Atomic force microscopy allowed for the direct measurements of these nanoparticles [21, 84, 86] (see Figure 5). These nanoparticles were shown to form at an equivalence ratio just below or close to values where soot primary particles or aggregates form [21, 67, 482]. All sooting flames, including aromatic fuels such as benzene flames, were found to possess this mode near 2 nm, which will be referred to as *incipient nanoparticles* in this review [101]. Desgroux and co-workers have studied so-called *nucleation-dominated flames* [31, 36, 112, 221, 373]. Nucleation-dominated flames allow nanoparticles to nucleate but surface growth and coagulation appears marginal, with oxidation dominating, meaning the soot mass increases only by nucleation from the gas phase [112, 373]. These flames can be stabilised at atmospheric and low pressure flames for methane, ethylene and *n*-butane [31, 36, 112, 373] (see Figure 3a).

Evidence for nanoparticle >4 nm was also found. Grotheer and colleagues developed a time of flight reflectron mass spectrometer able to measure millions of mass units [180] and in 2007 they showed that aromatic molecules right through to nanoparticles with millions of mass-to-charge values could be detected using photoionisation [20, 189, 190]. Figure 3b shows similar results from nano differential size mobility analyser (nano-DMA) [83,



(a) Normalised particle size distributions measured by 1 nm-SMPS (a) bars), HIM (b) bars), and LII (blue line) in an *n*-butane/ O_2/N_2 $\phi = 1.75$ premixed flame [31]. (b) Particle size distribution measured on a Vienna style nanoDMA in an C_2H_4 /air premixed flame [88].

Figure 3: Used with permissions from Elsevier©.

448], which also was shown with scanning mobility particle sizing (SMPS) [476]. This figure shows nanoparticles increasing in mass to form primary particles. We will refer to nanoparticles > 4 nm mode as *primary nanoparticles*. Helium ion microscopy and electron microscopy have provided evidence for nanoparticles down to 4 nm in size showing their development into primary particles, shown in Figure 5b) [437]. This study also revealed primary particles' non-symmetric structure indicating they form, at least partly, through coagulation of smaller nanoparticles.

Some evidence has emerged for structural or chemical differences between the incipient and primary nanoparticles. Grotheer found that the photoionisation process was a two-photon process for incipient nanoparticles and a single-photon process for primary nanoparticles [181]. The two-photon process indicated that smaller aromatics are the constituents of the incipient nanoparticles [111]. These smaller nanoparticles also lack visible light absorption when measured by laser spectroscopy, suggesting small aromatics with only a few aromatic rings [96] and leading some to label these incipient nanoparticles as "transparent" or nanoorganic carbons (NOC) [126]. The incipient nanoparticles were found to be stable under infrared laser absorption (1064 nm), while the primary nanoparticles fragmented with a laser fluence of 1–3 mJ/mm². Higher laser fluences (10 mJ/mm²) were found to generate fullerene ions [181]. (It is important to note that fullerenes are

not present in the flame at high concentration but in these experiments are products of the rapid heating of soot, which is well known to lead to significant carbon vapour [170, 422].) IR pulsed laser ablation is known to significantly modify aggregate soot nanostructure, through carbonisation (hydrogen removal), partial graphitisation (thermal transformations towards graphitic structure) [498] and fragmentation [350]. However, recent optical studies indicate only slight differences between the molecular units involved in incipient and primary nanoparticles [109]. Instead the supramolecular organisation was suggested to be the distinguishing feature between these nanoparticles.

Figure 4 shows this fluorescence, which has been observed since the 1980s when rare gas plasma lasers became available [78, 115, 159, 193]. Initially, this was seen as a response from the individual molecules as PAH are known to fluoresce [473]. However, the signal extending well into the visible spectrum suggested an excimer origin. Excimers are long-lived optical states that are formed from the delocalisation of the $\pi-\pi^*$ excited state across both stacked aromatic species, and are present in the fluorescence spectra of PAH dissolved in liquids [34, 204].

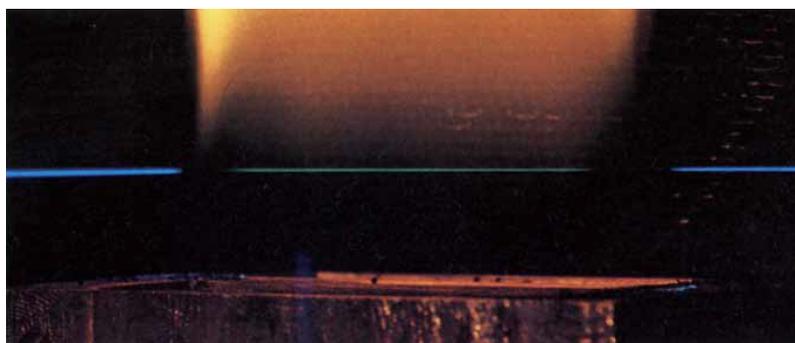


Figure 4: *Green fluorescence from UV laser excitation (top) [159]. Used with permission from Springer Nature America ©.*

Time resolved laser induced fluorescence (TR-LIF) experiments have established that this green fluorescence signal belongs to excimers [346, 464]. Excimer states are long-lived (tens of nanoseconds) and TR-LIF confirmed such long-lived states for signals in the range 500–600 nm. Critically, the excimer signal reveals that physically bound, stacked aromatic species are present during soot formation. In Section 3 another change in the flame chemistry is shown with the transition from a nucleation domination flame with larger aromatic species being observed [112].

There is still no consensus on the naming and number of distinct nanoparticles [351] and we do not see a resolution of these issues until the mechanisms involved can be fully understood. Maximally there is evidence for five nanometre-sized species that can exist in various combustion environments;

- *Charged nanoparticles* (~ 1 nm)
- *Fullerenes* (~ 1 nm, polyhedral carbons)
- *Graphene* (> 1 nm, nanographenes, giant polycyclic aromatic hydrocarbons)

- *Incipient nanoparticles* (<4 nm otherwise called transparent nanoparticles, nanoorganic carbon – NOC, D’Alessio nanoparticles, precursor nanoparticles, soot nuclei, nascent soot, disordered)
- *Primary nanoparticles* (>4 nm otherwise called stacked nanoparticles, growth precursors, soot nuclei, Dobbins nanoparticles, nascent soot)

It is important to mention that many of the naming conventions of nanoparticles are directly associated with the mechanism or model of growth that is thought to occur, thus our reason for choosing the more neutral names of incipient and primary nanoparticles. We will return to the nomenclature of nanoparticles at the beginning of Section 4.

2.2 Unwanted particulates

Particulates are an aerosol of particles suspended in the air and are usually undesirable in the context of aerosol/climate science. It is important to outline some semantics when discussing combustion products as particulates. The use of nanoparticles in the aerosol community often refers to all ultrafine particles (<100 nm). We will follow the nomenclature from the combustion community that predominantly refers to these smallest particles (<10 nm) as being called the nanoparticle mode (Nano) or nucleation fraction PM0.01 [98, 297].

To further aid our discussion of the range of combustion products emitted as particulates we have prepared Figure 5. The majority of combustion products fall below 2.5 μm (PM2.5 or fine fraction) and have significant negative health impacts [15, 169]. Most primary combustion emissions just below this range are soot aggregates (see Fig 5c). As mentioned these are fractal-like arrangements of smaller carbon spheres (called “primary particles” in combustion and “nodules” or “spherules” in materials science). These primary particles are chemically connected to their neighbours, forming a solid aggregate, as opposed to physically connected soot agglomerates (see Figure 5f). Figure 5c) – d) shows the soot emitted from a heavily sooting ethylene flame revealing that with increasing fuel-rich conditions, unburnt hydrocarbons will condense on the soot aggregate. This forms a “mixed soot” of black carbon (highly carbonised primary combustion product) and brown carbon (collection of unburnt hydrocarbons and small aromatic species) [44, 453]. Even larger brown carbon spheres of condensed unburnt hydrocarbons (often called “tar balls”) can form [68, 312]. They are produced from smouldering fires such as agricultural fires. Recent work using high resolution mass spectrometry showed this brown carbon is made up of a large proportion of oxygenated and unsubstituted PAH. These species have the mean molecular mass of benzo[a]pyrene as well as some aliphatic structures with aromatic cores [525]. We will return to the mixed soot with unburnt hydrocarbons when we discuss liquid-like mechanisms in nanoparticle formation.

A further complication arises when comparing the various aerosol modes found in the literature. Often the terminology “nuclei”, “accumulation” and “coarse” modes are borrowed from atmospheric science when discussing engine emissions. Unfortunately, these modes refer to water condensation with the accumulation mode referring to water droplets in the atmosphere. The “nuclei” mode is usually defined as <100 nm or ultrafine PM0.1

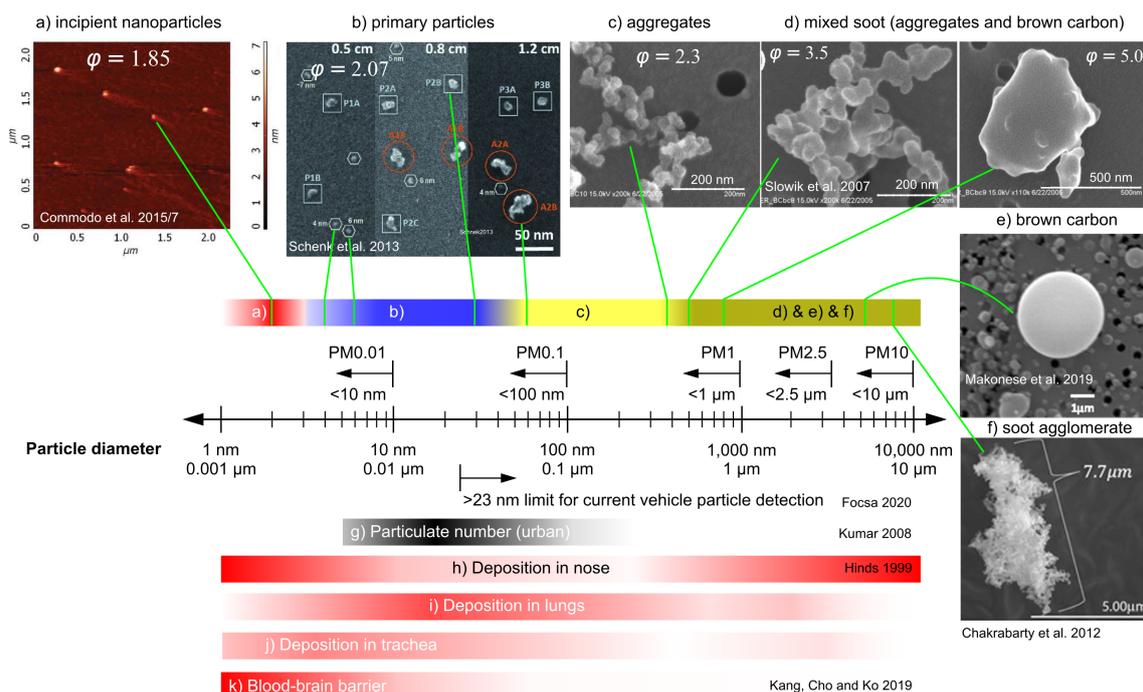


Figure 5: a) – d) Various combustion products sampled from a McKenna burner with an ethylene/air atmospheric pressure flame with varying equivalence ratio. Imaging performed using a) AFM [84], b) HIM [437] and c) SEM [468]. e) – f) Combustion products from solid combustion of coal [312] and biomass [68], respectively, imaged using SEM. g) Particle number distribution in an urban environment [280]. h) – k) Deposition of nanoparticles within mammals from inhalation [200, 239].

and constitutes most of the soot particulates emitted in the urban environment (see Fig 5g). It could be argued that the condensed aromatics and hydrocarbons lead to a similar accumulation mode in the exhaust of diesel engines, which can be demonstrated by solvent extraction or with a particle thermal denuder [6, 480]. However, as can be shown this condensed brown carbon and mixed soot can span many orders of magnitude and do not necessarily correspond to the range of aerosols found for water droplets in the atmosphere. In short, the “nuclei” mode discussed in aerosol science often refers to water nuclei and not soot nuclei, which are one to two orders of magnitude smaller in diameter.

Many detailed reviews on the health impact of combustion products have been conducted over the past two decades [174, 198, 205, 227, 287, 297, 299, 352, 353, 360, 379, 439, 532] and therefore only a cursory discussion will be provided. We will highlight at the outset, however, that the health impacts of the nanoparticle mode are still not well understood or widely measured [399]. The carcinogenicity of soot and diesel exhaust particulates has been mainly associated with the small aromatic molecules that are present in the brown carbon fraction [17, 47, 417] (such as naphthalene, acenaphthylene, acenaphthene, fluorene, phenanthrene, anthracene, pyrene and the particularly active benzo[a]pyrene). Figure 5h) – k) shows the deposition of particles as a function of size [200, 239]. It is clear that the nanoparticles are able to penetrate further into the lungs and translocate

from the lungs into the circulatory system in animals and humans [361, 362] while carrying carcinogenic aromatics [46]. (For engine emissions, other species such as sulfur or transition metals could also adsorb onto the surface of the nanoparticles and may further contribute to their reactivity and oxidative potency.) These nanoparticles have higher surface area to mass ratios compared with larger particles [98, 257]. Due to these large surface areas, nanoparticles are very potent inducers of oxidative stress [46, 367, 535]. Once in the bloodstream they can lead to cardiovascular disease such as heart attacks and strokes due to plaque build-up [114]. There is also evidence that the smallest nanoparticles readily cross the blood-brain barrier in mammals (rodents) [239], causing an inflammatory response and impacting development [8]. *In vitro* toxicological studies have shown that once in the organs, PM_{0.01} are taken up by cells causing toxicity and mutagenicity [399, 449, 451]. Various studies have also found a significant amount of oxygen on the nanoparticles' surfaces [59, 221, 438] which is correlated to their hydrophilic character [85, 451]. This hydrophilic character leads to partial water solubility, which is cause for concern in human health and suggests an additional impact on the climate through cloud seeding [451]. Black carbon is already implicated in 1.1 W/m² [44] of climate heating, potentially matching methane's contribution to global heating. Brown carbon has a cooling impact on the atmosphere that offsets the warming caused by black carbon in most agricultural burning [44]. Industrial sources of carbonaceous emissions, on the other hand, are predominantly black carbon and are therefore important to eliminate. These detrimental effects depend on the chemical and structural composition of the nanoparticles, so it is critical that we understand the formation mechanism of these particulates.

Nanoparticles (PM_{0.01}) are emitted by combustion systems, including vehicles, industrial burners and indoor combustion sources like cookstoves/heaters, which are a significant source of airborne nanoparticles [257, 297, 364, 423, 465, 538]. Significantly lower coagulation efficiencies were found for the incipient nanoparticles compared with primary soot particles and have been demonstrated to be emitted from combustion devices [447]. Particularly concerning is that many devices operating with a blue flame, such as natural gas domestic burners or cookstoves, are producing these nanoparticles [364, 399]. The emission of these nanoparticles can be explained by the decreasing physical interactions between nanoparticles below 5 nm leading to low coagulation efficiencies at flame temperatures [212]. The low interaction energy between incipient nanoparticles was confirmed with atomic force microscopy (AFM) studies showing the van der Waals interactions of these particles are decreased compared with primary soot particles [447]. Preliminary work shows that aftertreatment systems are only able to remove 40–50% of particles below 10 nm [463]. Another issue to consider is that fuels which are known to decrease the mass of soot emissions can increase the number of nanoparticles formed, for example biodiesel [313, 465]. Recently, the effective removal of these nanoparticles has been achieved using fibrous and granular activated carbon filters [253]. Challenges still exist for the detection of nanoparticles [144, 258, 259, 509]. Current regulations for the number of particles emitted from vehicles are based on instruments that are only able to measure down to 23 nm reliably [144, 517, 550]. This will be discussed further in Section 5.

2.3 Useful materials

Carbon blacks are an old material and yet many new applications are being found for them that rely, critically, on their formation and chemical composition. Examples include conductive carbon black for electronics and battery applications, such as in lithium ion batteries. Some applications that have yet to become widely used include electrodes in dye sensitised solar cells [376], fluorescent carbon nanodots [300] and coherent spin systems for quantum computing [382]. Understanding the earliest stages of carbonaceous particle formation would be beneficial for chemically tuning the properties of carbon blacks. This could provide the means to increase the yield of carbon blacks, thus reducing CO₂ emissions. Smaller particles could be produced by understanding particle formation, which can be useful for applications where high surface area is required.

Useful fluorescing carbonaceous quantum dots have also recently been synthesised in flames. As previously mentioned, visible fluorescence is present within sooting flames [159] (see Figure 4). Yet fluorescent nanoparticles were only recently extracted by Liu et al. in 2007 [301]. This was achieved by various acid treatments of candle soot and a size separation using gel electrophoresis to provide nanoparticles with a variety of fluorescent emissions from blue to red (see Figure 6).

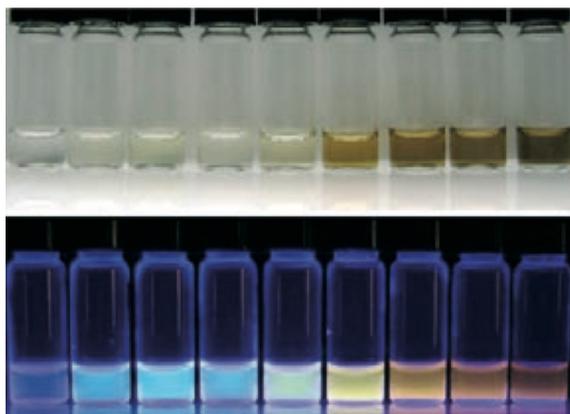


Figure 6: Carbon nanodots illuminated using ordinary light and UV revealing various fluorescence emissions as a function of size [301].

A simpler solvent-based method was developed using size exclusion chromatography showing similar results [426]. Recently, a one step method was developed by adding various amounts of benzene to a premixed ethylene flame; a single extraction allowed for nanoparticles from blue to yellow to be produced [466]. Raman spectroscopy suggested this tunability was achieved by increasing the size of the aromatic structures within the nanoparticles. Evidence has also mounted for tunability through the nanoparticle diameter [70, 108, 300, 507] (see Figure 7).

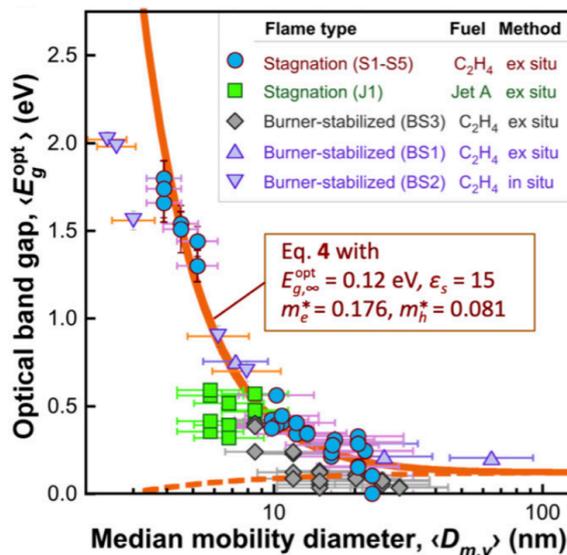


Figure 7: Optical band gap of flame-formed CNPs at room temperature with the expected behaviour of quantum confinement (shown as the solid line) [300].

3 Precursor formation

This section will concentrate on the most important precursors for soot formation, polycyclic aromatic hydrocarbons. Other species that were historically suggested as direct soot precursors to incipient soot nanoparticles including diatomic carbon, carbon monoxide, acetylene, polyynes and chemi-ions will be discussed in Section 4.

3.1 Pericondensed aromatic hydrocarbons (PCAH)

In 1825, Faraday demonstrated the significant sooting propensity of aromatic fuels such as benzene, even as he isolated benzene for the first time [137]. The sooting propensity can be illustrated by considering a simple diffusion pool flame (Figure 8), remembering that soot provides the luminosity of the flame (incandescence). For the benzene fuel, soot is rapidly formed at low heights above the burner, but for an aliphatic fuel such as hexane, a “dark zone” is observed that indicates a delay in soot formation [162]. This “dark zone” implies that the aliphatic fuels must be broken down into soot precursor species before becoming soot.

The diffusion flame has been used extensively to assess the sooting propensity of chemicals and fuel blends (see Dryer’s 2015 review for a comprehensive discussion [122]). For example, the height reached by a diffusion flame without soot emission occurring (smoke point height) has been a staple of measuring sooting propensities since the beginning of the 20th century [248, 436, 477] (developed into the ASTM D1322 ‘Standard Test Method for Smoke Point of Kerosene and Aviation Turbine Fuel’). Calcote and Manos in 1983 combined various literature data into a burner agnostic scale – the Threshold Sooting Index (TSI) [60]. Critically, it was found that binary mixtures would follow a linear mixing rule with TSI [165]. (This metric has been extended to oxygenated biofuels

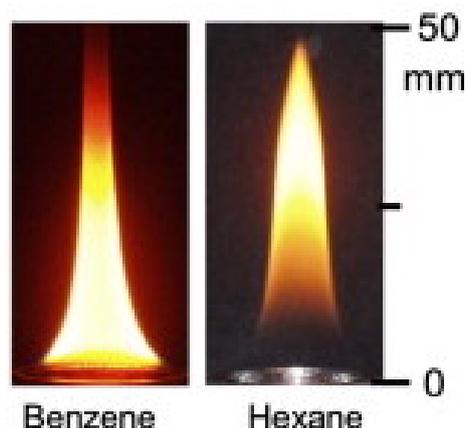


Figure 8: *Diffusion pool flame benzene and hexane fuels* [263].

with the Oxygen Extended Sooting Index (OESI) [22], which we will not be discussing in this review.) A theoretical method proposed by Sarofim's group allows prediction of the smoke point of pure hydrocarbon liquids from low-sooting paraffins to highly sooting aromatics; the method was based on structural group contributions [533]. We have recently improved the accuracy of such methods by considering the fuel flow rate as a function of flame height – the so-called fuel uptake rate measurement with threshold imaging (FURTI) method [520]. Independent work confirmed the suitability of this method [309] and further improved the threshold image processing [175]. Another approach is measuring the soot volume fraction using optical approaches such as the yield soot index (YSI) [103, 334]. In the YSI method a methane co-flow diffusion flame is doped with a small amount of the species of interest and the maximum soot volume fraction is measured. This methodology has been found to robustly determine sooting propensities allowing a wide range of species to be analysed, especially larger cyclic and aromatic species that have very low smoke point heights [334, 335, 368]. This model was also expanded to measure and predict the sooting tendency of oxygenated fuels [103]. A methodology was recently developed to improve the Abel transform required to determine the soot volume fraction using a low-cost two-colour pyrometry approach [121]. The micropyrolysis index (MPI) [92, 490] and particle size measurements should also be mentioned for determining sooting propensity [50]. Across the indices the ordering of the sooting propensities follows aromatics > unsaturated aliphatics > saturated aliphatics > oxygenated aliphatics [103, 297, 336]. These results show the critical role fuel structure plays in soot precursor formation. For further discussions we refer the reader to the excellent review by McEnally, Pfefferle, Atakan and Kohse-Höinghaus [336] in which important chemical concepts for fuel decomposition and aromatics formation such as bond energies, resonantly stabilised radicals and unimolecular dissociation of hydrocarbon radicals are explained, as are the decomposition products of several fuels. Several papers summarise new findings related to different kinds of fuels [23, 187, 265, 295, 296, 407] and the development of new techniques for new species to be identified in the fuel decomposition [233, 264, 481, 519]. These results show that aromatic species are critical intermediates of nanoparticle formation. The similarities between many aliphatic fuels also suggest similar thermal fragmentation (pyrolysis) routes to C1–C5 compounds, includ-

ing acetylene (C_2H_2), through radical-induced fragmentation to species that subsequently grow into aromatics.

The formation of the first unsaturated ring is of fundamental importance for understanding the formation of polycyclic aromatic hydrocarbons (PAHs) and soot in aliphatic fuels. The formation of benzene and small aromatics has been reviewed previously [35, 149, 264, 336, 420] and three main reaction routes proposed for the formation of the first aromatic PAH, benzene (see Figure 9). The first reaction involves the presence of C_2H_2 , whereas the others involve resonantly stabilised radicals. In all cases the formation of benzene comes from a sequential addition of small molecules. The acetylene pathway for benzene formation was proposed in the 1980s [35, 155] and has been studied in order to obtain appropriate values of the thermodynamic properties and rate constants of its reactions [340, 472]. This pathway has been found to be dominant at the medium-low temperature regime [151, 354]. Later in 1992, Miller and Melius [354] proposed the self-recombination of propargyl radicals (C_3H_3) as the key step in benzene formation. The reaction of two propargyl radicals is favoured over the radical-molecule reaction (C_4 radical + acetylene). The reason is that the competing oxidation reactions of C_3H_3 are slow due to resonance stabilisation [184]. Therefore, the propargyl pathway is the main mechanism for benzene formation with successive studies recognising this reaction to be predominant at high temperatures [79, 319]. Another proposed mechanism for the first aromatic ring formation is the cyclopentadienyl route, which is a combination of C2 and C3 pathways or the oxidation of aromatics. These radical reactions are in equilibrium; nevertheless, they lead to benzene ring formation that is highly stable due to aromaticity and in this way the reaction is promoted to the products [99, 420]. Recently, the reaction of cyclopentadienyl and acetylene to form tropylium, benzyl and vinylcyclopentadienyl has also been suggested to explain the formation of odd-numbered carbon species [234, 317] and methyl addition [549]. For a more detailed discussion of the early ring formation we recommend the 2020 review by Kohse-Höinghaus [264].

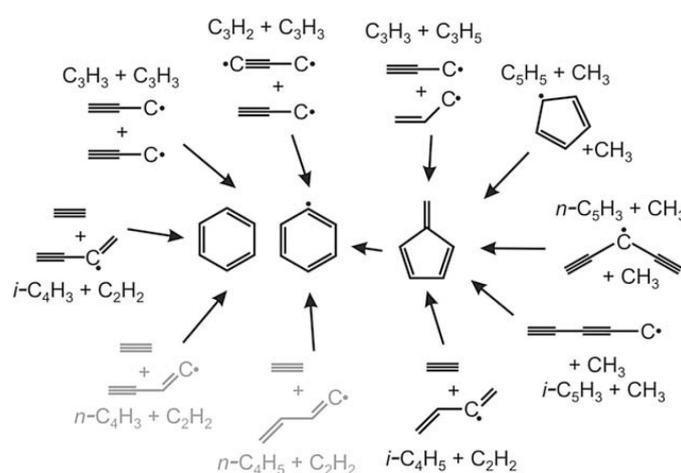


Figure 9: First aromatic ring formation from propargyl ($C_3H_3\cdot$), acetylene (C_2H_2), methyl ($CH_3\cdot$), cyclopentadienyl ($C_5H_5\cdot$) with other species possessing a variety of isomeric structures [187].

Further growth of the aromatics past the first ring proceeds predominantly by a radical

mechanism where a colliding hydrogen radical (or other radical) abstracts an aromatic hydrogen atom, providing a reactive site where acetylene can attach – the so-called hydrogen abstraction carbon (acetylene) addition (HACA) mechanism [149, 155]. Figure 10 shows one pathway that highlights the HACA mechanism, plotting the change in the free energy (at $T = 1800$ K, $P = 1$ atm) and showing a table of species consumed or produced by Wang [511]. The process is seen to be energetically downhill and spontaneous. This is primarily due to the generation of hydrogen gas which entropically drives the aromatic growth [511].

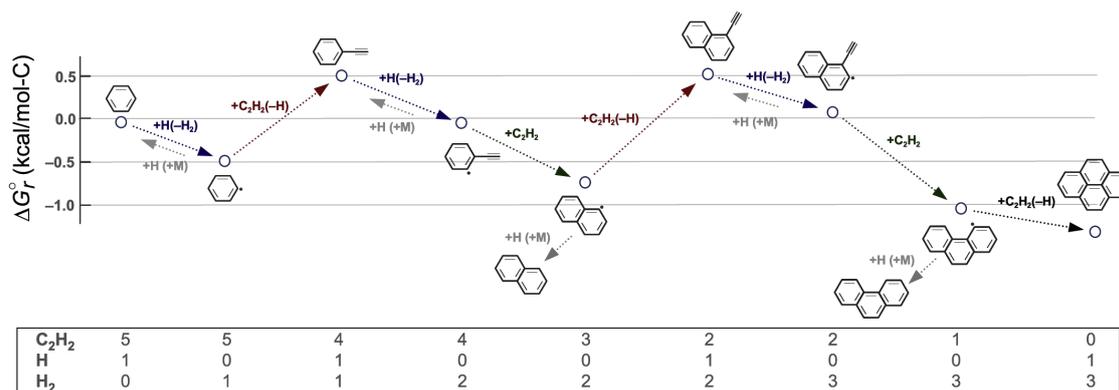


Figure 10: HACA mechanism with energetics of the intermediates and species count highlighting the release of H₂ [511]. Used with permission from Elsevier ©.

As the PAH grows, a variety of topological arrangements of fused aromatic rings are produced. Mass spectrometry allowed the ratio of the carbon to hydrogen (H/C ratio) in the PAH to be measured as $H/C = 0.3-0.5$ [208]. The reason for the presence of these species was explained by considering the thermodynamic stability of pericondensed polyaromatic hydrocarbons (PCAHA), revealing an “island of stability” or the “stabilomers” as described by Stein and Fahr, where aromatic rings are fused in a roughly circular fashion [475]. A lower H/C ratio was found than that from PAH with only hexagonal pericondensed rings (maximally pericondensed structures) and explained by the presence of pentagonal rings. Evidence for pentagonal rings has recently been found from tunable photoionisation mass spectrometry, which makes use of synchrotron light sources [231, 234, 347]. For example, many molecular formulas that were historically associated with only 6-membered ring structures were found to be a mixture of isomers with many pentagonal rings. For example, the ion with m/z 202 usually associated with pyrene has been found to be composed of a variety of pentagonal-containing species, such as fluoranthene [231, 234, 347]. Heptagonal rings can also be integrated for specific bay closure reactions next to partially embedded pentagonal rings [292, 343]. This indicates kinetically driven pathways play an important role in PCAHA formation and mechanisms that only consider the most thermodynamically stable 6-membered species are incomplete.

Finally, it is interesting to compare the concentration of PCAHA with that of soot. It has long been known in mass spectrometry that the concentration of PCAHA decreases exponentially with mass [38, 206]. This allows the mole fraction of the species involved in nanoparticle formation to be estimated [511]:

“If the mole fraction of benzene is $\sim 10^{-3}$, those of pyrene and coronene would be roughly 10^{-5} and 10^{-7} , respectively, which are of the same orders of magnitude as the number densities of soot nuclei (10^{11} – 10^{13} cm^{-3})”

Therefore, either PCAH the size of pyrene to coronene are involved in soot formation or larger aromatic species of a similar concentration.

3.2 Aromers

There has been growing evidence for a larger class of PAH, so-called aromers (=aromatic oligomers), from 300–1000 Da [207, 208, 243]. Detection of large aromatic species has been historically challenging [111]. Gas chromatography can detect species up to 8 aromatic rings with liquid chromatography extending this up to 11 rings [28, 206]. The first technique to detect large PAH was positive ion mass spectrometry, allowing species >500 Da to be found in 1965 [45]. However, early laser desorption ionisation mass spectrometry (LDI-MS) in the 1990s was unable to detect these larger aromatics [118]. A breakthrough in LDI came when the laser wavelength was tuned to provide the correct resonance for ionisation of larger PAH species with >11 rings [11, 189, 243] (a more complete explanation of the effect is described in Desgroux et al. [111]). Homann *et al.* demonstrated in low pressure benzene/oxygen rich premixed flames that the concentration of aromatics does not decrease monotonically, as mentioned in the previous section, but increased from 300 Da to 620 Da [208, 243]. Many recent results from LDI and secondary ion-mass spectrometry have reproduced these results [112, 134, 221], while recent advances in mass analysers resolution have shown clear evidence for the presence of large pericondensed aromatics in diffusion [224] and premixed flames [428, 547] with minimal amounts of oxygen present (see Figure 11).

Other evidence for species significantly larger than pyrene came from electron microscopy and spectroscopy. Fringe analysis of high resolution transmission electron micrographs indicate larger species than pyrene are present in early soot [12, 497, 499, 540]. In a recent study comparison with simulated HRTEM images indicated that species closer to circumpyrene in size are present in early soot nanoparticles [3, 49]. Optical spectroscopy also revealed evidence of larger species. Raman spectroscopy suggested aromatic species are approximately 1 nm in size [88]. Optical band gap measurements have been historically employed to suggest the size of the aromatic species [48, 95]. Recent studies show stronger sensitivities to ring topologies [4], functional groups [71], radical character and curvature [341]. On top of this the size of the nanoparticle changes the band gap due to quantum confinement effect [5, 300]. Wang *et al.* demonstrated this size dependence by measuring the optical gap and ionisation energy for nanoparticles >4 nm [108, 300]. This followed quantum confinement, which was shown to be due to stacked aromatic species [5, 70, 507] (see Figure 7). This provided the first possible resolution of a significant question surrounding whether an indirect or direct optical band gap is found in early carbonaceous nanoparticles with the authors concluding that [300] (brackets and italicised text added by the authors of this review):

“For the CNPs (*carbon nanoparticles*) studied here, however, we find the k exponent is decidedly equal to 2 (*behaves like a material with an indirect*

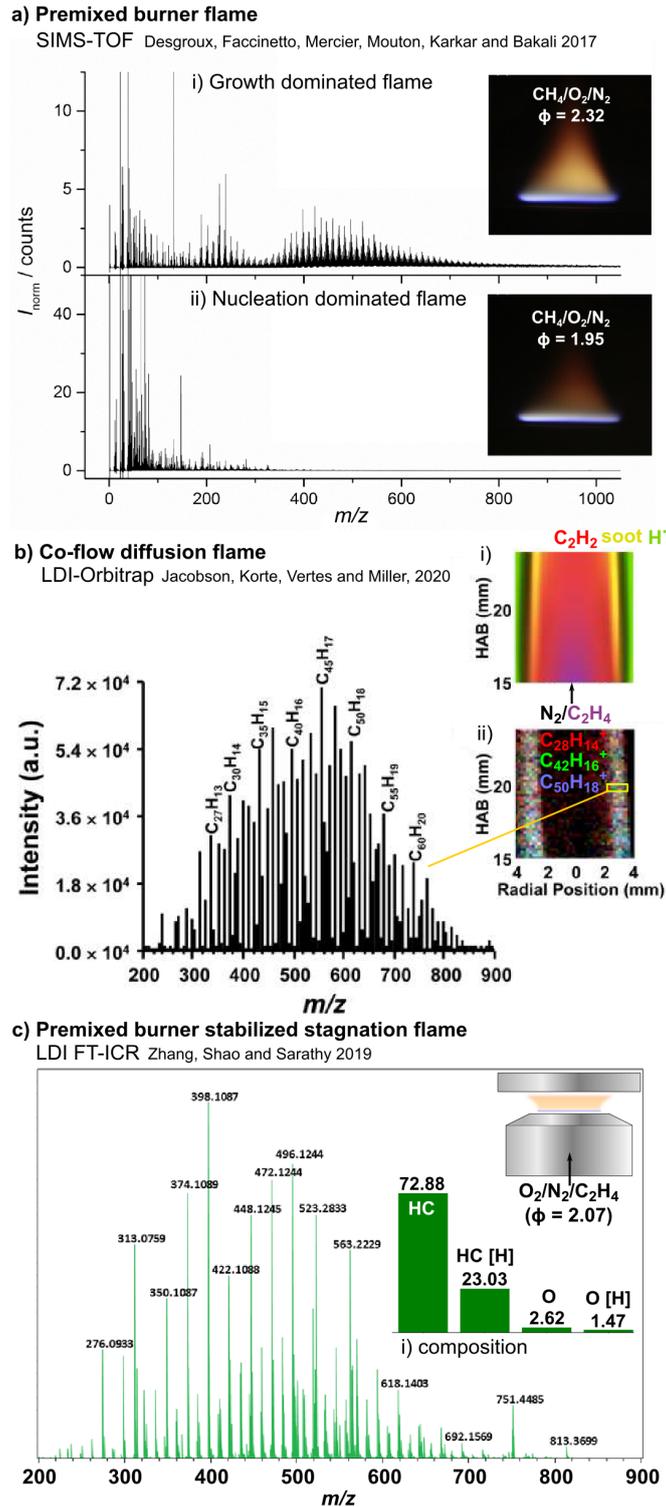


Figure 11: Mass spectrometry results for aromers from Desgroux et al. [112], Jacobson et al. [224], Zhang et al. [547].

band gap) even though the transition is expected to be excitonic ($k = 1/2$). ... Clearly, the band gap exhibits the expected quantum confinement effect.”

This size dependency clearly makes the optical band gap less useful for determining the size of aromatic domains.

Further evidence for aromers comes from recent direct imaging of aromatic soot precursors using non-contact or high resolution atomic force microscopy (nc/HR-AFM) from a nearly sooting premixed ethylene flame [88, 444] (see Figure 1). Figure 12 shows the H/C ratio for a collection of these directly imaged molecules with species significantly larger than pyrene seen (up to 650 Da). Additionally, many of these molecules were found to contain a higher concentration of hydrogen than that of maximally pericondensed species (the most condensed a set of hexagonal rings can be in an aromatic), due to methyl groups and the hydrogenation of the edges. This technique was limited to flat aromatics sampled from nearly sooting flames and could not adequately image the 3D aromatic molecules produced in a sooting flame. However, recent advances in HR-AFM have been developed that could allow 3D aromatics to be imaged in the future [327].

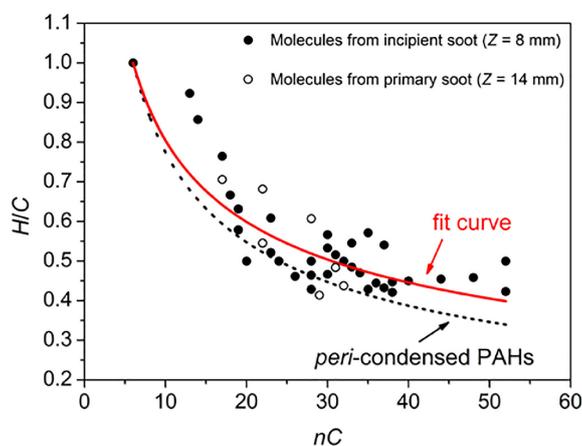


Figure 12: Stoichiometry of aromatics in nearly sooting flames imaged using HR-AFM [88].

Homann interpreted these larger PAH as containing curved PAH (cPAH) [208]. The evidence for this curvature came from these larger PAH readily forming negative ions. Curved aromatics, as with fullerenes, are known to have a high electron affinity and to easily form negative ions [110]. The type of curvature to which he was referring is due to the complete enclosure of a pentagonal ring within the aromatic network that causes the aromatic molecule to be bent out of plane and curved like a bowl. More direct evidence for curved PAH came from the extraction of corannulene **1a** and completely closed cages of carbon – C_{60} fullerenes – from flames and soot [164, 283] (see Figure 13).

The location of these larger PAH in the flame before the formation of fullerenes, as well as their loss of hydrogen, suggested they were fullerene precursors [16]. Recently, hydrogenated fullerenes have been extracted and crystallised from low pressure flames showing closure can occur before complete loss of hydrogen [484]. However, in most atmospheric flames the conditions for fullerene formation are unfavourable. They are therefore in a low concentration [197] and are unable to contribute to a soot formation mechanism. It appears that curved PAH help to create early soot nanoparticles instead of forming fullerenes. HRTEM has recently demonstrated tortuous fringes suggesting significant curvature [323, 510]. This imaging showed that the earliest soot particles (sampled

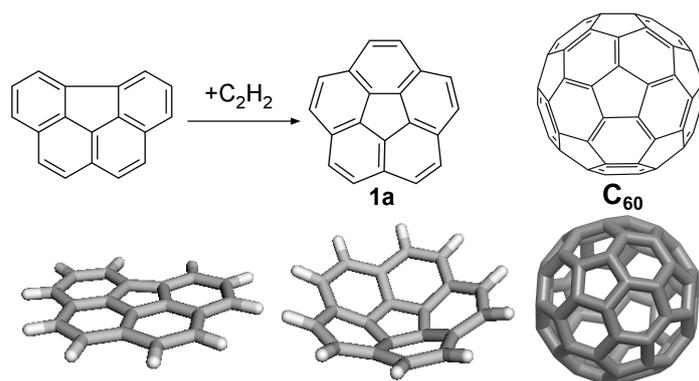


Figure 13: Kekulé and 3D molecular structure of corannulene **1a** and buckminsterfullerene **C₆₀**.

from a coflow diffusion flame), in particular, are significantly curved [323] (see Figure 1 HRTEM). The addition of cyclopentadiene [433] and oxygen [216] has also been shown to increase tortuosity of the nanostructure.

It is interesting to consider from where this curvature originates. Figure 14 shows the various mechanisms that have been proposed experimentally or computationally explored for curvature integration due to pentagonal ring embedding. These can be broadly separated into the corannulene pathway and the planar or flat PAH (fPAH) pathways. The corannulene pathway was suggested by Pope and Howard [405]. It involves small PAH and goes through the intermediate corannulene, which is the most well-known curved aromatic. Starting from benzene, a series of HACA reactions generate a variety of fPAH, as well as precursors for the cPAH. Recently, evidence has been found for a HACA pathway starting from cyclopentadiene either with acetylene [234] or methyl addition [531] that generates a variety of fPAH, some with an odd number of π -electrons giving resonantly stabilised π -radicals.

The first pentagon integrating reaction is shown in Figure 14i) where an aryl crosslink reaction between benzene and naphthalene is followed by cyclodehydrogenation to form fluoranthene. Aryl crosslinks twist the aromatic species relative to one another so that there is an angle between the two aromatic planes, due to the steric hindrance of the hydrogens neighbouring the crosslink. The π -bonding is optimal when the two aromatic planes are colinear and therefore at flame temperatures these species rapidly transform into planar structures in a process of cyclodehydrogenation or ring condensation [183]. This reaction is well-known experimentally [388] and is used in many modern mechanisms of soot PAH chemistry [496]. Pope and Howard suggested a mechanism where fluoranthene can also be generated from a thermal edge reconstruction or rearrangement with an edge pentagon becoming embedded and surrounded by three hexagonal rings [405, 445] (Figure 14ii)). HACA growth then can generate the next intermediate, benzo[ghi]fluoranthene, with a partially embedded pentagon enclosed by four hexagonal rings. This intermediate has also been suggested to arise from oxidation of a zig-zag edge [446, 460] or cyclodehydrogenation of the bay edge site of benzo[c]phenanthrene [501] (Figure 14iii) and iv)). Figure 14v) shows the final enclosure of the pentagonal ring through HACA growth onto benzo[ghi]fluoranthene, also referred to as a bay capping reaction. This forms corannu-

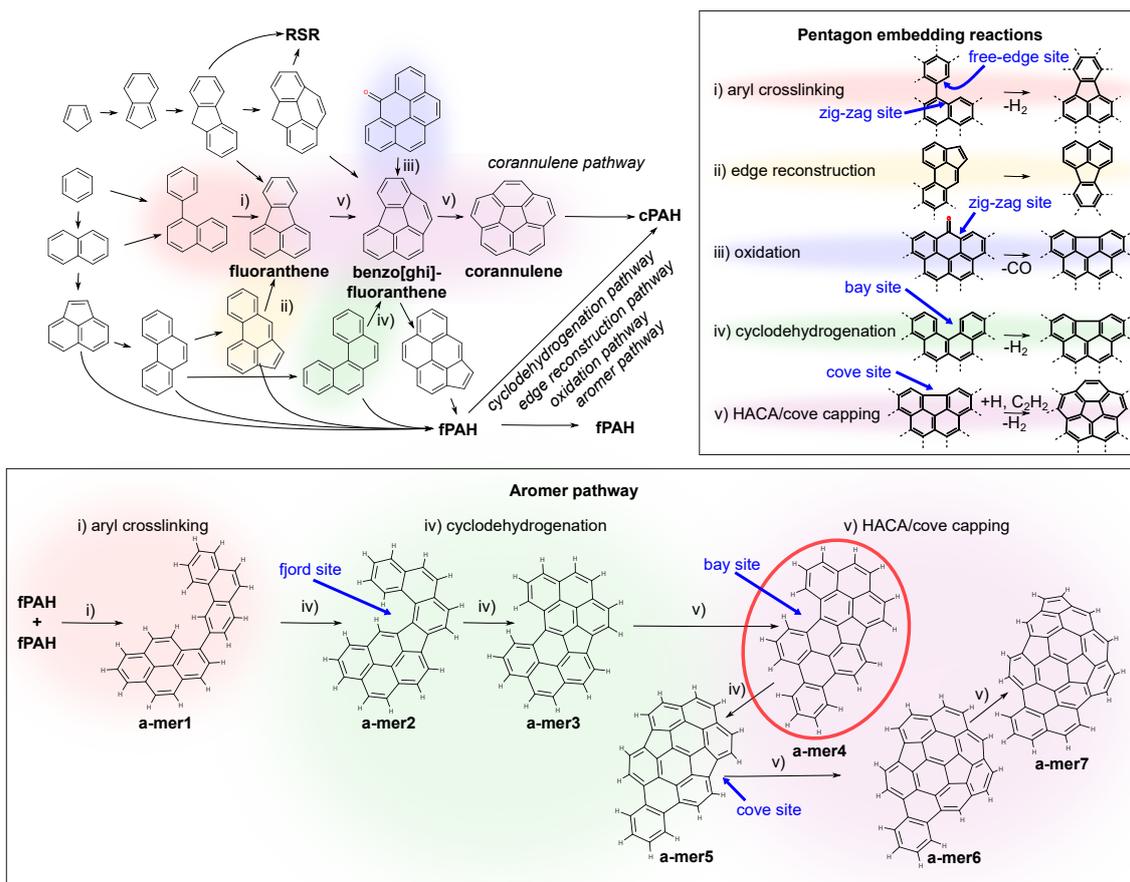


Figure 14: Curvature integration mechanisms. Insets show the pentagon embedding reactions (top right) and an aromer pathway (bottom). The structure circled in red is based on the structure imaged in HR-AFM [88]. Site types are shown with blue arrows to aid the discussion.

lene, the most well-known curved aromatic with five hexagonal rings enclosing a pentagonal ring [151]. Before this bay capping reaction the aromatic is flat, but afterwards the aromatic is bent into a bowl shape due to the considerable strain created by the enclosed pentagon [324]. This step is critical as the benzo[ghi]fluoranthene is still able to thermally rearrange into a flat aromatic with an edge-based pentagonal ring. However, once the pentagon has become embedded through a HACA reaction the mechanisms for pentagon migration are unlikely to occur. This migration involves C_2 rotations (Stone-Thrower-Wales transformations) with significant energetic barriers that kinetically “lock” the less stable pentagonal ring within the hexagonal network, which has been demonstrated experimentally from flash pyrolysis studies [445]. Lafleur et al. [283], however, found corannulene to be in low concentrations in benzene flames [(mass corannulene)/(mass pyrene) from 0.008 to 0.0063]. This pathway therefore appears to not be a primary formation mechanism of cPAH. Given that corannulene is the smallest cPAH known to date [324] this suggests species <300 Da contain rim-based pentagonal rings and partially embedded pentagons present in flat aromatics.

The other curvature integration pathways mirror the reactions seen in the corannulene

pathway yet become more likely as the aromatic grows in size. Cyclodehydrogenation of a bay site followed by HACA growth has been studied using kinetic Monte Carlo simulations of growing aromatics and has been found to enclose pentagonal rings [505, 526, 539]. However, these reactions are slow as they require a particular bay site, which is not readily generated for PAH ~ 500 Da in size [152, 292]. This pathway is therefore unlikely to provide the curvatures required to explain the significant curvature integration in flame or fullerene formation [151]. An oxidation pathway is also more likely for larger aromatics [446, 460]. Experimentally it has been found that partially premixed diffusion (Bunsen-type) flames have structures with increasing curvature as a function of oxygen concentration [216] and another recent study using *in situ* HRTEM imaging showed curling of graphene flakes into curved fragments at the surface of a soot particle during oxidation [486]. It is unclear how oxidation contributes to overall curvature integration, however, the low amount of oxygen found in early soot particles [86] and the prevalence of these curved species in diffusion flames [323], with much lower oxygen concentrations, indicates it is also not a primary curvature integration mechanism. Recent Kinetic Monte Carlo simulations of PAH growth from HACA do not support the significant curvature integration observed [152, 292].

Thermal rearrangements have also been found to provide partially embedded pentagonal rings that with further HACA growth produce cPAH. These can be classified into pericondensation and edge rearrangements. Pericondensation involves the rearrangements of orthocondensed (otherwise known as catacondensed) PAH into pericondensed structures with the loss of hydrogen. This has been extensively explored as a synthesis route for buckybowls and graphene. Edges of aromatics are highly mobile above 1300 K and rapidly rearrange into partially and fully embedded pentagonal rings [445]. Some example schemes from buckybowl synthesis are shown in Figure 15.

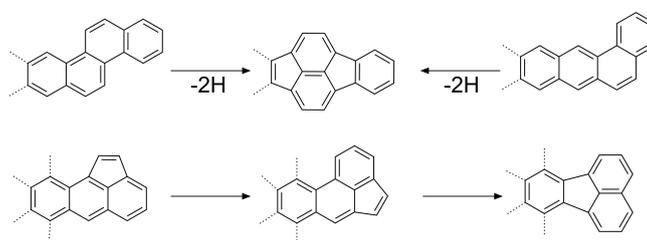


Figure 15: Thermal rearrangements that embed pentagonal rings [445].

Another recent experimental work on the transformation of ethylene into graphene on an Rh(111) surface using scanning tunnelling microscopy found some interesting thermal transformation of PAH [508]. Long acenes were formed at 470 K, however, heating to 670 K led to the breakup of these long acenes and the formation of pericondensed species, which then grow and fuse into polycrystalline graphene. While in this study the surface likely catalysed the rapid rearrangement reaction, flash pyrolysis experiments demonstrate that past 1300 K aromatics also rapidly rearrange into pericondensed species in the gas phase [445]. However, edge rearrangement competes with the embedding of pentagonal rings by allowing the migration of the ring to an edge (as it does not involve hydrogen loss and is therefore highly reversible). This inhibits the formation of long acenes and was the initial reason curvature integration was not explored in the combustion community for a

long time – the edge rearrangements were thought to provide more thermodynamically stable planar PAH [151].

Homann suggested the aromer pathway, which is a combination of the aryl crosslinking, cyclodehydrogenation and HACA/bay capping reactions, which can be seen in the inset of Figure 14. The experimental evidence for the aryl crosslinking of two fPAH arises from the presence of a separate distribution of larger PAH as mentioned, suggesting a separate mechanism from HACA [243]. Recent tandem mass spectrometry has also been used with collision-induced dissociation to show the fragmentation of this mode at 500 Da [2]. The possible radical sites for aryl crosslinking are shown in Figure 16, which we will consider further in Section 5.

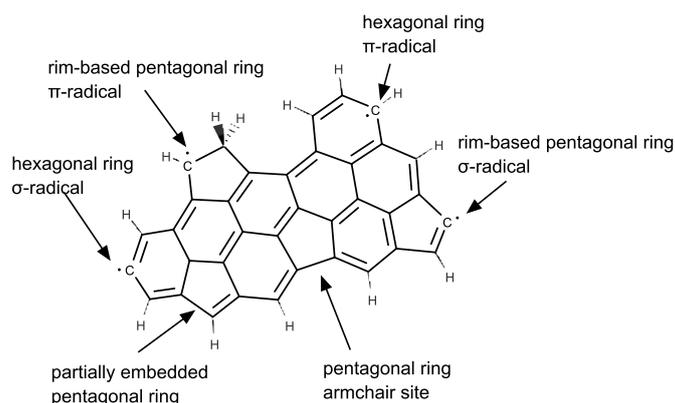


Figure 16: Reactive edges of soot precursors.

Howard considered σ -radicals produced from hydrogen abstraction from the edges of hexagonal and pentagonal rings and computed that molecules ~ 600 Da in size would contain 1–6 of these radical sites each [213]. σ -radicals are considered to be the most reactive radicals in the flame, reacting readily with acetylene in the HACA mechanism [149]. Homann mentioned the odd number of carbon atoms and suggested a non-bonding π -radical that is delocalised [243] and has also been imaged in HR-AFM [443]. These resonantly stabilised π -radicals are important in benzene formation, as mentioned – being less reactive than σ -radicals, they have longer lifetimes in the flame [187]. Frenklach also suggested a partially saturated rim-based pentagonal ring that forms a π -radical, showing it impacts surface rearrangements and growth processes, but did not explore the reactivity with other aromatic species [148, 526].

Subsequent cyclisation of these aryl crosslinked species has been experimentally found to favour the partial embedding of a pentagonal ring as opposed to a hexagonal ring [375, 435] (*e.g.* the free edge found to preferentially react with the zig-zag edge in pyrene pyrolysis, forming a pentagonal ring). Evidence for the crosslinking and partial embedding of pentagonal rings has also been found in HR-AFM with species found containing two aromatic segments with predominantly hexagonal rings linked via pentagonal rings [88]. These species are then highly orthocondensed and will thermally rearrange and cyclodehydrogenate to further embed the pentagonal rings, with HACA growth also contributing to pentagon enclosure. **a-mer4** from Figure 14 is highlighted as this aromatic network was experimentally observed in HR-AFM experiments [88] (see Figure 1 IS4). This species

can rapidly cyclodehydrogenate or have HACA growth to form the curved species. Evidence for this suggestion comes from the slightly higher concentration of hydrogen rich species in the 300 to 700 Da range and the fact that dehydrogenation rapidly gives way to species in the region with H/C ratios suggesting pericondensed structures [16]. More recently principal component analysis of SIMS-TOF MS of soot from flames provides strong evidence that the aromers arise from the crosslink of small aromatics with a subsequent dehydrogenation of 4–8 hydrogens [135].

Aryl crosslinks and further thermal rearrangements are known to integrate curvature and close cage structures completely [420]. However, it appears that multiple crosslinks are required for the integration of sufficient curvature to allow for complete formation into fullerenes. This is not possible in most atmospheric sooting flames but is possible in some low pressure flames [208, 505]. It is interesting to note that Homann originally suggested that this process was enhanced by the physical interactions holding PAH dimers together while the edge zipped up [25, 208]. This was based on an early model of fullerene formation called the zipper mechanism [222]. The summarised synthesis work on buckybowls highlights that no such physical interactions are required and that crosslinks, cyclodehydrogenation and thermal rearrangements are sufficient to integrate curvature.

3.3 Clustering (reactive) PAH

Reactive PAH were reported in one of the first mass spectrometry studies of aromatic species in flames in 1967 [207]. Of course, the naming “reactive PAH” contains the connotation of a chemical reaction occurring, which is yet to be shown, therefore we refer to these species as clustering PAH through either physical or chemical routes. It was only during the 2000s that mass spectrometric instruments were able to observe the molecule to particle transition, using soft laser desorption ionisation techniques with reflectron time of flight mass analysers that could extend the range to millions of mass/charge (m/z) units [180]. With these instruments Grotheer and colleagues were able to show clustering of aromatics [190]. Figure 17 shows this series of peaks with a periodicity of $\Delta = 500$ Da. This has since been reproduced in an atmospheric ethylene premixed flame by Carbone *et al.* revealing clustering only for the positive ions with $\Delta = 450$ Da and not for the negative ions [65] (see Figure 48). We will return to this work at the end of the review.

From these mass spectrometric studies the collision efficiency to allow such aromatic species to form was computed [410]. This comes from a simple second order kinetic model that has been found to accurately describe the rate of soot formation,

$$R_{C_{a,b}} = C_E \times \beta_{a,b} \times C_a \times C_b, \quad (1)$$

where the reaction rate, $R_{C_{a,b}}$, of molecules a and b is the product of the collision efficiency, C_E (other authors use α [511], β [127] or γ [250]); the free molecular collision coagulation kernel, $\beta_{a,b}$; the concentration of molecules a , C_a ; and b , C_b (in Kraft notation [410]) (the collision efficiency is often further split to separately consider the van der Waals enhancement, E_F , which we will not do in this work). It was found that aromatic species would need to cluster with a collision efficiency $C_E > 0.01$ (see Figure 31). In other studies collision efficiencies ranging from $C_E = 0.01 - 1.0$ have been used to produce the

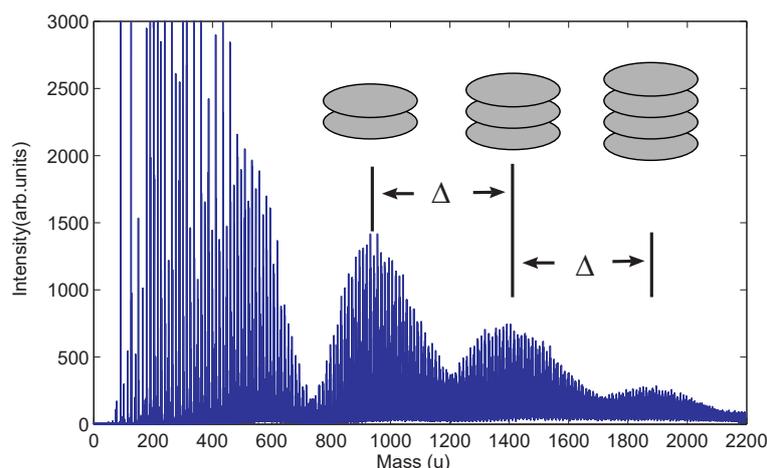


Figure 17: Mass spectrum of high-molecular weight species extracted from a 13 kPa acetylene–oxygen flame ($\phi = 3.25$) by molecular beam mass spectrometry with 193 nm laser ionisation [190].

flux of nanoparticles found during soot formation [420]. Therefore the goal of the rest of the review is to explore what is allowing PAH to stably cluster at these high collision efficiencies.

4 Nanoparticle formation

Before exploring soot nanoparticle formation some nomenclature must be discussed. There is much controversy around the language used to describe soot nanoparticles [351]. This confusion is unsurprising, given that there is still significant uncertainty surrounding how soot forms. Without understanding the possible mechanisms for soot formation which are operating under different conditions, naming conventions will remain undecided. For the sake of clarity we will make a distinction between chemical and physical soot nanoparticle formation preferring the term *soot inception* unless specifically discussing a physical nucleation mechanism. Mechanisms involving both chemical and physical interactions will be referred to as *physically stabilised soot inception*.

While the transition from molecule to nanoparticle is somewhat arbitrary we will consider any species above 1000 Da to be a nanoparticle. The growth of curved or planar pericondensed PAH is generally not found to extend past 1000 Da. This cutoff is consistent with how the term nanoparticle is used in the combustion literature [98, 351, 511]. There are some exceptions to this definition that are worth mentioning. PAH growth has been seen to extend slightly further than 1000 Da, in low-pressure premixed acetylene flames [208, 243, 521] and inverse diffusion flames [425]. Another exception is the formation of giant fullerenes that can extend to 6000 Da within low-pressure flames [25]. As our focus is on the nanoparticles that lead to primary and aggregate carbonaceous particles these exceptions are not an issue.

Table 1 lists the many mechanisms that have been proposed for the formation of carbonaceous nanoparticles in hydrocarbon flames. The main strengths and weaknesses that have been discussed in the literature are consolidated. We have provided a schematic of the most relevant nanoparticle formation mechanisms in Figure 18.

Table 1: Formation mechanisms for soot nanoparticles

Mechanisms	Scheme	Strengths	Weaknesses	Possible
Disproportionation				
(a) diatomic carbon	$\text{fuel} \rightarrow \text{C}_2(\text{g}) + \text{H}_2 \rightarrow \text{C}(\text{s})$	Presence of C_2 [470]	Cyanogen (C_2H_2)-oxygen flame sootless [416]. Soot contains hydrogen [483]	N
(b) CO	$2\text{CO} \rightarrow \text{C}(\text{s}) + \text{CO}_2$	Boudouard reaction well-known on surfaces low T [26]	Thermodynamics do not support this past 1000 K [203]	N
Acetylene inception				
(c) amorphous	$-\text{HC}_2\bullet + \text{C}_2\text{H}_2 \rightarrow -\text{C}_2\text{HC}\bullet$	Suggested from photolysis of acetylene [406]	Too slow does not explain aromatic sooting propensity [390]	N
(d) C_2 , acetylene	$\text{C}_2 + \text{C}_2\text{H}_2 \rightarrow 2\text{C}_2\text{H} + 2\text{C}_2\text{H}_2 \rightarrow 2\text{C}_4\text{H}_3 + \text{C}_2 \rightarrow 2\text{C}_4\text{H}_2 + \text{C}_2\text{H}$	Presence of C_2 [470], reactivity of C_2H_2 [161].	Insufficient C_2 at flame T [390]	N
(e) chemi-ion	$\text{C}_3\text{H}_3^+ + \text{C}_2\text{H}_2 \rightarrow \text{PAH}^+$	Ion-neutral reactions are fast. Ions and soot correlated [63]	Reactions are not much faster [513]. Neutral PAH grow at same rate [521].	N
(f) graphene	$\text{PAH}(\sigma\bullet) + \text{C}_2\text{H}_2 \rightarrow \text{PAH}$	Acetylene rapidly forms PAH [149, 155]	Too slow for nanoparticle formation [149]	N
(g) icospiral	$\text{PAH}(\sigma\bullet) + \text{C}_2\text{H}_2 \rightarrow \text{cPAH} \rightarrow \text{icospiral}$	PAH integrate curvature [179, 284], fullerenes present in flames [164], templated growth is fast [276], spirals and onions observed in HRTEM [218, 494]	Too slow [151] Closure into fullerenes is more likely [208]	N
Polyne inception				

Mechanisms	Scheme	Strengths	Weaknesses	Possible
(h) ring condensation	$C_2H_2 \rightarrow C_nH_2 \rightarrow PAH \rightarrow C(s)$	Many polyynes in the flame [207] thermodynamically stable at high T [273].	Rigid unlikely to cyclise [304], Radical-induced fragmentation limits growth [163]	N
(i) fullerene-like	$C_2H_2 \rightarrow C_nH_2 \rightarrow cage (+ PAH)$	Fullerenes present in flames [164], High pressure acetylene pyrolysis simulations [544]	Radical-induced fragmentation limits growth [163], fullerenes are formed from aromatic species in flames [208]	N
<i>Polyaromatic inception</i>				
(j) PAH, PAH	$PAH + PAH \rightarrow PAH-PAH$	PAH most stable, resistant to radical-induced fragmentation, so high conc. [149, 475], curved PAH were also suggested [7]	Edges are unreactive in peri-condensed PAH [442]	N
(k) aryl, PAH(6)	$PAH(\sigma\bullet) + PAH(6) \rightarrow PAH-PAH$	Hydrogen abstraction generates many σ radicals [213]	Requires large number of radicals for creating σ -radicals [511], prone to radical-induced fragmentation [149]. Low collision efficiency [316]	Y
(l) aryl, aryl	$PAH(\sigma\bullet) + PAH(\sigma\bullet) \rightarrow PAH-PAH$	Hydrogen abstraction generates many σ radicals [213], strong bonds formed [316]	Requires large number of radicals for creating σ -radicals [511]. Low conc. and collision efficiency [316].	Y

Mechanisms	Scheme	Strengths	Weaknesses	Possible
(m) cyclodehydrogenation	PAH-PAH → PAH	Ring condensation rapid at flame temperature [435] reduces impact of radical-induced fragmentation	Slow as relies on the initial crosslinking of aryl radicals (see above)	Y
(n) pentaring, pentaring	PAH(5) + PAH(5) → PAH(5)=(5)PAH	Pentaring more reactive than 6-mem ring [434]	Symmetry forbidden [2+2] pericyclic reaction unstable [434]	N
(o) aryl, pentaring (AALH)	PAH($\sigma\bullet$) + PAH(5) → PAH-(5)PAH	Pentaring more reactive than 6-mem ring [100]	Requires large number of radicals for creating σ -radicals [511] Prone to radical-induced fragmentation	Y
(p) aryl, RSR (CHRCR)	PAH($\pi\bullet$) + PAH($\sigma\bullet$) → PAH-PAH($\pi\bullet$)	π and σ -radicals are present in flames [213, 243]. Reaction easily lose H to regenerate π -radical [234].	Conc. of odd number PAH (likely to be π -radicals) not reduced [243]. Radical-induced fragmentation likely to compete	Y
(q) aryne	PAH($\sigma\bullet$) → PAH(2 $\sigma\bullet$) + PAH → PAH-PAH	Strong binding energy to PAH [82, 201]	Requires two H-abstraction the second having a significant barrier [211], unlikely due to concentrations of H and PAH($\sigma\bullet$) [213].	Y

Mechanisms	Scheme	Strengths	Weaknesses	Possible
(r) furans	$\text{PAH}(\sigma\bullet) + \text{O}\bullet + \text{PAH} \rightarrow \text{Furan}$	Furan-like PAH found in some flames [232] Oxygen can enhance soot formation [345]	Large oxygen rich PAH not found in most flames [208, 546]. Insignificant oxygen content has been found in early soot particles [86]. Prone to thermal and radical-induced fragmentation [500].	Y
Physical nucleation				
(s) aliphatic polymer	$\text{Fuel} \rightarrow \text{polymer} \rightarrow [\text{polymer}]_n$	Some vapours are light emitting [147]. Condensable tar is seen in thermophoretic samples from diffusion flames [249, 415],	Aliphatics are found to increase later in the flame [58, 386] Prone to radical-induced fragmentation [414], condensable tar can be removed with fast sampling [51]	N
(t) fPAH	$\text{fPAH} \rightarrow [\text{fPAH}]_n$	Irreversible dimerisation describes soot particle number [512]. Internal rotors improve stability [442]	Dimerisation not possible <650 Da [427, 489, 511]	N
(u) aliphatic chains	$\text{PAH} + \text{aliphatic} \rightarrow \sim\text{PAH}\sim \rightarrow [\sim\text{PAH}\sim]_n$	Evidence from IR spectroscopy [339]. Seen in HR-AFM [444]. Improves clustering [130]	Enhancement is minor ≈ 2.5 kcal/mol [130]	N
(v) aromatic polymer	$\text{Fuel} \rightarrow \text{aromatics} \rightarrow \text{polymer} \rightarrow [\text{polymer}]_n$	Large polymers are able to condense [125, 285]. Large polymer can cluster more effectively [217] Extension of polyaromatic routes	Prone to radical-induced fragmentation, aromatically linked PAH have lower dimerisation propensity than fPAH [132, 217]	Y

Mechanisms	Scheme	Strengths	Weaknesses	Possible
(w) penta-linked (APLH)	$(5)\text{PAH}(\sigma\bullet) + (5)\text{PAH} \rightarrow \text{PAH}(5)=(5)\text{PAH}$	Imaged HR-AFM [444], provides planar species [396]	Unlikely for $(5)\text{PAH}(\sigma\bullet)$ to react with pentaring, prone to radical-induced fragmentation	Y
(x) cPAH	$\text{cPAH} \rightarrow [\text{cPAH}]_n$	van der Waals interactions [25]. Dipole-dipole interactions improve clustering [323, 324]	Dimerisation energy similar to fPAH <i>i.e.</i> too low [324].	N
(y) ion, fPAH	$\text{fPAH} + \text{C}_3\text{H}_3^+ \rightarrow [\text{PAH}]_n^+$	Long range interactions [266]	Low binding energies [69].	N
(z) ion, cPAH	$\text{fPAH} \rightarrow \text{cPAH} + \text{C}_3\text{H}_3^+ \rightarrow [\text{cPAH}]_n^+$	Long range strong interactions [323, 324]	Limited to small clusters [323]	Y
Physically stabilised soot inception				
(aa) zipper mechanism	$\text{fPAH-fPAH} \rightarrow \text{cPAH}$	Suggested for fullerene formation [7, 25, 208]	aryl-linked aromatics cannot stack	N
(bb) internal rotors	$[\text{PAH}(\sigma\bullet), \text{PAH}(5)]^* \rightarrow \text{PAH-PAH}$	Increase interaction time for polyaromatic reactions [73, 152], bound internal rotors for large PAH [489]	aryl-radical collision did not reveal effect for small PAH [316]	Y
(cc) aliphatic, bridge-linked (CH ₂ -ABLH)	$\text{PAH}(\pi\bullet) + \text{PAH}(\pi\bullet) \rightarrow \text{PAH}-(\text{CH}_2)_m\text{-PAH}$	Allows stacking and bonding [125, 130]. Mass spectrometric evidence in some flames [2]	Prone to radical-induced fragmentation [414] high H/C ratio	Y
(dd) acetylene bridge-linked (C ₂ H ₂ -ABLH)	$\text{PAH}(\pi\bullet) + \text{PAH}(\sigma\bullet) + \text{C}_2\text{H}_2 \rightarrow \text{PAH-C}_2\text{H}_2\text{-PAH}$	Acetylene is abundant and π -radicals have also been detected [444], stable complex [166]	Prone to radical-induced fragmentation [414], polymerisation mechanism unclear	Y

Mechanisms	Scheme	Strengths	Weaknesses	Possible
(ee) O ₂ , bridge-linked (O ₂ -ABLH)	PAH($\pi\bullet$) + O ₂ + PAH → PAH-O ₂ -PAH	Oxygen is found to enhance soot formation in some flames [131], binding energies are strong [318]	Insignificant oxygen content has been found in early soot nanoparticles [86]. Prone to radical-induced fragmentation [414], polymerisation mechanism unclear	N
(ff) excimer	PAH* + PAH → (PAH,PAH)*	Presence of fluorescence in soot forming region [358], excimers formed with stacked PAH [357]. LIF gives long duration fluorescence supporting excimers [346, 464]	Weak interactions over nanoseconds [346], can only stabilise a dimer, trimers weakly bound [102]	N
(gg) multicentre-linked (pancake) (AMLH)	PAH(deloc. $\pi\bullet$) + PAH(deloc. $\pi\bullet$) → PAH≡PAH	Many π -radicals present [444, 506], multicentre bonds allowing stacking [246, 469]	Low interaction energy [93, 246, 324], polymerisation mechanism unclear	Y
(hh) zig-zag-linked (AZLH)	2diradicaloid → diradicaloid=diradicaloid	Long acenes have large dimerisation energies [269, 511], large PAH with zig-zag edges can be open-shell singlet multiradicals [401, 545]	Acenes fragment or rearrange into fPAH [508, 511]	Y
(ii) rim-linked (ARLH)	PAH(loc. $\pi\bullet$) + PAH($\pi\bullet$)/(5)PAH → PAH-PAH	Many π -radicals present [444, 506]. Strong bonding and less prone to radical-induced fragmentation [324]	Unknown concentrations of PAH(loc. $\pi\bullet$) and collision efficiencies.	Y

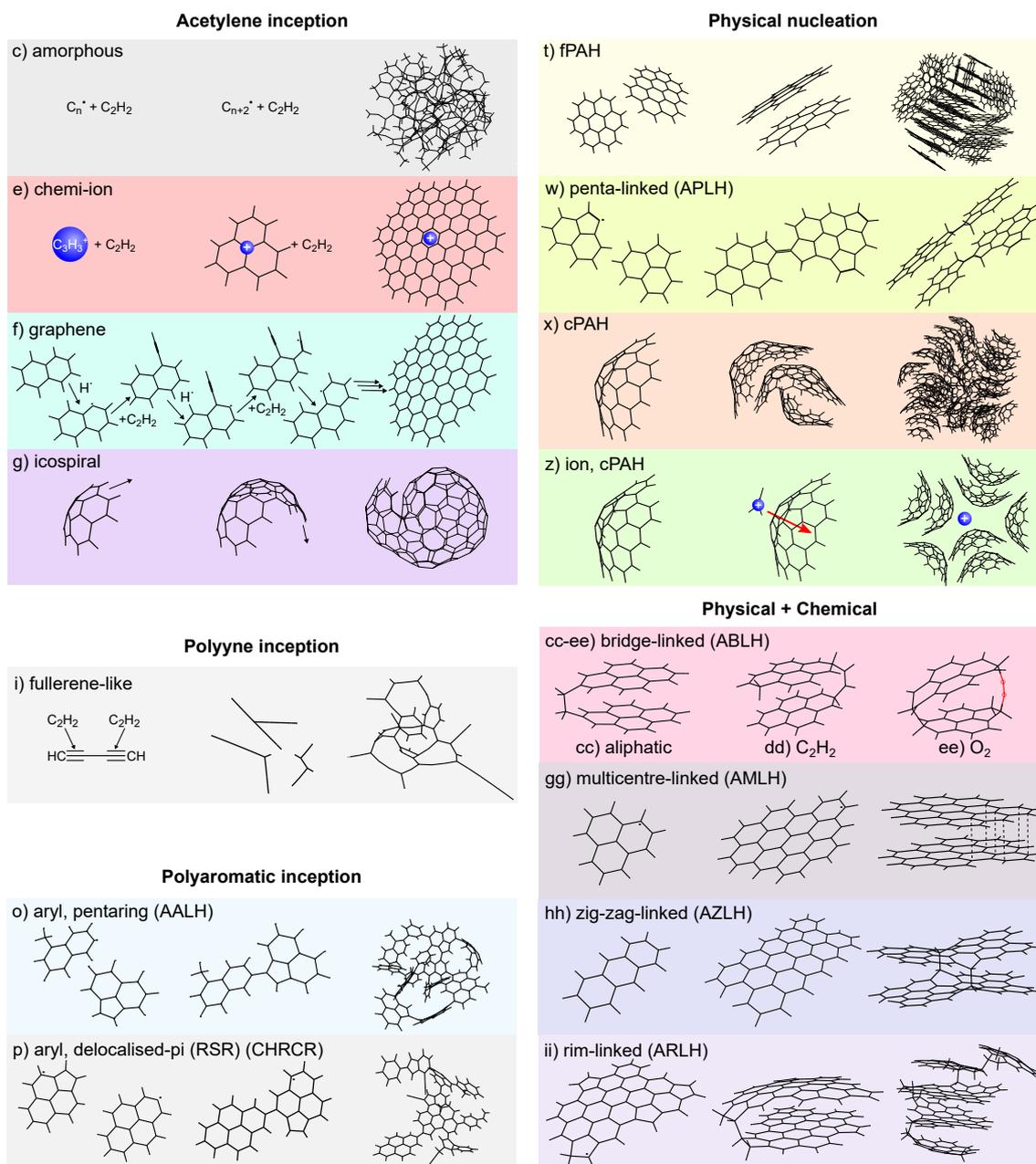


Figure 18: Schematics for a collection of mechanisms from Table 1.

4.1 Disproportionation

4.1.1 Diatomic carbon

The earliest view of soot formation was the direct dehydrogenation of hydrocarbon fuel into solid carbon particulates [390]. Flame spectroscopy revealed how the ethylene optical emissions gave way to the C_2 Swan bands that cease upon soot formation with increasing fuel/air ratio [470]. This led Smith in 1940 to suggest disproportionation of the fuel

into C_2 and H_2 with the former reacting to form solid soot [see Table 1(a)]. However, the concentration of C_2 was found to be too low to support soot formation [162]. Additionally, flames in which C_2 was produced in high concentrations, such as cyanogen (C_2N_2) [416] and carbon suboxide (C_3O_2) [261] were not found to produce significant amounts of soot.

4.1.2 Carbon monoxide

Carbon monoxide is produced during fuel pyrolysis and is one of the main products of incomplete combustion [see Table 1 (b)]. The so-called Boudouard reaction was well known in gas works where carbon monoxide decomposes into solid carbon deposits and was also suggested to produce soot in flames [26] [see Table 1(b)] according to,



An equilibrium analysis revealed that >1000 K carbon formation is not possible from Eq. 2 and therefore carbon monoxide dominates at flame temperatures over disproportionation to solid carbon and CO_2 [203].

4.2 Acetylene inception

Acetylene was first isolated by Davy in 1836 and he immediately noted the significant luminosity and soot produced by this fuel [107]. It was then found by Berthelot [30] and others that acetylene was formed from the pyrolysis of hydrocarbons in arcs and tube furnaces (the partial combustion of hydrocarbons now being the dominant industrial synthesis route for acetylene). In the 1890s, Lewes then showed that this acetylene formation preceded soot formation in flames. This led him to posit that acetylene was the origin of luminosity and therefore soot in flames [294].

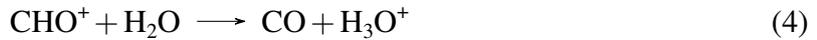
Acetylene was thought to directly decompose into carbon [see Table 1 (c)]. This was supported in the 20th century by Porter's flash pyrolysis experiments which showed acetylene decomposition to a carbonaceous material after photoexcitation with no extractable fractions [406]. Porter suggested a radical chain mechanism where acetylene added to the carbon material and hydrogen was evolved (leading to what we will call an amorphous inception mechanism). Others suggested acetylene reactions catalysed by C_2 [390] [see Table 1(d) and Figure 18]. The presence of significant hydrogen in early soot nanoparticles suggested more complex mechanisms were at play and other intermediates such as PAH were important.

4.2.1 Chemi-ions

Calcote provided one of the first detailed reviews of various pathways and kinetics involved in acetylene inception [62] [see Table 1(e) and Figure 18]. He showed that none of the chemical mechanisms suggested before the 1980s were rapid enough to explain

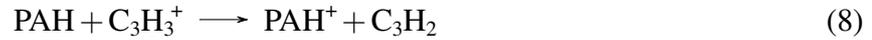
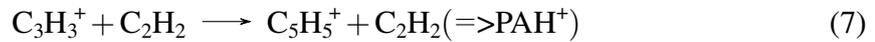
nanoparticle formation. Instead he proposed an ionic mechanism based on two observations: the correlation between soot and charged species in the flame and the more rapid reactions between neutral species and charged hydrocarbon ions.

The correlations between soot and charged species are well known and have been thoroughly reviewed by Hayhurst and Jones [192], Lawton and Weinberg [289] and more recently by Fialkov [143]. Briefly, significant concentrations of charged species are found in flames ($10^{15} - 10^{17}$ ions m^{-3}) [63]. This significant charge concentration was found to be due to chemi-ionisation reactions and not thermal ionisation [61]. Chemi-ionisation reactions rely on the ejection of an electron in a high energy reaction between an electronically excited molecule and a neutral species. The main reactions are [192],



where the electronically excited carbyne (CH^*) reacts with an oxygen radical (O^\bullet) to form the cation radical formyl (CHO^+) (Eq. 3). This is a short-lived radical that reacts rapidly with other species including water to form the hydronium ion (H_3O^+), which is the predominant ion in combustion exhaust (Eq. 4). Many other small positively charged hydrocarbons are produced through protonation with the formyl cation (Eq. 5).

Under rich flame conditions the primary ion-producing reactions become,



where excited carbyne reacts with acetylene (C_2H_2) to form propenyl cations (C_3H_3^+), which are longer lived as they can cyclise into cyclopropenyl (Eq. 6) [143]. PAH are known to become charged as they grow through reactions with chemi-ions (Eq. 8 and 9) allowing them to be detected in molecular beam mass spectrometry [208]. Soot can also be charged due to thermoionisation (Eq. 10), which is most effective for larger soot particles that are sufficiently carbonised to have a low ionisation potential [143].

Why are these positive species not neutralised by negative charges? The primary negative species are electrons, however, low concentrations of negatively charged species are able to be formed *i.e.* in equilibrium with the electrons.

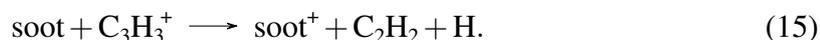


Formation of negative ions is through electron attachment. However, the electron affinity of most flame species is low, with most electron ion collisions leading to elastic scattering and the majority of negative charge being carried by the electrons [143, 192], explaining the lack of neutralisation. One exception is curved PAH that easily become negatively charged by electron attachment (Eq. 13) as shown by Homann [208]. Soot is also able to become negatively charged through electron attachment. Electron attachment (Eq. 14) and thermoionisation (Eq. 10) provide a charge equilibrium for primary and aggregate soot particles that is in thermal equilibrium and is described by the Saha equation [143]. This list of flame ion reactions is not comprehensive and more complete mechanisms exist for flame ion chemistry [9].

Returning to soot formation, Calcote also drew attention to the location of the ions directly preceding the formation of soot nanoparticles and to the similar soot and ionic concentrations ($10^{14} - 10^{16}$ ions m^{-3}), suggesting a causative link [63]. It is well known in atmospheric chemistry that reactions involving charged species and neutral molecules can be significantly faster than neutral-neutral reactions due to the ion-induced dipole forces. Calcote's reaction mechanism was then based on the chemical polymerisation of $C_3H_3^+$ with acetylene (Eq. 8) [see Figure 18(e)] [63]. Charged molecules were suggested to polymerise by acetylene addition at a rate sufficient to explain the rapid growth of soot nanoparticles. Preliminary studies supported such a mechanism with positive nanoparticles up to 8×10^3 Da being found using mass spectrometry in acetylene flames [25, 163] (see Figure 2). Experiments involving electric fields and easily ionised metals were used to further explore such a mechanism.

Electric fields have long been seen as evidence for an ionic mechanism. Brande in 1814 showed that a diffusion flame can be deflected towards a negative plate within an electric field, suggesting positive ion carriers [57]. The influence on soot inception is complicated by the production of an ionic wind. The accelerated chemi-ions in the flame entrain air in such a way that the flame is aerated, increasing oxidation and thereby reducing soot formation. Weinberg and Place were the first to realise that a counterflow diffusion flame would allow for the ionic wind to have no impact on the aeration of the flame [402]. Counterflow flames provide a flame front nearly perpendicular to the flow field. An electric field applied across the burner provides an ionic wind which merely shifts the stagnation surface. Soot's residence time in the flame was found to be reduced, as was the size of the primary particles. Figure 19 shows the significant impact of the electric field on the formation of soot, recently measured using laser induced incandescence (LII) and the aromatic species and the hydroxyl radical using laser induced fluorescence (LIF) [391].

The application of the electric field shifts the reaction zone, providing some quenching of the production of aromatics, however the impact on soot formation is more pronounced with a complete removal of soot. This effect is most pronounced when the electric field is established in such a way that shifts the chemi-ions formed in the chemiluminescence zone of the flame into the soot-forming region, increasing the charge present during soot formation [143]. Weinberg suggested that this reduces soot formation through the attachment of cations to soot particles;



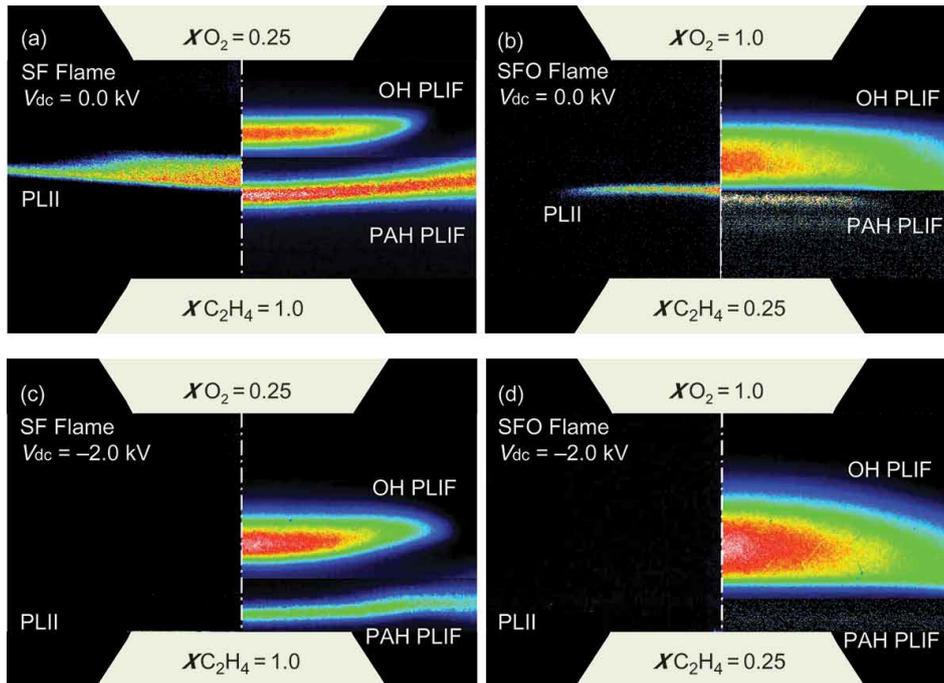
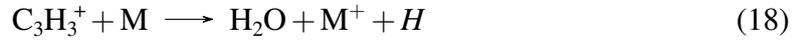


Figure 19: Counterflow $C_2H_4/O_2/N_2$ diffusion flame without (top) and with (bottom) an electric potential difference of 1 kV applied. Luminous carbon particulates measured with LII disappear from the flame upon application of the field (from Park et al. [391]; used with permission from Taylor & Francis ©).

This charge attachment reduces the coagulation efficiency of soot as an excess of positive charge increases the repulsion between soot primary particles. The reduction in size was then initially attributed to a reduction in the residence time of the charged soot in the flame. By tuning the direct current (DC) electric field strength, these positively charged soot particles were held in the soot forming region allowing them to grow to hundreds of nanometres in size. Weinberg suggested that only soot particles larger than 9 nm are able to become charged due to charge attachment as in Eq. 19 [289]. However, as has been mentioned, smaller charged soot particles were also able to be observed as the resolution of particle mass analysers improved [25]. Furthermore, the electric field uniformly reduces all soot primary particles' diameters, not only the charged soot, indicating that charged and neutral soot formation is linked [143]. Using DC electric fields to explore the impact of ionic soot mechanisms is challenging. The flow fields can be modified through ionic winds and chemi-ions can shift within the flame, which makes distinguishing the impact on soot nanoparticle formation and soot aggregation difficult to decouple. Alternating current electric fields have also shown an impact on soot nanoparticle formation, causing soot emissions to increase or decrease depending on the frequency and voltages used [271]. These results were interpreted as primarily impacting soot nanoparticle formation.

Addition of easily ionised metals to flames provides a further opportunity to explore ionic aspects of soot formation. They have long been studied as anti-smoke additives to diesel engines [311] and in polystyrene combustion have been shown to reduce soot emissions

by 50–90% [76]. These metals increase the ionic concentrations through a variety of processes and reactions:



Thermal ionisation (Eq. 16) is the first mechanism considered for alkali metals as they possess a low ionisation potential. Ashton and Hayhurst found the rate of thermoionisation in a hydrogen flame to be determined by the Saha equation to be $k = (9.9 \pm 2.7) \times 10^{-9} T^{1/2} \exp(-E_I/RT)$, where E_I is the ionisation energy [14], with the ionisation energy decreasing down the periodic table. Therefore, larger alkali metals are expected to be more completely ionised in flames. Experimentally, the ionisation effect can be less pronounced as seen in Figure 20 where ionic concentrations are measured in a premixed flame aspirated with water and alkali metal salts [173].

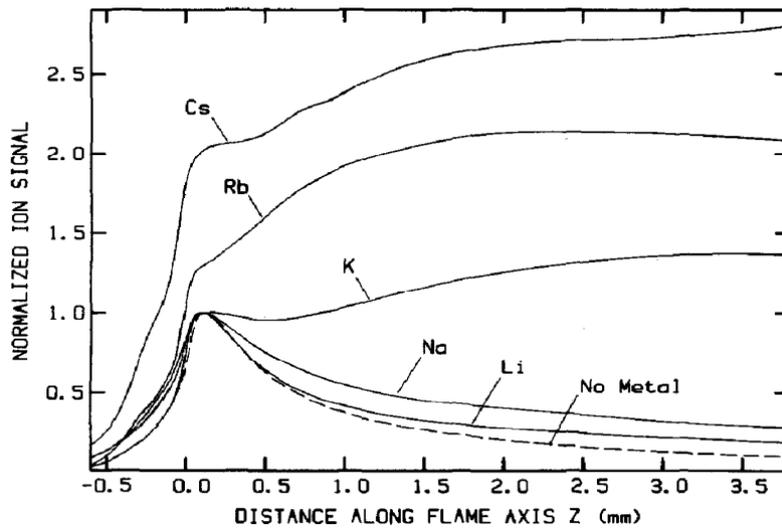


Figure 20: Ionisation signal with different metals addition to a flame [173]. Used with permission from Elsevier ©.

The delayed increase in the charge concentration for most alkali metals in this flame was explained as being due to the high ionisation potential of these species. The charging later in the flame when the temperature is lower was suggested to be due to charge transfer from hydronium ions (Eq. 17). This late charging is thought to primarily influence coagulation. In this case charge transfer to soot increases the fraction of positively charged soot primary particles (Eq. 19). This reduces the coagulation efficiency due to electrostatic repulsion, producing less aggregated primary particles that are more easily oxidised. A partially premixed coflow ethylene flame ($\phi = 2.27$) probed by small angle X-ray diffraction indicates that the size of primary particles does not change significantly for potassium addition [116]. However, in a different flame (premixed ethylene/air flame on a modified

PerkinElmer burner $\phi = 2.6$) potassium has been found to reduce the size of the primary particles [457]. Another complication in interpreting these results is the catalytic effects of alkali metals. Potassium has been found to reduce the mass of soot as demonstrated by experiments that added the potassium further downstream where coagulation has already occurred, finding a decrease in soot emissions from improved oxidation [421]. Recent x-ray absorption spectroscopy supports a “classic catalytic role of activating O_2 into reactive oxygen species, with the mobility of K_2CO_3 facilitating the transport of these species to immobilised soot particles” [106]. Similar challenges exist for interpreting the role of alkaline metals such as Ba, Ca, *etc.*, which are known to form cations with excited hydroxyl (Eq. 20) and catalytically produce the aggressive hydroxyl oxidant [143].

Cesium provided the most insight on the impact of ions on soot formation. It has a low ionisation potential and leads to a considerable increase in the ionic concentration in the soot-forming region of most flames [173], as seen in Figure 20. In the mentioned study, a decrease in the chemi-ion corresponding to $C_3H_3^+$ was found, indicating that the metal was able to be charged through charge transfer according to Eq. 18, and was suggested to support a chemical mechanism for soot formation (Eq. 7). The reduction in soot was then explained by Calcote as being due to the reduction in the number of nuclei chemically grown from $C_3H_3^+$ [63]. However, *in situ* small angle X-ray diffraction using synchrotron light sources has recently found that addition of cesium into an ethylene flame doubles the concentration of the smallest carbon nanoparticles [116], which suggests that cesium promotes soot nanoparticle formation. This would indicate a different mechanism for the soot reduction, one which is more in line with that suggested by Howard and Kausch [214] and Bonczyk [43]. In their proposed mechanisms, the ions play a stabilising role for nuclei, producing large numbers of smaller carbon particles with increased surface area allowing for their rapid oxidation and destruction and leading to less soot.

Other significant critiques arose for the chemical ionic mechanism. Firstly, there are a number of soot-producing systems that have insufficient ion concentration such as benzene flames, and shocktube and pyrolysis experiments [420]. Secondly, the molecular beam mass spectrometry of larger PAH found that the growth rates of charged and neutral aromatic molecules were similar [521]. While reaction rates can be enhanced in atmospheric chemistry for ions at room temperature, the high temperatures found in flames provide thermal energies that overwhelm any ion induced-dipole enhancement [513]. The HACA mechanism was able to explain the growth of pericondensed aromatic molecules under flame conditions [149]. We will return to ion-induced nucleation mechanisms in the context of physical nucleation later in this review.

4.2.2 Graphene

Graphene inception is the continuous growth of PAH into large graphene molecules that could be considered soot nanoparticles [see Table 1(f) and Figure 18] [143]. This is envisaged to occur through the HACA mechanism reported earlier. It is clear, however, that while this mechanism can explain the formation of small aromatics it cannot explain the rapid formation of soot nanoparticles [149]. There is an exception for low pressure acetylene oxygen flames in which the conditions can be tuned to produce large flat graphene structures [521]. This is of considerable interest for the gas phase synthesis of graphene

for material and electronic applications. Most of the studies have focused on plasma reactors using low sooting fuels, such as alcohols, to produce graphene in the gas phase at atmospheric pressure [104, 105, 380].

4.2.3 Icospiral

The discovery of fullerenes by Kroto, Curl and Smalley in 1985 [277] led to a number of new proposed mechanisms for soot formation [275]. The first was that buckminsterfullerene C_{60} could act as the nuclei for soot formation, an idea supported by their detection in many flames [164]. However, the concentration of C_{60} was found to be too low in atmospheric flames to be critical for soot formation [197, 208]. A second suggestion was that an aromatic species was formed that then curved onto itself like a nautilus shell [276] [see Table 1(g) and Figure 18]. This geometry (the icospiral) is achieved by two screw dislocations allowing for the fullerene layers to be wound together (see Figure 21). Evidence came from electron micrographs of soot and carbon black particles, where closed and spiral fringes indicated such an icospiral seed [218, 494]. These early electron micrographs were often formed by strong electron annealing that allowed for the fringes to be clearly imaged. Such annealing is known to convert many zero-dimensional carbon materials such as nanodiamond into fullerene-like carbon onions [495], suggesting these structures were formed during the electron irradiation.

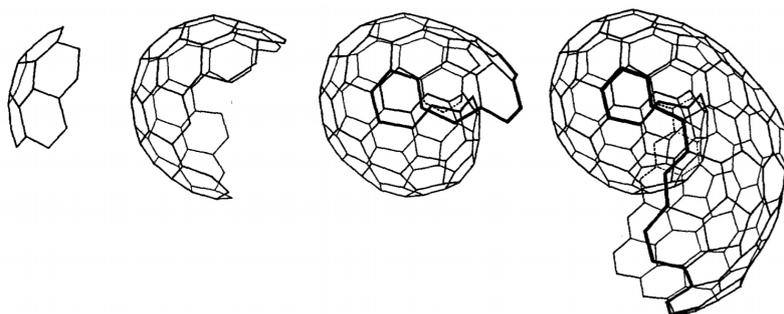


Figure 21: *Icospiral growth as envisaged by Kroto [274].*

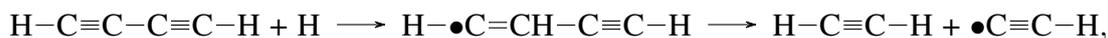
The icospiral geometry was suggested to allow for a templated growth process, which is known to be rapid and the predominant growth mechanism in crystals [241]. Templated HACA growth of a small aromatic on a larger aromatic structure has recently been studied computationally. Minimal, if any, impact at flame temperatures was found for templated HACA growth due to the weak dispersion forces involved between acetylene and graphene [219]. Some other recent work on curved aromatics has shown that HACA type growth can be enhanced due to curvature integration [409]. While this is of considerable interest, curvature has also been found to modify the rate of oxidation, in most cases increasing it [413, 460]. Therefore, more work is required to determine the impact that curvature has on PAH growth. Nevertheless, the fraction of hydrogen in early soot and the molecular beam mass spectrometry support the view that PAH growth does not extend past 1000 Da in most sooting flames, which would be required for an icospiral [151].

In summary, acetylene is critical for PAH formation and therefore indirectly contributes to soot nanoparticle formation. However, the HACA mechanism is too slow to explain

soot nanoparticle formation through chemi-ions, graphene or icospirals due to weak enhancements to PAH growth from ionic, curvature or templating effects.

4.3 Polyynes inception

The first molecular beam mass spectrometry from within flames revealed significant concentrations of polyynes, suggesting they could be potential precursors to soot nanoparticles [207]. The first kinetic mechanism developed focused on the stability of polyynes that are more thermodynamically stable than pericondensed aromatic hydrocarbons at high temperatures (> 2000 K) and suggested a ring condensation where polyynes react to form PAH species [273] [see Table 1(h)]. Recent molecular beam Raman analysis also confirms the significant concentration of polyynes present in soot forming flames [290]. However, mass spectrometry showed that the growth of these species was not found to extend past 150 Da [207, 208]. This is because they are prone to degrade in flame environments [152]. Hydrogen addition to growing polyynes leads to radical-induced fragmentation such as,



where the hydrogen addition leads to a radical that fragments through a β -scission, breaking up the chain [152]. Analysis of polyynes in partial equilibrium with hydrogen radicals and H_2 supported a limit to polyne growth of C_mH_2 , $m < 16$ [163, 348]. Long polyynes are unlikely to cyclise into PAH due to their high rigidity [304] and are more likely to degrade to acetylene and C4 species that cyclise into aromatics [187].

Recently a range of reactive molecular dynamics simulations have suggested a fullerene-like polyne mechanism [185, 302, 544] reminiscent of fullerene cage formation which was explored using similar methods [408] [see Table 1(i) and Figure 18]. In simulations involving highly concentrated mixtures of acetylene and other fuels (0.1 g/cm^3), and extreme temperatures (2000–3000 K), large fullerene-like structures were observed [185, 302, 544]. These extreme temperatures led to C–H bonds breaking and a large number of radicals. These radicals quickly react in these high density simulations forming long polyne chains that condense into cage structures. As mentioned, such growth of long polyynes is not observed in hydrocarbon flames. The H/C ratio of early soot particles of 0.3–0.5 is also too high compared with what would be expected from a fullerene-like polyne mechanism. Careful reactive molecular dynamics of benzene pyrolysis showed the initial formation of aromatic species [429, 430] and only after loss of all hydrogen atoms were fullerene-like cages able to form. This result matches what is observed in the negative mass spectrum during aromatic to fullerene transformations [16, 208, 484].

The discussion of polyynes leads us to recall the comment from Bansal and Donnet from 1993 [119],

“...the presence of a particular species is not sufficient proof that it is involved in soot formation. A species may be present because it is not reactive.”

It also reminds us that a soot mechanism must take into account not only the construction

towards soot nanoparticles (forward reactions) but also the destruction of the growing species (reverse reactions).

4.4 Polyaromatic inception

Some of the first to discuss a polyaromatic inception were perhaps Rummel and Veh [424] in 1941 when they suggested that moderately sized PAH molecules react to form soot. These species had by then been extracted from sooting flames. These suggestions were revived in the discussion of meteoric carbon [371] and nanoorganic carbon in flames in the 1990s [96].

We have already mentioned that as PAH grow in the harsh environment within flames they form and fragment producing many stabliomers (highly pericondensed aromatics) [475], which have low reactivity towards each other [see Table 1(j)]. Therefore, most polyaromatic inception mechanisms rely on a radical species recombining with other radicals or crosslinking with reactive PAH.

Experimental evidence for such a mechanism historically came from the significant increase in soot production following the addition of chlorine, which increased the aryl-radical [338] and aromer concentrations [208]. Since then crosslinked species and species strongly suggesting crosslinking have been directly imaged in HR-AFM (see Figure 1) [88]. Indirect evidence has also been provided from the mechanical hardness of primary soot particles measured with *in situ* nanoindentation HRTEM experiments [33]. These experiments combined with reactive molecular dynamics simulations suggested 2–3 crosslinks per aromatic molecule to provide the hardness values measured [395, 397].

4.4.1 Aryl-linked (AALH)

Palmer and Cullis suggested that the abstraction of an edge-based hydrogen from a PAH produces an aryl-type σ -radical able to react with highly pericondensed PAH containing hexagonal rings (PAH(6)) – called aryl, PAH(6) polyaromatic inception [see Table 1(k)]. This follows the well-known pyrolysis reactions of aromatics. Benzene pyrolysis, for example, will yield biphenyl with subsequent phenyl additions giving triphenylene, which involves cyclodehydrogenation [see Table 1(m)] [375]. Unless subsequent cyclodehydrogenation takes place the phenyl addition of an aromatic ring is prone to radical-induced fragmentation [136]; for example, bond energies of only -20 to -23 kcal/mol are found for the hydrogenated biphenyl/phenyl-benzene complex [392, 456]. Therefore, soot mechanisms involving the reaction between σ -radicals and highly aromatic PAH were not considered to be thermally stable in the flame under radical-induced fragmentation [149]. However, in pyrolysis systems operating at lower temperatures the aryl, PAH(6) inception appears to be critical for the formation of PAH and possibly carbonaceous nanoparticles [81, 455].

As the aromatic network increases in size, so does the concentration of σ -radicals. This in turn heightens the chance of the aryl, aryl polyaromatic inception mechanism occurring [see Table 1(l)]. Howard calculated that PAH \approx 600 Da in partial equilibrium with H^*/H_2 would each possess 1–6 σ -radicals [213]. However, a reactive molecular dynamics study

of colliding aryl, aryl PAH found collision efficiencies one to two orders of magnitude lower than those required for nanoparticle formation as discussed [316]. Some other reactive molecular dynamics studies have suggested rapid clustering of PAH radicals with close to unity C_E [244, 542]. However, the high densities used, 0.2 g/cm^3 , significantly enhanced the clustering, overshadowing the importance of fragmentation in flames where PAH densities are closer to 10^{-6} g/cm^3 [143]. Furthermore, high temperatures (2000–2500 K) have often been used to speed up these simulations, leading to direct hydrogen loss from PAH edges. This does not occur, at any significant rate, at flame temperatures without a radical abstraction, which means that the number of radicals in these simulations is much higher than in the flame itself [244, 542]. Mao *et al.* demonstrated the importance of temperature in reactive molecular dynamics [315]. No clustering was seen at 2000 K for PCAH such as coronene, however increasing the temperature to 2500 K led to hydrogen loss and chemical inception [315]. Chemical inception has been suggested at 2000 K if nickel is added [452]. However, even in combustion systems with large amounts of metals present, such as diesel engines, small amounts of metals are found in the soot suggesting no critical role of metals in soot formation [369]. Finally, aryl-linked hydrocarbons have been suggested to be prone to radical-induced fragmentation [152] and therefore many consider cyclodehydrogenation to be critical for the high temperature stability of these linkages [see Table 1(m)] as was discussed for the aromers.

More reactive edges on PAH molecules than maximally pericondensed were also suggested to contribute to polyaromatic inception, such as rim-based pentagonal rings on acenaphthalene or the 9, 10 low aromaticity free edge on phenanthrene [100]. While these edges are not able to crosslink with one another (*e.g.* [2+2] pericyclic reactions are symmetry forbidden [434]) [see Table 1(n) and Figure 18] they have significant reactivity with aryl σ -radical PAH [see Table 1(o) and Figure 18o)]. Significant bond energies of -44 kcal/mol have been calculated between phenyl radicals and acenaphthalene crosslinks, suggesting flame stability [503]. However, hydrogen addition to the unsaturated carbon part of the crosslink would lead to its breakdown. This could be overcome if hydrogen abstraction from the saturated carbon formed a closed shell C–C bond, which is highly stable [504] forming aromatic aryl-linked hydrocarbons (AALH) (see Figure 22a). As with the other aryl crosslinks a similar low collision efficiency would be expected as was determined for aryl, aryl crosslinks [316].

Another recent suggestion was a partial dehydrogenation to form a so-called E-bridge structure allowing the formation of 3D structures [152]. Evidence for such an E-bridge can be seen in the fully unsaturated dual pentagon species in Figure 1 IS30 from Commodo *et al.* [88].

Within an aromatic molecule π -electrons are able to form aromatically stabilised bonds, providing significant thermal stability within PAH and allowing for radical chain reactions [see Table 1(p) and Figure 18]. An odd number of π -electrons within hexagonal ring networks gives rise to a resonance stabilised π -radical (RSR). A mechanism where RSR crosslinks with aryl radicals forms a strong bond (80 kcal/mol) [234]. Critically, this is rapidly further stabilised by a unimolecular loss of hydrogen with a barrier of only 4.5 kcal/mol . This regenerates the RSR and further reactions with aryl radicals can occur. The ability to regenerate the reactive radicals led to the naming of the mechanism as clustering of hydrocarbons by radical-chain reactions (CHRCR) [see Table 1(r)] and

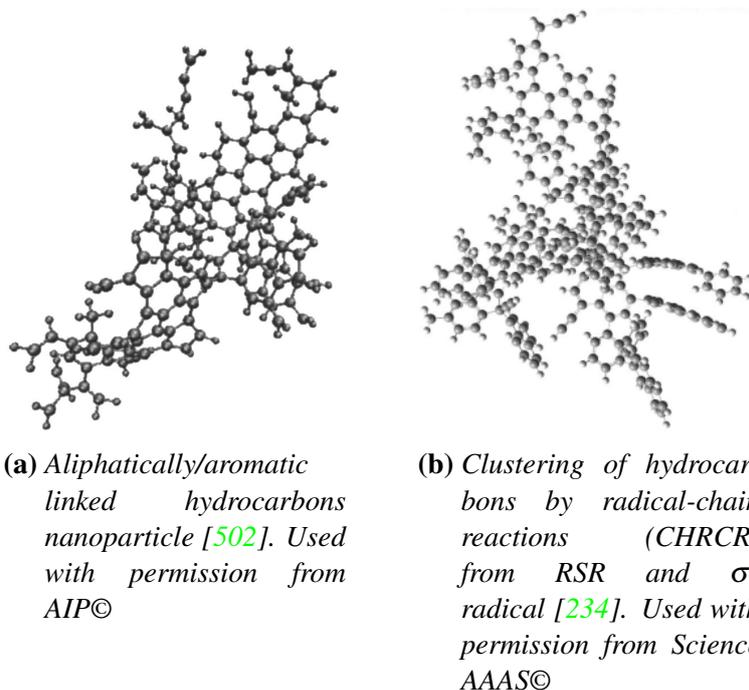


Figure 22: Nanoparticles from chemical inception mechanisms.

Figure 22b]. Unlike the mechanism between aryl and pentarings [see Table 1(p)] CHRCR does not require a subsequent hydrogen abstraction to produce a stable single bond as hydrogen is instead easily lost, restoring aromaticity to the π -radical.

However, such an increased reactivity for odd numbers of carbon atoms, most likely to be RSR, was not seen experimentally [243]. For this reason Homann suggested that RSR were not very reactive. While it is true that aromatic RSR are less reactive for recombination with themselves, reactions with σ -radicals were calculated to form strong bonds even more so than with pentaring polyaromatic inception [234]. A possible answer to the similar concentration of even and odd carbon fragments in flames could be inferred from the recent HR-AFM analysis of aromatic soot precursors [88]. Many regions of aromatic molecules with an odd number of carbon atoms, where one would anticipate an RSR to form, contained a hydrogen saturated edge carbon (most often on a zig-zag site). Therefore, while aromatic σ -radicals can react with RSR, it is unclear how hydrogen radicals could terminate these chain reactions. Hydrogen addition across the crosslink at the unsaturated carbon atom, or neighbouring site, could also lead to fragmentation [152]. Therefore, experimental evidence for this pathway is required as well as a full reaction mechanism that includes all pathways. A low collision efficiency would also be expected for this mechanism, as with other polyaromatic inception mechanisms (see Section 5.1).

4.4.2 Arynes

Arynes can form when two hydrogen abstractions occur from a PAH and have been suggested to allow for PAH crosslinking [82] [see Table 1(q)]. The simplest example is *o*-benzyne (1,2-didehydrobenzene see Figure 23), where benzene loses two neighbouring

hydrogen atoms [82, 201].

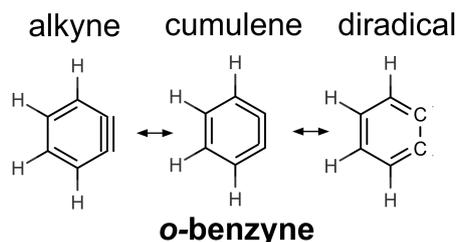


Figure 23: Kekulé structure for *o*-benzyne.

There are three main resonances that describe its electronic structure; the alkyne with a triple bond, cumulene with three neighbouring double-bonds and the open-shell diradical. There is little contribution from the diradical resonance structure (given a singlet-triplet splitting of 38 kcal/mol [522]). A more significant diradical character, and reactivity similar to two σ -radicals, is found for meta and para-benzyne (with singlet-triplet splitting of 21 and 4 kcal/mol respectively [522]). *o*-benzyne is closest to the cumulene structure from NMR studies. Recent HR-AFM suggest larger arynes are also dominated by the cumulene resonance structure, with contributions from the alkyne resonance as we will see. This electronic structure leads to a reduction in reactivity compared with a σ -radical, however, this may increase their concentration due to their reduced susceptibility to oxidation (as with the C3 pathway for benzene formation) or acetylene addition, making them of interest for polyaromatic inception [80, 82].

o-Benzyne rapidly dimerises, like a cumulene, to form biphenylene possessing an anti-aromatic 4-membered ring. Flash vacuum pyrolysis of biphenylene and polyphenylenes show thermal rearrangements to pericondensed aromatics with 5- and 6-membered rings, suggesting this pathway could contribute to PAH growth [398]. It can also react like an alkyne through a concerted Diels-Alder cycloaddition with acenes (see Figure 24). Reaction paths were computed showing a possible role for PAH growth and nanoparticle formation [82]. Fragmentation barriers of 40–47 kcal/mol indicate these crosslinks are thermally stable in flames. Rates for these reactions were not computed making the route difficult to compare with soot formation mechanisms. Other contributions of *o*-benzyne have been suggested in the decomposition of benzyl radicals studied in shocktubes [328] and combinations with (C_3H_3) resonantly stabilised radicals leading to a rapid pathway to indene [333], however, more work is needed to determine the role of these species in PAH growth.

The concentration of these species in flames is critical for assessing an aryne mechanism. Phenyl – produced by one hydrogen abstraction – is able to undergo a unimolecular decomposition to *o*-benzyne with a barrier of some 80 kcal/mol. This large barrier makes phenyl concentrations significantly greater than *o*-benzyne in flames [310]. It was also found that above 1500 K, the benzyne ring breaks open and the linear form of 1- C_6H_4 becomes dominant [310]. For larger PAH, hydrogen abstraction is unlikely to provide two neighbouring sites, given the average 1–6 σ -radical sites per 600 Da species as mentioned [213]. The other option for aryne creation is the decomposition pathway of the neighbouring hydrogen from larger σ -radical PAH. This has not been explored in larger

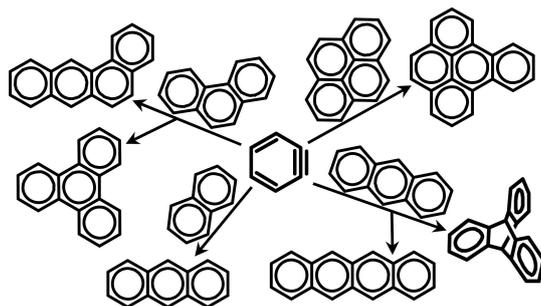


Figure 24: *o*-benzyne polyaromatic mechanism [82]. Used with permission from Elsevier ©.

PAH but if similar barriers are seen, as for phenyl, then concentrations of arynes would be expected to be low.

Finally, *o*-benzyne reacting with the rim-based pentagonal ring of acenaphthalene has been shown to form a 4/5-membered ring pair that breaks open into the 7-membered ring species pleidene [268]. This species and similar molecules readily dimerise through a cycloaddition reactions due to their diradical character [270]. These species have yet to be explored in the context of soot formation.

Indirect insight into an aryne mechanism in nanoparticle formation can be provided by a recent exploration of the pyrolysis of coronene and dibenzo[*a,e*]pyrene [387] (see Figure 25).

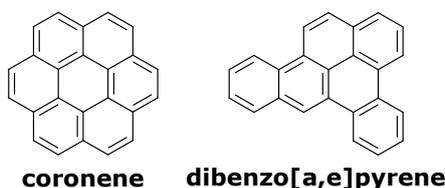


Figure 25: Kekulé structure for dibenzo[*a,e*]pyrene.

These two species have the same number of carbon atoms but significantly different edge types: coronene possesses a more condensed structure with six zig-zag and six free edges while dibenzo[*a,e*]pyrene possesses nine free edges, three armchair edges and two zig-zag edges. If an aryne route was dominant, the species with more free edges would be expected to dimerise more readily, forming more soot. However, dibenzo[*a,e*]pyrene, with its numerous free edges, inhibits soot formation compared to coronene (with more zig-zag edges than free), suggesting an aryne mechanism is not dominant.

4.4.3 Carbenes

Carbenes are neutral species with a valence of two and two unshared electrons. Methylene :CH₂ is the most well-known hydrocarbon carbene and is important in combustion for CH radical formation [145]. Carbenes have also been shown to be important intermediates for molecular rearrangements of larger PAH [398]. A variety of electronic spin configurations

are possible for such species (see Figure 26) [54]. For methylene the lowest energy state is the triplet (3B_1) with the singlet (1A_1) lying 9.0 kcal/mol higher in energy [229].

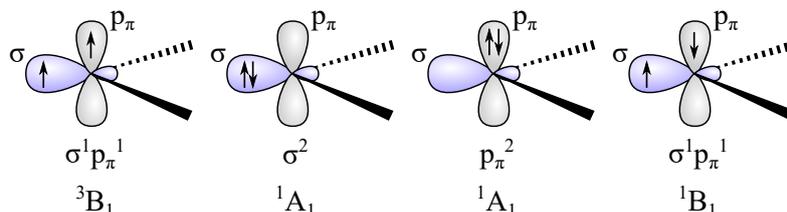


Figure 26: Carbene electronic spin configurations. Redrawn from [54].

Triplet carbenes possess high reactivity with methylene recombination rates 1–2 orders of magnitude faster than methyl ($\cdot\text{CH}_3$ a σ -radical) at flame temperatures [24]. Carbenes can be stabilised in the less reactive singlet states through heteroatoms [54] or solvation [90], which can lead to reduced reactivity as seen by considerable barriers to dimerisation [54, 171]. However, these effects are unlikely to be present in flames due to the low concentrations of aromatics.

Of interest for polyaromatic inception mechanisms are aryl carbenes (see Figure 27). For example, phenylcarbene could be formed in a combustion environment from hydrogen abstraction from benzyl, benzene with CH radical [196] and perhaps from carbon atom addition to benzene in rare cases [337].

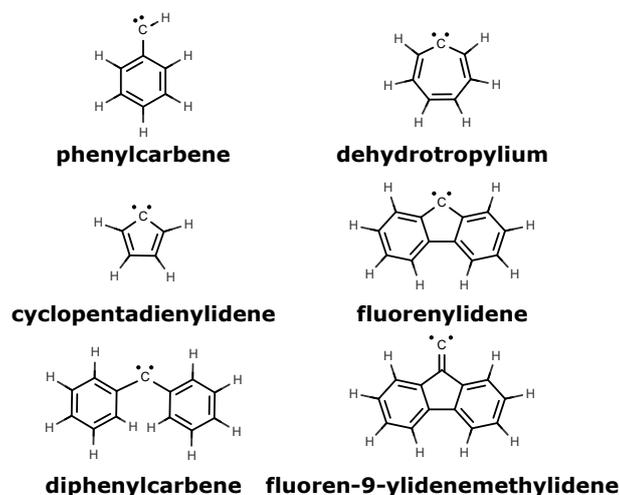


Figure 27: Kekulé structure for aryl carbenes.

This phenylcarbene could recombine forming the bridge that will be discussed in section 4.6. However, thermal rearrangement of phenylcarbene rapidly forms the more stable dehydrotropylium (or cycloheptatrienylidene) [282]. The electronic structure has yet to be confirmed for this product, however, calculations suggest two triplet states only 1.5 and 3.2 kcal/mol above the singlet ground state [440]. This indicates stabilisation through a cumulene structure as was seen for *o*-benzyne. Nevertheless, this species readily dimerises with rates yet to be determined. Further thermal decomposition of dehydrotropylium gives fulvenallene [282]. Fulvenallene is also known to crosslink [196].

At flame temperatures (1500–2000 K) even further fragmentation of fulvenallene forms cyclopentadienylidene, another carbene [196, 404]. Pentagonal ring containing carbenes such as cyclopentadienylidene and fluorenylidene are found to be reactive with a triplet ground state [40, 440] indicating greater reactivity than dehydrotropylium. Hexagonal ring carbenes with odd π -electron species such as phenalenyl and zig-zag edges have been suggested to dimerise rapidly [77]. However, reactivities similar to σ -radicals are predicted due to the delocalisation of the π -bonding system [389] as indicated by the low barriers for rotation [403]. For all these crosslinked carbene species rapid rearrangement to pericondensed species is found above 1200 K, potentially contributing to PAH formation [523].

A further option includes aromatics crosslinking through a carbene bridge, *e.g.* diphenyl-carbene. It is unclear how these would form in the flame, however, some stabilisation and reduced reactivity of the triplet carbene can occur for aromatic extension of phenyl-carbene providing decoupled localisable π -diradicals that polymerise [254, 530]. We will return to these diradicals in Section 4.6.

Finally, unsaturated (or “free”) carbenes could allow crosslinks ($(R_2)-C=C:$) *e.g.* fluoren-9-ylidenemethylidene. These could form in flames from hydrogen abstraction *e.g.* 9-methylfluorene. These species are able to dimerise as well as add across a double bond [474], however, these species have not yet been detected or explored in gas phase combustion chemistry.

Insufficient knowledge of the rates and reaction pathways makes it difficult to consider possible contributions of carbene mechanisms to PAH growth and nanoparticle formation. We therefore did not add an entry to Table 1. However, the high concentration of H radicals and H₂ in soot forming regions of the flame would suggest a small concentration of carbenes (as has been found from radical scavenging experiments of small aryl carbenes [182]).

4.4.4 Furans

Oxygen has been suggested to allow aromatic species to crosslink through 5-membered oxygen heterocycles [131] [see Table 1(r)]. Pyrolysis experiments have demonstrated that aromatic phenols allow for crosslinking followed by ring condensation [537] and there is some recent evidence from biofuel experiments that oxygen content can increase PAH or soot growth under certain conditions [345]. Furan-like PAH are found in some flames [232] and are a significant component of brown carbon [525]. However, large oxygen-rich PAH have not been found in most flames [208, 546], with a recent jet stirred reactor study concluding for oxygenated PAH (OPAH) [305]:

“ ... OPAH chemistry can be ignored in the soot nucleation process, since OPAH have significantly lower concentrations than PAH in soot formation”

Insignificant oxygen content has also been found in early soot particles [86]. A recent comparison of molecules predicted from these oxygen crosslinking reactions with those structures found in HR-AFM [88] indicate an overprediction of furan species [515]

(with none found in HR-AFM), suggesting significant fragmentation pathways are not included [305].

In summary, many polyaromatic inception mechanisms have been suggested. Some have been integrated into kinetic Monte Carlo simulations and have shown the ability to grow nanoparticles ≈ 2 nm in size [502] (see Figure 22a). We will return to comparing them in the final section.

4.5 Physical nucleation

Frankland was perhaps the first to consider a physical nucleation or condensation mechanism for soot formation. Upon lighting a candle at the summit of Mont Blanc he noticed a significant reduction in flame luminosity [146]. Back at the Royal Society he made use of air pumps to reproduce this effect as well as operate a candle above atmospheric pressure finding an increased flame luminosity, which indicated that soot formation was being inhibited or enhanced respectively. Frankland's initial suggestion that the emission of light from flames was not from solid particles but from a dense vapour was quickly disproved [293]. However, the strong pressure dependence of soot formation has long been seen as evidence for physical nucleation of hydrocarbons in flames.

Recent experiments on sooting flames within high pressure chambers further highlights the influence of pressure on soot formation [10, 89, 240]. Figure 28 reveals the increase in primary particle size of soot aggregates, sampled from within the pressure vessel, as the pressure was increased. Such a strong dependence is not seen for kinetically controlled chemical pathways in soot formation [87, 314], for example HACA growth, as they are characterised by reaction rates, which are first order in monomer concentration [511]. However, the significant increase in particle size and non-linear increase in soot volume with pressure [240, 332] suggest condensation, which is second order in monomer concentration [149, 511].

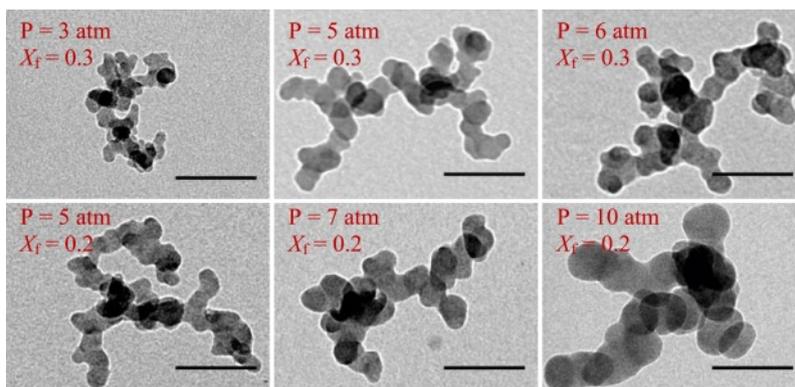


Figure 28: Soot sampled from counterflow diffusion flames over a variety of pressures [10]. Used with permission from Elsevier ©.

4.5.1 Aliphatic polymer

Polymerisation of fuel into an aliphatic polymer that condenses [see Table 1(s)] can be quickly dismissed given the rapid radical-induced fragmentation of aliphatic fuels in flames and that no large liquid particles are detected with laser scattering [195]. However, aromatic polymerisation [see Table 1(t)] has been considered in detail as mentioned in the previous section. After the influential paper of Rummel and Veh [424] suggesting that larger polycyclic molecules precipitate soot particles, Parker and Wolfhard suggested such a mechanism [393]. In their 1950 review they state,

“Higher hydrocarbons are formed by pyrolysis. The molecular weight and concentration of these increase until the saturation vapour pressure is exceeded, whereupon condensation occurs and fine droplets are formed.”

The higher hydrocarbons they discussed are crosslinked PAH that form an aromatic polymer which then condenses into a liquid droplet. The evaporation or thermal breakdown was proposed to be counteracted by carbonisation reactions. This mechanism represents a combination of many mechanisms already discussed, where PAH grow through the HACA mechanism, polymerise according to a polyaromatic inception mechanism and then physically nucleate. Such a proposal relies therefore on the mechanisms preceding condensation and is subject to their limitations.

Liquid halos around soot particles have been suggested to indicate a liquid-like mechanism that subsequently carbonises and forms soot [415]. Recently evidence was found that this halo is most likely a sampling artifact [51, 53]. Invasive sampling often involves injection of a cold probe onto which soot particles are thermophoretically deposited. Figure 29 shows the impact of the probe’s residence time in the flame which we obtained using a high speed camera. For long residence times a liquid halo is observed, however, upon decreasing residence time the liquid halo is removed [51, 53]. It was also interesting to observe the evaporation of these halos if the sample was left in the electron microscope’s vacuum for 24 hours, indicating it is not persistent at flame temperatures (other insights into the electron beam intensities required to not cause nanostructural changes are also reported [53]). As mentioned, other non-invasive techniques (X-ray or optical scattering) confirm that there is no evidence for these large liquid-like droplets [195].

A simple explanation for this observation in the TEM and AFM is that during the rapid cooling from thermophoretic sampling the soot particles present in the flame act as nucleation sites for the condensation of aromatic soot precursor molecules present in the gas phase. This is supported by the fact that the effect is only seen in diffusion flames or very rich premixed flames, where aromatic concentrations would be high enough to enable condensation [468] (see Figure 5d). As mentioned in Section 2, these species have been previously called brown carbons or tar and have been considered more important in turbulent flames such as forest fires, where aromatic species can escape the flame front and condense on soot.

It is clear, however, that as the primary particles traverse the diffusion flame the brown carbon becomes harder to remove as our sampling is limited in its speed [51]. In particular, just prior to coagulation of the primary particles into aggregates it was found to be

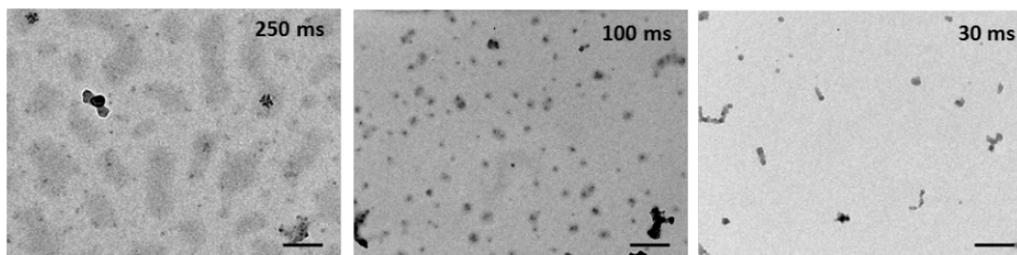


Figure 29: TEM images of soot sampled at 25 mm HAB and different exposure times. The calibration bar in the images corresponds to 200 nm.

increasingly difficult to sample rapidly enough to remove the halo, suggesting the aromatics are increasing their boiling point as they grow. Wang *et al.* also showed with infrared spectroscopy that the early soot particles are low in aliphatics but that these increase as they mature, which is assumed to be due to hydrogenation of the surface [59]. This suggests an increase in reactivity of the surface. However, these discussions do not principally concern nanoparticle formation.

4.5.2 fPAH

Direct physical nucleation of flat PAH species (fPAH) [see Table 1(t) and Figure 18] has been, arguably, the most widely explored mechanism in soot nanoparticle formation. This suggestion was considered unlikely by Haynes and Wagner in their 1981 review given the low boiling/sublimation temperatures for PAH molecules [195]. While condensation was seen as unlikely, the evidence for stacked aromatic species grew following the discovery of a green fluorescence signal in flames in the 1980s (see Figure 4), as mentioned in Section 2.

Miller turned to the formation of molecular clusters and used, as a proxy to cluster stability, the dimerisation of PAH in flames employing intermolecular potentials, suggesting it could be possible for larger species to condense [356, 359]. These results were extended by performing highly accurate calculations of intermolecular energies between PAH and provided a new description of the intermolecular interactions, making use of the SAPT(DFT) method to develop the isotropic PAH anisotropic potential (isoPAHAP) [488]. Experiments confirmed the accuracy of the forcefield in describing both the virial coefficient for benzene and the exfoliation energy of graphene [488]. More recently, scanning tunnelling microscopy of coronene clusters revealed similar morphologies to isoPAHAP clusters compared with other potentials [516] (see Figure 30).

Wang developed a full statistical description of PAH homodimerisation using statistical mechanics [511]. This was combined with the isoPAHAP forcefield allowed for the determination of the intermolecular vibrations, ν_i , and intermolecular interactions, E_{int} , for fPAH [488]. The equilibrium constant for dimerisation could then be computed as;

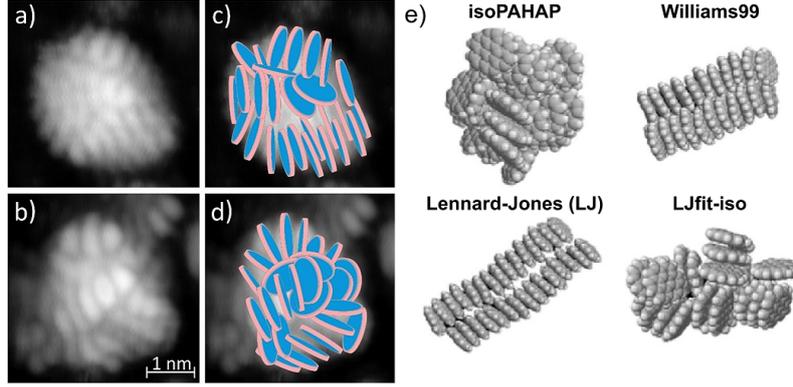


Figure 30: *a-b) Scanning tunneling microscopy imaged clusters of coronene molecules. c-d) Shows potential orientations of the coronene molecules in these clusters [516]. e) Shows the computational results from clusters formed during a molecular dynamics simulation of coronene with different forcefields used [394]. Used with permission from Elsevier©.*

$$\Delta H = \sum_{i=1}^6 \left(\frac{1}{2} + \frac{1}{\exp(h\nu_i/k_B T) - 1} \right) h\nu_i - 4k_B T - E_{int}, \quad (21)$$

$$\frac{\Delta S}{k_B} = \ln \left[\frac{h^6 p}{\pi^4 (8M)^{3/2} (ek_B T)^4} \frac{\sigma_m^2 (I_{A,d} I_{B,d} I_{C,d})^{1/2}}{I_{A,m} I_{B,m} I_{C,m}} \right] + \sum_{i=1}^6 \left[\frac{h\nu_i/k_B T}{\exp(h\nu_i/k_B T) - 1} - \ln(1 - \exp(-h\nu_i/k_B T)) \right], \quad (22)$$

$$K = \exp \left(-\frac{\Delta H - T\Delta S}{k_B T} \right), \quad (23)$$

where ν_k is the k th intermolecular vibrational frequency, E_{int} is the dimer interaction energy, h is Planck's constant, k_B is the Boltzmann constant, T is the temperature, $I_{k,m}$ and $I_{k,d}$ are the moments of inertia for monomer and dimer respectively, for the k th principal axis of each, M is the monomer mass and σ_m and σ_d are the symmetry numbers for the monomer and dimer, respectively. Figure 31 shows the equilibrium constant of dimerisation for various sized fPAH, where $K > 1$ dimerisation is favoured. The curves reveal that species larger than circumcoronene ($C_{54}H_{18}$, 667 Da) would be required to form stable dimers at temperatures in the flame where soot begins to form (1500 K).

Figure 31 also shows collision efficiencies of fPAH, determined from molecular dynamics simulations [489], providing a more straightforward comparison with polyaromatic inception mechanisms. A comparison is drawn with collision efficiency to be required to explain experimental PAH mass spectra [411]. It is clear that insufficient collision efficiencies are found for physical nucleation of the size of species found to cluster in the flame at 1500 K. This analysis is consistent with a recent estimate of the boiling point of fPAH [306]. It was found that a fPAH with 60–65 carbon atoms would be required to form liquid particles at temperatures within the flame where soot forms (1450–1700 K) considering the low partial pressures of aromatics found in flames.

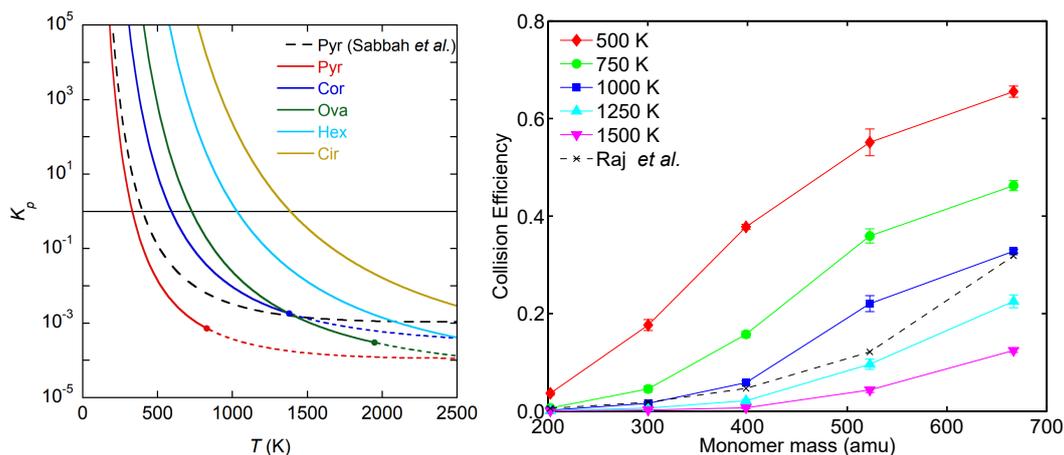


Figure 31: (left) K as a function of temperature for *pyrene*, *coronene*, *ovalene*, *hexabenzocoronene* and *circumcoronene* with 4, 7, 10, 13 and 19 rings respectively [489]. (right) Collision efficiency of fPAH derived from molecular dynamics simulations. Experimentally determined values by Raj et al. also shown [411].

Other suggestions were made for the stabilisation of moderately sized PAH clustering through activation of non-equilibrium internal rotations. In molecular dynamics simulations of colliding PAH species, Miller observed orbiting of the PAH [356]. Schultz and Frenklach explored this effect using a quantum molecular dynamics approach and found evidence for internal rotors [442]. The establishment of internal rotors were suggested to remove thermal energy from intermolecular vibrations between the clustering PAH reducing fragmentation. From vibrational analysis only one bound internal rotor can be identified ($\sim 10 \text{ cm}^{-1}$ twisting mode) [489]. In a non-equilibrium scenario it was estimated that at least four internal rotors would be required to provide a significant nucleation flux [152, 511]. Experiments on supersonic jets of pyrene also confirm the lack of stability past its boiling point [427]. These results suggest that non-equilibrium effects are unlikely to enable a physical nucleation of PAH.

4.5.3 Aliphatic chains

The presence of aliphatic chains was suggested to improve the clustering of fPAH due to the entropic advantages of more internal degrees of freedom [75, 130] [see Table 1(u)]. These chains have been observed in HR-AFM of PAH [444] (see Figure 32).

Metadynamics simulations were employed that allowed the free energy to be directly and economically computed from molecular dynamics simulations with guided dynamics [75, 130]. Again, similar results were found for pericondensed PAH but soft modes could be included from aliphatic chains. They were found to improve the clustering rate but the collision efficiencies were similar to the pericondensed sub-structure, indicating it is the dispersion interactions between the pericondensed structure that still govern the ability to form complexes at high temperature. However, for 500 Da mass species the chains are still unable to provide the increased intermolecular forces required to allow for clustering

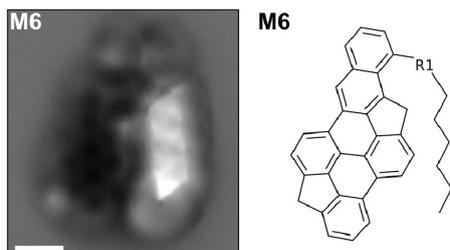


Figure 32: HR-AFM image of an aliphatic chain attached to an aromatic [444].

at temperatures exceeding 1500 K.

4.5.4 Aromatic polymer

Evidence for heterogeneous nucleation, where aromatic polymers are nuclei, has also been seen within some early primary soot particles [see Table 1(v)]. High resolution transmission electron microscopy, which is sensitive to stacked aromatic structures, has found disordered cores without such stacking [223] (see our own image Figure 33). Automated methods to detect these regions have been developed in fringe analysis software [485]. This feature has been interpreted as indicating an aromatic polymer nuclei [181]. It should be mentioned that other fuels provide early primary soot particles with significant internal fringes *i.e.* do not contain disordered nuclei [52].

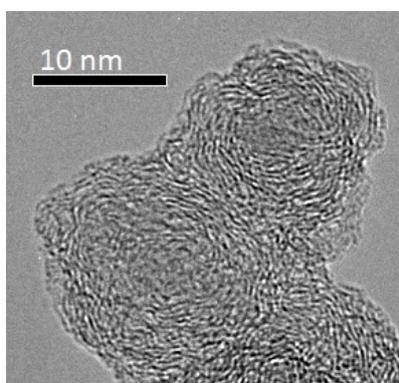


Figure 33: Soot primary particle from a 10% cyclohexane doped hexane co-flow diffusion flame imaged with HRTEM showing disordered cores.

The possibility of aromatic polymers acting as nuclei for heterogeneous nucleation was explored by Chung and Violi in 2011 [75]. Fullerenes (C_{60} and C_{180}) were used as proxies for these nanoparticles. Little impact on the rate of clustering was found for heterogeneous nucleation of fPAH in these simulations. Classical nucleation theory would dictate that the vapour needs to be supersaturated before condensation is possible heterogeneously [241]. Therefore, while the nuclei can reduce the barrier for nucleation and therefore increase the nucleation rate, they cannot allow condensation of species that lack sufficient intermolecular interactions to condense.

The condensation of polyaromatic clusters formed via aryl-linked PAH have also been

suggested. Using molecular dynamics simulations, aryl-linked PAH were found to cluster with greater propensity than their monomeric components, however, the two aromatic planes were not coplanar, which significantly reduced physical interactions compared with similar sized pericondensed PAH [217]. Therefore, for the same reason pericondensed fPAH are unable to cluster, aryl-linked PAH are unlikely to be able to condense until they grow to larger than 5 nm [212] (see Section 5.1 for full comparison).

4.5.5 Penta-linked (APLH)

Pentagonal ring linked aromatic species can form planar species with similar cluster behaviour as planar pericondensed PAH [see Table 1(w) and Figure 18]. Recent HR-AFM results demonstrated planar aromatics crosslinked through pentagonal rings (see Figure 1 IS43). It was found that these species could form through a σ -radical on a rim-based pentagonal ring attacking a rim-based pentagonal ring (aryl-pentaring mechanism) [396] (see Figure 34).

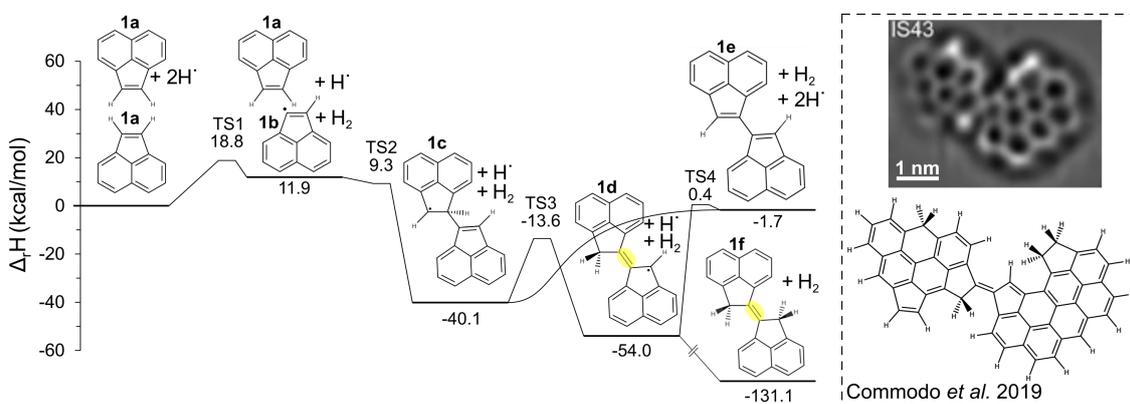


Figure 34: Potential energy surface of the planar crosslinked aromatic molecule with a double bond (highlighted in yellow) (at 0 K with M06-2X/cc-pVTZ+ZPE level of theory). Inset shows similar species from HR-AFM [88] used with permission CC BY-NC-ND 4.0.

If the pentagonal ring is partially saturated a double bond forms between the two pentagonal rings leading to a flat geometry. Metadynamics studies showed this crosslinked molecule to have a similar free energy profile to a similar sized pericondensed species. Molecular dynamics confirmed that the planar penta-linked species clusters at a similar rate to the pericondensed molecule. Species **1d** in Figure 34 will be discussed later as it is a localised π -radical able to bond and stack.

Another planar penta-linked aromatic crosslink could be formed by a σ -radical on a 6-membered ring attacking a rim-based pentagonal ring. Frenklach and Mebel recently showed this species can dehydrogenate to form an E-bridge structure, as mentioned [152]. Further dehydrogenation could lead to a planar structure (see Figure 1 IS43). However, as with fPAH these penta-linked species are unlikely to possess the interaction energies to condense at temperatures within the flame where nanoparticles form.

4.5.6 cPAH

Homann was one of the first to consider that curved polycyclic aromatic hydrocarbons (cPAH) could cluster and lead to soot formation [25] [see Table 1(x) and Figure 18]. The discovery of fullerenes in flames helped support such a suggestion [164, 208] as well as the extraction and detection of corannulene in flame products [283]. Evidence was also provided from species found in the negative ion mass spectrometry that led to fullerene formation [208], cPAH being more likely to form negative species due to their high electron affinity [110]. More recently, high resolution transmission electron microscopy suggested a significant fraction of early soot nanoparticles contain cPAH [323, 510].

Figure 35 shows the electrostatic potential surrounding water, corannulene (a cPAH) and coronene (an fPAH). Corannulene possesses a similar dipole moment to water, however, it still has a similar local quadrupolar charge distribution to coronene. This polarity is due to the flexoelectric effect [322], where pyramidalisation of sp^2 carbon networks rehybridises the π -bonding network [123, 237, 281]. Small PAH were unable to curve until at least six rings are present with an internal 5-membered ring being critical [323]. For the size of species found in early soot nanoparticles this dipole is considerable (between 4–6.5 debye) [322]. These larger cPAH (>11 rings, \approx 450 Da) were found to be persistently polar at flame temperatures and did not invert at temperatures within the flame where soot forms [326].

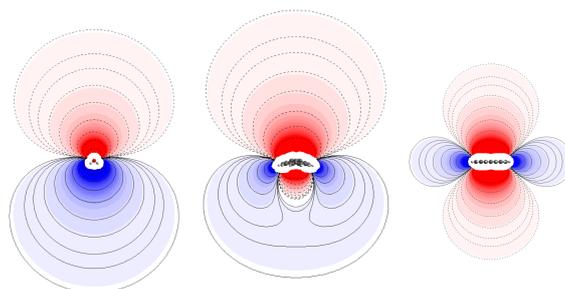


Figure 35: Cross section of the electric potential, (+) blue, (-) red for water, corannulene and coronene [324].

How does this electric dipole moment possibly improve the clustering of cPAH compared with fPAH [323]. Comparing the dimerisation energy between cPAH and fPAH we found little difference for 1–2 pentagonal rings with a significant decrease in binding energy for cPAH with ≥ 3 internal pentagonal rings [323]. High accuracy calculations (SAPT(DFT)) revealed that while the dipole moment does enhance the binding energy, the steric issues of stacking cPAH led to reduced dispersion interactions [323]. A new forcefield, curPAHIP, was developed to see whether this result translated into an enhanced clustering rate [55]. While collision efficiencies were greater for corannulene compared with coronene, the similar binding energy meant little difference was found in clustering behaviours, thus suggesting cPAH nucleation is as unlikely as fPAH nucleation. Finally, for heterogeneous clusters of cPAH some enhanced interactions were found where the smaller cPAH fits into the concave side of larger cPAH, however, this enhancement was not found to be significant [56].

4.5.7 ion, fPAH

Frenklach and Wang in 1991 were among the first to suggest the possibility of an ion-induced physical nucleation mechanism in soot formation [153] [see Table 1(y)]. Experimental work on cationic benzene dimers had found an enhanced binding energy increasing from -0.5 – 3 to -17 kcal/mol for the neutral to the cationic dimer, respectively [307, 454]. More recently, computational work on larger PAH cationic dimers found binding energies in the range -15 – 20 kcal/mol for PAH with 4–5 rings [MP2/6-31G(d)] [419]. Larger clusters were recently explored using basin hopping and density functional tight binding methods [120]. More compact clusters were formed with a positively charged dimer or trimer in the centre, indicating that the enhanced binding energy is only reserved for a few molecules in the cluster adjacent to the ion. Cation- π interactions are more significant with small cations such as metals or flame ions. Binding energies to benzene of -108 and -151 kcal/mol were found for Mg^{2+} and Fe^{2+} , respectively [266], while the $1+$ cation Na^{1+} was found to be weakly bound with -21 kcal/mol. Binding energies of larger PAH (1–4 rings) with more flame relevant chemi-ions were recently computed [69]. Binding energies of -30 – 60 , -18 – 27 and -26 – 32 kcal/mol were found between CHO^+ , $c\text{-C}_3\text{H}_3^+$ and H_3O^+ , respectively. Chen and Wang noted;

“...the cation-enhanced binding remains to be too weak to impact the gas-phase PAH chemistry or the clustering of PAHs leading to soot nucleation.”

4.5.8 ion, cPAH

Curved PAH, unlike planar PAH, have considerable interactions with ions due to their polarity. This could lead to an ion-induced nucleation mechanism [see Table 1(z) and Figure 18]. cPAH–ion interactions are well known [124] and have been used in lithium ion storage [543]. We have previously mentioned the large number of ions present in flames from chemi-ionisation reactions. In 2018, a binding energy between $c\text{-C}_3\text{H}_3^+$ and a 15 ring cPAH with two pentagonal rings were computed to be -40.6 kcal/mol [323], suggesting important interactions for soot formation. Quantum *ab initio* molecular dynamics revealed this complex to be stably bound at 1500 K over 2 ps [326]. Molecular dynamics simulations of corannulene clustering revealed a near doubling of the clustering rate with ions present, while no difference was found for coronene clustering in the presence of ions [55] (see Figure 36). However, only a couple of cPAH can be bound to an ion with further growth requiring supersaturation of the vapour of cPAH from classical nucleation theory [241], which we have previously demonstrated as being unlikely.

Such a mechanism could perhaps explain the positively charged experimentally nanoparticle mode, mentioned in Section 2.1, as correlations have been found with large aromers species in low pressure acetylene flames and this mode [210]. Larger nanoparticles are found to take on a charge distribution given by thermal equilibrium [450, 514], however, the speed with which they acquire their charge indicates it is not from thermal ionisation but from coagulation of charged nanoparticles suggesting a link between larger soot particles and this mode [143]. Finally, recent work showed a high charge fraction (up to 95%) of sub-3 nm nanoparticles in the flame front where the chemi-ion concentration is greatest [536]. This could provide evidence for the charged nanoparticle mode in atmospheric

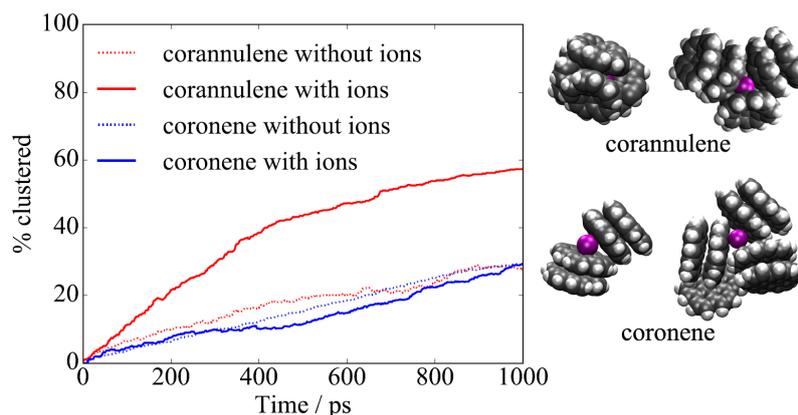


Figure 36: Clustering of *cPAH* corannulene and *fPAH* coronene at 500 K with and without ions (K^+) present [55].

flames. However, it is clear that these nanoparticles do not contribute significantly to primary particle formation with a recent study measuring the charge fraction of sub-10 nm nanoparticles concluding that [514]:

“Ion-induced soot nucleation was not the main contributor to nucleation since the charge fraction was less than 10% when $T_{max} < 2000$ K.”

In summary, physical nucleation provides a rapid soot formation pathway, given that sufficiently strong intermolecular interactions allow for a supersaturated vapour to form. However, the clustering PAH in flames of mass 500 Da are found instead to have interactions too weak to explain soot formation.

4.6 Physical + Chemical

The crux of the soot formation problem is that the physical and electrical condensation of precursor molecules is rapid but too weak to hold soot together, while most chemical bonds are strong but the mechanisms proposed to date are too slow to account for rapid growth of soot as observed in experiments. A mechanism that combines both aspects, condensation and chemical bonds, is required – so-called physically stabilised soot inception.

One of the first clear articulations of such a proposal was from Harris and Weiner in 1989 [191]:

“Once coagulated they will quickly become chemically knit together since a significant fraction of the aromatic species are radicals.”

Miller followed with a similar suggestion in 1991 that [356]:

“...if individual PAH or their dimers undergo rapid, irreversible reactions, the net rate of production of the soot nuclei may be sufficiently high so that the

concentration of the nuclei far exceeds the concentrations of the reacting, intermediate species.”

Frenklach and Wang developed this suggestion into a kinetic model for soot formation, where PAH dimerisation was assumed to be irreversible, facilitated by some sort of chemical or non-equilibrium process [153]:

“...one cannot judge the PAH coagulation flux using the equilibrium assumption – these fluxes must be computed kinetically. The equilibrium among individual PAHs and clusters may never be attained, and the mass flux is likely to be driven by an irreversible process following the dimer formation...It is also possible that a PAH dimer is stabilized by a reaction with an aliphatic, forming a covalently bonded link between the PAH layers... the van der Waals enhancement should be larger than the factor of 2.2 assumed in the present study.”

This irreversible nucleation of PCAH was the first successful kinetic model of soot formation that captured the particle number as well as the volume fraction [153, 329–331, 512]. Similar suggestions have been proposed recently such as the reactive dimerisation models [251, 252]. These models have arguably been the most successful in describing nanoparticle formation in flames. This section details some possible detailed mechanisms to explain such a “middle way”.

4.6.1 Zipper mechanism

Homann suggested that an aryl-linked PAH dimer could fold upon itself then react at the rim, releasing hydrogen and becoming a curved PAH or a fullerene – the zipper mechanism [7, 25, 208] [see Table 1(aa)]. Aryl-linked hydrocarbons are unable to bond without disrupting the stacked configuration (for the size of PAH found in flames) due to the direction of the σ -radical bonding that is optimal when the bond is colinear with the aromatic planes. For fullerene formation it has been found instead that near-complete loss of hydrogen is required before the carbon will curl and close into a fullerene [429].

4.6.2 Internal rotors

Frenklach and Mebel recently suggested an enhancement of polyaromatic inception due to colliding PAH activating internal rotations [152] [see Table 1(bb)]. These rotors were argued to provide multiple opportunities for an aryl-radical to attach to a reactive edge of a PAH such as a rim-based pentagonal ring. For an internal rotor to be persistent between non-bonded monomers they must be strongly bound. Interactions in the T-configuration (C–H with π -network) are too weak to provide a persistent internal rotor [487]. Therefore, the only bound internal rotor that could form, from analysis of the intermolecular vibrations, is the twisting mode of a stacked dispersion stabilised PAH dimer [489], thus the reason for its consideration in this section.

This internal rotor could indeed increase the chance of a radical reacting with a reactive edge. Insights into such a scenario can be gained from recent quantum molecular dynamics simulations of pyrene radical attacking the 9,10-free edge at very low temperatures [73] (see Figure 37). Preliminary results of aryl-radical recombination in reactive

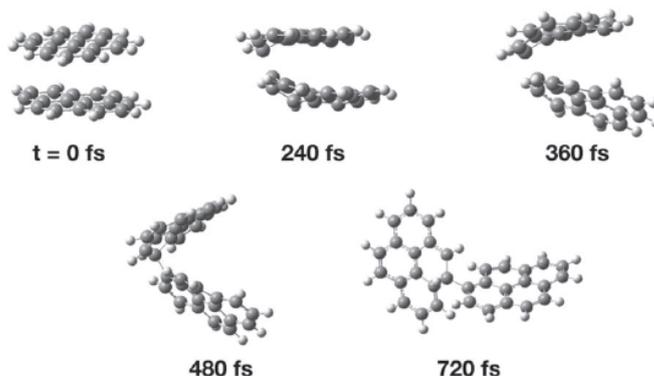


Figure 37: *Quantum molecular dynamics simulations at low temperature [$T = 4$ K ADMP B3LYP-D3/3-21G*] of stacked pyrene with the lower species possessing a σ -radical [73].*

molecular dynamics at flame temperatures did not reveal such an enhancement [316], however, significantly larger PAH would be required to see the bound internal rotor at temperatures within the flame where soot forms. More work is clearly required to examine the impact of internal rotors in enhancing polyaromatic inception.

4.6.3 Bridge-linked (ABLH)

Aliphatic bridges between stacked PAH have also been discussed in detail since the 1990s [see Table 1(cc) and Figure 18]. In relation to the formation of interstellar dust, a mechanism was proposed by which a “cross-linked structure of aliphatic and aromatic hydrocarbons” formed and was suggested to explain soot formation under certain flame conditions [149, 371]. Aliphatic bridges were also included in the early models of stacked species from Homann et al. [25], which showed the first stacked complex that was stabilised by an aliphatic chain. This mechanism was suggested as part of the formation of some of the smallest nanoparticles in flames with D’Alessio commenting during the 1994 Heidelberg soot workshop [125]:

“We think of two-ring structures connected together with some non-aromatic, some aliphatic bridges. You may also think about oxygen bridges...”

We will come back to the oxygen bridges. This description would later become known as aromatic aliphatic-linked hydrocarbons (AALH) [148] with aryl-linked pentagon containing species being introduced later [100].

Molecular dynamics revealed that aliphatic bridged ($[\text{CH}_2]_n$, $n = 2$) aromatics of mass ~ 250 Da were found to stack below the boiling point of the aromatic species [75, 529].

However, at flame temperatures (above the boiling point) these physical interactions were overcome and clustering of these species was at a significantly lower rate compared with pericondensed PAH. Considering also the hydrogen content required for aliphatically-linked chemical mechanisms at least one $[\text{CH}_2]_n$, $n = 1$ linkage would be required per PAH. This would lead to an H/C ratio greater than one, when most early soot nanoparticles have $H/C = 0.5$. However, the rapid carbonisation processes that occur in flames could rapidly decrease the H/C ratio, so this is less conclusive.

Detailed kinetic mechanisms of how these aliphatic crosslinks form and fragment have also not been explored in significant detail. Some kinetic Monte Carlo codes do include such aliphatic crosslinks allowing comparison with other chemical pathways [502, 504, 505]. However, the aryl, aryl bonds continue to be more dominant than these aliphatic links (high collision efficiencies between radicals were assumed). More recently, for a $[\text{CH}_2]_n$, $n = 2$ aliphatic crosslink, one conceivable option is the reaction between two benzylic methylene π -radicals. Simulations and experiments have recently been performed using free electron laser IR radiation and mass spectrometry to probe the pyrolysis products of benzyl and indenyl [202, 461, 462]. The crosslinked species bibenzyl was found and shown to rapidly cyclodehydrogenate into pericondensed structures in a similar manner to the aryl-linked species discussed previously. These methyl radical sites could form from hydrogen abstraction of a methyl group. Methyl radical sites $-\text{C}^*\text{H}_2$ have not been directly imaged using HR-AFM, however, the precursor $-\text{CH}_3$ group has been imaged in soot precursor molecules using HR-AFM [88]. Another possible mechanism by Chen and Wang [69] involves C_3H_3^+ reacting with the edge of a PAH to provide a methyl radical group. It is also conceivable that for larger PAH the rearrangement reactions could be less important. Aliphatic bridges have yet to be imaged using HR-AFM (while they have been imaged in pitch [72]) although some preliminary evidence for them in the low temperature regions of an inverse diffusion flame has been found [2].

Acetylene groups attached to the edge of PAH have also been suggested to crosslink the PAH, reacting either with an RSR [166] or PAH σ -radical [542] [see Table 1(dd) and Figure 18]. All aliphatic and acetylene bridges detailed to date are prone to significant radical-induced fragmentation as mentioned in polyaromatic inception Section 4.4 [152, 414].

Finally, an oxygen-containing double crosslink was suggested between PAH where one is a RSR [318] [see Table 1(ee) and Figure 18]. The impact of oxygen crosslinks can be considered minimal in most cases due to the lack of significant oxygen in soot nanoparticles [86] and the ability of pyrolysis reactors to produce soot without oxygen being present [420].

4.6.4 Excimers

Excimers have been discussed as evidence for stacking of aromatic species in the previous section but they also provide a bound state that has been suggested to stabilise soot nanoparticles [357]. Figure 38 shows the potential energy surface for the ground and excited states of a stacked aromatic dimer [346, 357, 431]. After laser excitation of a π - π^* transition on one of the aromatic planes, the excited state delocalises over the dimer lead-

ing to an energy reduction. The binding energy D_e is usually defined as the energy for the excimer to dissociate (see Figure 38). A wide range of small fPAH species have been calculated with binding energies up to -20 kcal/mol found [278, 346], too low to provide significant stabilisation at flame temperatures. The stabilisation is also only appreciable between pairs of species; the trimer is found to be weakly bound indicating the excimer is only able to delocalise effectively across two species [102].

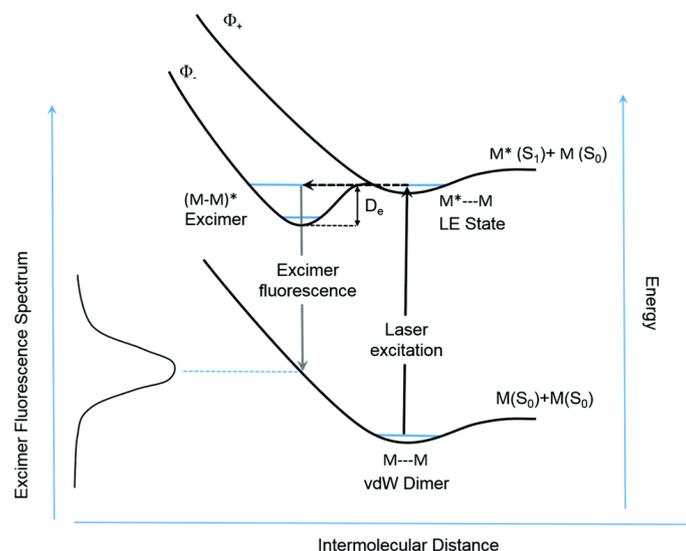


Figure 38: Potential energy surface for the optical states of an aromatic dimer. The binding energy of the excimer is indicated by D_e [346].

Time resolved studies have found lifetimes of tens of nanoseconds for the excimer state [346], which are too short to provide stability over the hundreds of nanoseconds to milliseconds required for soot nanoparticle formation. Finally, insufficient UV light is produced in the flame to maintain a sufficient concentration of these species. This is evidenced by no spontaneous emission of the excimer signal. These excimers therefore require external, often laser, illumination to maintain and produce the fluorescence response.

An interesting aside is that aliphatically bridged species still produce the excimer signal [278], indicating that stacked, non-conducting bridges also possess the excimer signal (see Figure 39). They were also able to show that the effect is significantly different in excimers containing pentagonal rings forming more tightly bound structures (for cyclopentadiene increasing to -32 kcal/mol), leading to a decreased fluorescence emission [279].

4.6.5 Multicentre-linked (pancake) (AMLH)

The term ‘‘Pancake bond’’ was coined by Mulliken and Person in the 1960s [377] to describe a multicentre two-electron bond [see Table 1(gg) and Figure 18]. These form when AB stacking of aromatic species, both with an odd number of π -electrons in an aromatic network, allows for the two singly occupied molecular orbitals (SOMO) χ_a, χ_b to form a multicentre bonding molecular orbital, $\phi_+ = N_+(\chi_a + \chi_b)$, where N_+ is the normalisation constant [246] (see Figure 40). These bonds form between π -radicals that are delocalised

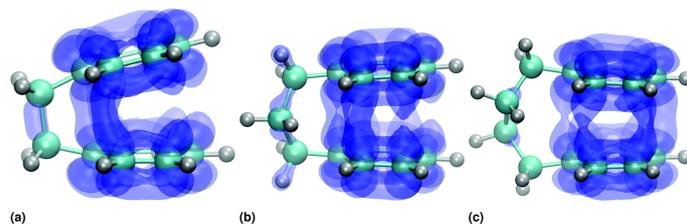


Figure 39: Isosurfaces (± 0.05) of the orbitals involved in the $S_0 \rightarrow S_1$ optical transition for aliphatically bridged benzene dimers [278]. Used with permission from the Royal Society of Chemistry ©.

on the edge of a 6-membered network. For larger non-symmetric aromatic species it was found that the multicentre bond only forms across a few edge carbon atoms [325], which can be seen in Figure 40.

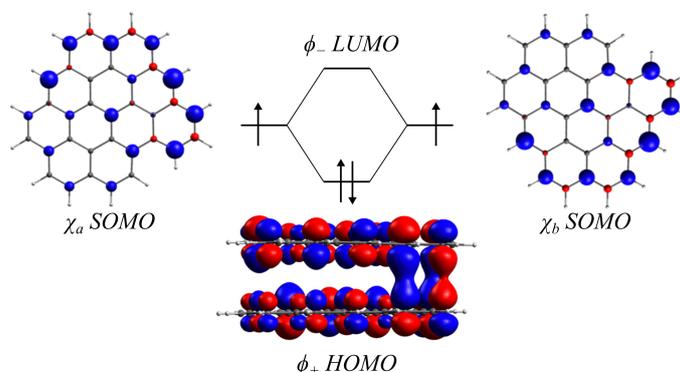


Figure 40: Molecular orbital representation of pancake bonding where two singly occupied molecular orbitals (SOMO) χ_a and χ_b form a multicentre two electron bonding highest occupied molecular orbital (HOMO) ϕ_+ . Based on Kertesz [246].

In flames, odd π -electron aromatics have been directly imaged in soot precursors using HR-AFM [88] and have been suggested to stabilise soot nanoparticles [469, 506]. However, the pancake bonding is weak due to the strong Pauli repulsion from the molecular orbitals not involved in the pancake bond. Therefore, poor overlap between orbitals is found in these multicentre bonds with < 10 kcal/mol of additional interaction above that of the dispersion interactions [246, 325]. They are also highly angle dependent, breaking after rotating by 30° , requiring strict AB stacking [93]. In fact, for small species such as phenanenyl, a non-stacked crosslinked species is lower in energy than the stacked configuration (a so-called σ -dimerisation [372]). This σ -dimer has been shown to dehydrogenate forming a 7-membered ring fPAH [493].

4.6.6 Zig-zag-linked (AZLH)

Wang was the first to consider localisation of π -radicals due to diradical character (diradicaloid) in the context of soot formation in 2010 [511] and since then considerable work

has been undertaken to explore their impact on soot formation [see Table 1(hh) and Figure 18]. Localised states have been experimentally observed and computationally studied at the zig-zag edge of graphene [260, 262, 383, 479]. Some aromatic molecules with dual zig-zag edges and an even number of π -electrons can possess a diradical character. In Section 4.4.3, we introduced carbyne and carbene diradicals formed with σ -radicals. A 2019 review from Hofmann et al. [478] provided a comprehensive discussion of diradical reactivity of π -radicals. Firstly, they distinguish between localisable and nonlocalisable diradicals. For the former, an orbital transformation is able to “localize their singly occupied orbitals on different sites so that they do not share a considerable region of space.” [478]. Carbynes and carbenes are examples of unlocalisable diradicals for which a complex interplay between exchange and coulomb interactions determines whether the species is closed-shell singlet or triplet and determines the reactivity. This orbital localisation can be performed for most π -networks, making them localisable diradicals. While many metrics have been proposed, the recommended indicator for diradical character in these localisable diradicals (for which the exchange interactions are weaker) is the singlet–triplet energy splitting ΔE_{ST} . Figure 41 shows the transition from a closed-shell species where the singlet is lower in energy.

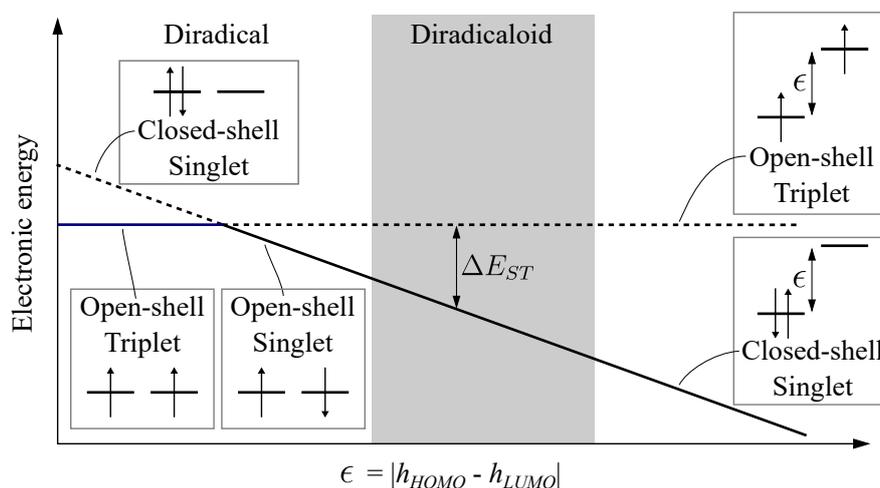


Figure 41: Schematic showing the energies of the triplet and singlet as the degeneracy between the frontier orbitals, ϵ , is lifted. Redrawn from Stuyver et al. [478]. Note that h_{HOMO} and h_{LUMO} are the one-electron energies associated with the HOMO and LUMO and not the full orbital energies. The triplet is shown as constant to allow for comparison.

As the difference in the one-electron energy of the frontier orbitals, ϵ , decreases it gains diradical character, $\Delta E_{ST} \rightarrow 0$, which is named a diradicaloid (usually considered to be thermally accessible). A diradical forms when the localisable orbitals become degenerate, $\epsilon = 0$, giving either an open-shell singlet or triplet, depending on magnitude of the Coulomb and exchange interactions as well as potential spin polarisation effects [478]. A clear indication of diradical character is if the triplet is lower in energy than the closed shell singlet, $\Delta E_{ST} > 0$. A good example of diradicaloids is the polyacene series (anthracene, tetracene, pentacene, etc. see Figure 42).

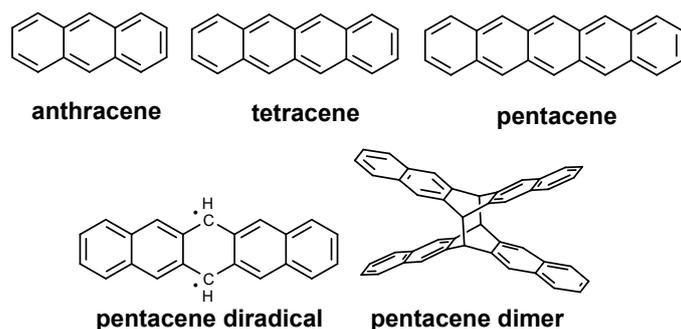


Figure 42: *Kekulé structure for acenes.*

As the number of linearly fused rings increases ΔE_{ST} approaches zero but does not become negative and therefore becomes an open-shell singlet ground state for infinite polyacene [478]. This leads to significant reactivity with >5 rings spontaneously dimerising in solvent at room temperature [27]. This dimerisation is a [4+4] cycloaddition reaction, which is symmetry forbidden but can be achieved through photoexcitation at room temperature or thermal excitation in a flame.

Polyacenes require considerable length of some five rings to attain significant binding energies up to 39 kcal/mol [269, 545], which is nearing a value of significance for soot formation. Given the growth mechanisms found for PAH it is highly unlikely that a concentration of linear acenes with >5 rings will be present as evidenced by the species observed in the HR-AFM [88]. However, a hydrogenated pentacene was directly observed in HR-AFM imaging [88] (PS8 see Figure 43). This is interesting for two reasons. Firstly, it shows that protonation can change the character of a reactive PAH with further protonation potentially leading to a non-reactive closed shell species. Secondly, this protonated diradicaloid takes on a doublet radical electronic state with considerable reactivity. Recent experiments have shown that hydrogenated pentacene can form dimers in the solid state [199] (we calculate a bond energy of -50.1 kcal/mol at the M06-2X/cc-pVTZ//B3LYP/6-311G(d,p) level of theory). These dimers were also found to dehydrogenate to large 14 ring peripentacene species [199].

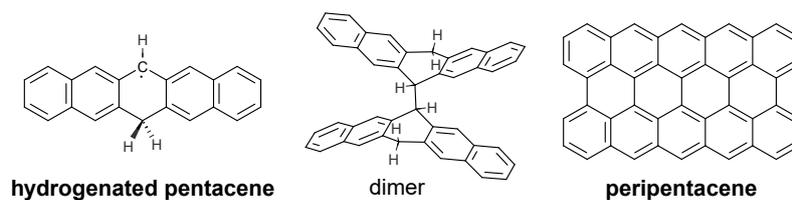


Figure 43: *Kekulé structure for acenes.*

Non-acene species have also been considered. Koley et al. [269] considered adding circular pericondensed PAHs to the end of the acene to combine stacked dispersion interactions and acene cycloaddition. However, this type of structure is highly unlikely to form in the flame from a HACA type mechanism and has not been observed in HR-AFM studies [88]. Finally, larger non-acene PAH in roughly rectangular geometry, such as peripentacene, were computed to dimerise along their opposite zig-zag edges [545] [see Figure 18(hh)].

But as with the polyacenes, zig-zag edges of at least 5 rings were required to attain binding energies of 41 kcal/mol. If we consider that in HR-AFM such symmetric species are not widely found and rarely are more than three adjacent zig-zag edges found (with a maximum of four zig-zag edges in a row observed) [88], it is unlikely that this mechanism can explain the clustering of species of mass near 500 Da. However, diradicals are attractive as soot precursors as they can theoretically polymerise and we will return to them.

4.6.7 Rim-linked (ARLH)

Rim-bonds arise from localised π -radicals that allow bonded and stacked configurations with considerable binding energy [see Table 1(ii) Figure 18]. Localised electronic states were discussed in the previous section with regard to diradicaloids in even-numbered aromatic systems.

In odd-numbered π -electron aromatic systems localisation can also occur through the presence of non-hexagonal rings, *e.g.* fluorenyl and indenyl, or methylene groups. Figure 44 shows the π -radicals based on localised edge types as compared with phenalenyl-type edges that are delocalised as the network enlarges. Spin density has been found to linearly correlate with the reactivity of a site, both for dimerisation and ability to abstract [478]. It is important to reiterate that by localised we do not mean that the π -radical is solely localised to a single carbon site, as with the σ -radical formed from hydrogen abstraction from a PAH, but that the π -radical is pinned to the edge. For example, while the indenyl-type radical is strictly a resonantly stabilised radical, with the spin density being shared between two equivalent positions, it is still a localised electronic state. This is shown in Figure 44 as the aromatic network is enlarged, minimal changes to the spin density of the most spin rich carbon atoms are seen. The first three localised π -radicals can be classed as arising from hydrogen abstractions from fluorene, indene and a methyl group and are well known reactive species in the flame.

Partial saturation of aromatic edges from hydrogen addition is the second class of localised π -radicals. The earliest discussion of this in the soot literature that we could find was by Abrahamson in 1977 [1], in which saturated platelets were suggested to form soot. These partially saturated edges and aromatic interiors were suggested to form reactive localised π -radicals. The issue with these suggestions and the reason saturation was not generally considered is that at high temperatures, hydrogen is readily lost from partially saturated PCAH (part sat. PCAH-type) with strong aromatic stabilisation [213]. Aromatic stabliomers are predicted to be fully unsaturated from thermodynamic calculations [475].

The recent experimental work from Commodo et al. [88], challenged the lack of saturation by showing that particular ring topologies allow partially and fully saturated aromatic edges. In the previous section, we mentioned partially protonated pentacene had been found in the flame [88] and allowed for strong dimerisation energies. Figure 44 shows minimal delocalisation of the spin density for this partially saturated diradicaloid-type localised π -radical (Part. sat. diradicaloid-type). The other edge type imaged was a partially saturated rim-based pentagonal ring (part. sat. rim. pent.-type) (see Figure 1 species IS1). This π -radical is similar in topology to the benzyl-type π -radical, but is perhaps more likely to form as many more rim-based pentagonal rings were found compared with methyl groups [88]. The importance of these radicals in the HACA mechanism [157]

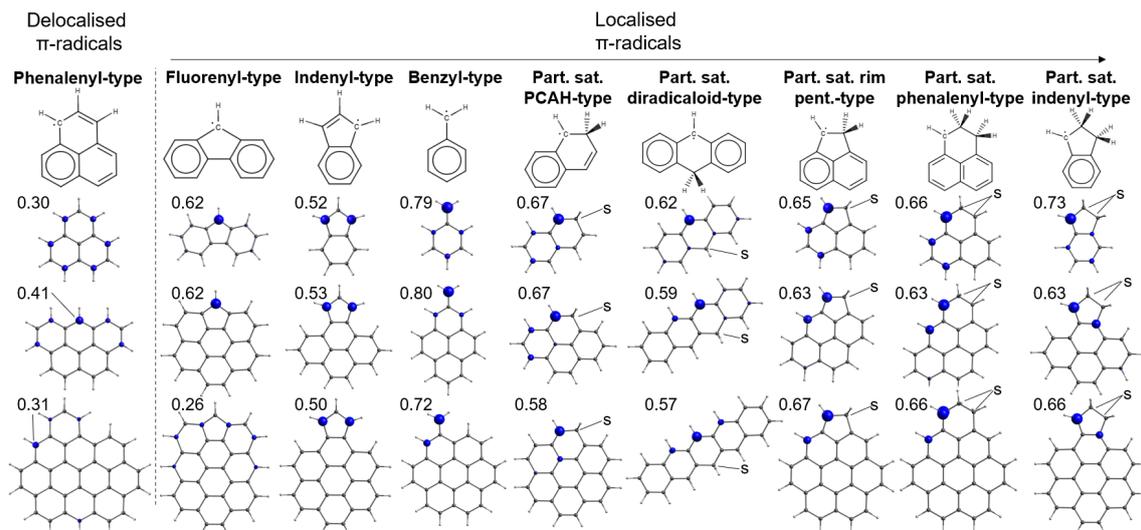


Figure 44: Different classes of π -radicals with spin density isosurfaces=0.025 computed with the B3LYP/6-311G(d,p) level of theory as a function of size. The Mulliken spin density value is shown for the most spin rich carbon site. Carbon atoms marked with s are saturated.

and shuttling rim-based pentagons along zig-zag edges was first appreciated in calculations performed by Frenklach and coworkers [156, 528]. Wang and coworkers found that this site reacted with the σ -radical phenyl to form a stable species unable to break open across the pentagonal ring (this is opposed to hexaphenylethane, which readily breaks to form free radicals [97]). Further to this, Frenklach and Mebel recently confirmed that this site is also unlikely to fragment at flame temperatures showing remarkable stability against radical-induced fragmentation [152].

Of most interest for soot formation are polyaromatic mechanisms that involve these reactive sites. A recent computational study systematically computed the energetics of polyaromatic crosslinks with localised π -electrons (see Figure 49) [325]. Significant bond energies were found with σ -radicals, but interestingly strong bonds were also formed between localised π -radicals [325]. These results are unsurprising considering that smaller localised π -radicals are known to recombine and form large aromatics *e.g.* benzyl forms phenanthrene [461], indenyl forms chrysene [230], while benzyl and indenyl can form pyrene [462], as mentioned. Further experimental evidence comes from the molecules that readily soot and could be seen as precursors for these localised π -radicals through hydrogen addition or abstraction, such as toluene, fluorene, indene, cyclopentadiene and acenaphthalene [103]. Another example is the significantly enhanced sooting of 1,2,4-trimethylbenzene compared with the structural isomer n-propylbenzene [74] (see Figure ??).

While these small species appear to crosslink and cyclodehydrogenate, larger localised π -radicals could form dispersion-stabilised stacks. One of the first suggestions of dispersion-stabilised stacked and bonded localised π -radicals was perhaps from Tonachini *et al.* in 2015 [318], where a partially saturated rim-based pentagonal ring crosslinks with a PAH through a reaction with oxygen (see Figure 18(ee)). It was found that significant bonding

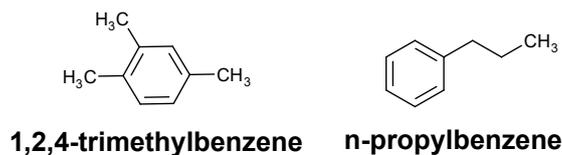


Figure 45: Kekulé structure for 1,2,4-trimethylbenzene

could occur in stacked aromatics between localised π -radicals without any oxygen (see Figure 46). A full thermodynamic equilibrium analysis of the dimer further confirmed the stability of such structures in flames (1500–2000 K) and a significant physical enhancement for larger species [344]. We decided to name these structures rim-bonded to

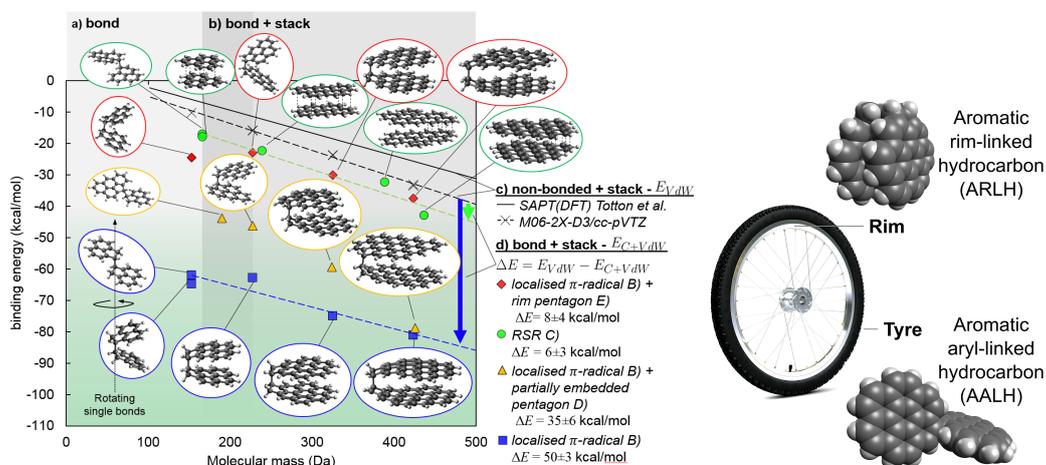


Figure 46: Bonded and stacked binding energies [325]. The blue arrow shows the enhancement due to localised π -radical bonds compared with only dispersion interactions.

distinguish them from aryl-bonded. Figure 46 shows the tyre analogy where rim-linked hydrocarbons could be thought to link via the rim of a bicycle wheel, which is only accessible on the face of the molecule. The aryl-linked structure can be thought of linking via the tyre so that the bond is colinear with the aromatic planes. This naming was chosen to also distinguish them from delocalised π -radicals that can form σ -dimers when not stacked but form weak multicentre pancake bonds when stacked.

It is still unclear how prevalent such sites are within the flame. In early soot formed from pyrolysis, significant spin concentrations were found ($\approx 10^{21}$ spins/gram) using electron paramagnetic resonance (EPR) [534]. Wang put this number into context in his review stating that [511]:

“Assuming the residue is made of carbon only, the number of spins is roughly 1/50 atoms, or one free radical for each pair of PAHs of the size of coronene.”

. This has recently been explored in EPR experiments on soot collection at different locations in the flame [506]. A change in radical character occurring at soot inception suggested the involvement of π -radicals. An initial attempt was made to answer

this question using a computational approach by considering localised π -radicals forming from hydrogen addition and abstraction from a rim-based pentagonal ring on acenaphthylene (*i.e.* in partial equilibrium with H/H₂ in the flame). This was a similar approach to that employed by Howard in 1991 to consider the formation of σ -radicals from hydrogen abstraction [213]. It was found that, for temperatures in the flame where soot begins to form (1400–1500 K), 0.1 to 0.01 fraction of rim-based pentagonal rings were localised π -radicals. This is consistent with the ratio of unsaturated, fully saturated and partially saturated rim-based pentagonal rings found in HR-AFM of 27:12:4 [88]. This is a considerable fraction and under certain circumstances is greater than the mole fraction of σ -radicals on rim-based pentagonal rings. At higher temperatures (1800–2000 K) the unsaturated rim-based pentagonal ring is favoured. Perhaps most interestingly for a soot mechanism it was shown that multiple localised π -radicals can exist on a single aromatic molecule. Taking the example of 1,3-diaecorononyl (see Figure ??), we calculated the triplet to be considerably more stable than the singlet making it a true diradical as discussed in Figure 41 (B3LYP/6-311G(d,p) $\Delta E_{ST} = 17.7$ kcal/mol). As noted by Abrahamson [1] in 1977, such multiradicals could allow for a chemical polymerisation of aromatics.

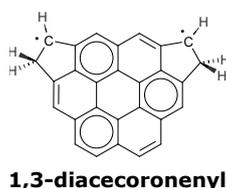


Figure 47: *Kekulé structure for 1,3-diaecorononyl.*

There is also some preliminary evidence from mass spectrometry that protonated aromatics, which are more likely to be localised π -radicals, cluster. The clustering species from Grotheer et al. have a H/C of 0.4, while the species at 500 Da have a H/C of 0.3 [190]. There was also a preference for an even number of hydrogen atoms in the clustered species that could indicate reaction between species with an odd number of hydrogen, which are more likely to be localised π -radicals. Recently, Carbone presented a positive mass spectrum, which is more likely to be protonated species [65] (while cPAH are found in the negative mass spectrum as mentioned [208]). Figure 48 shows how the positive species cluster, while the negative mass species did not. As with the earlier work a H/C ratio close to 0.5 indicates reactive species with an excess of hydrogen. However, no definitive experimental evidence has been found to date and significant work is required to justify such an interpretation of these results. This mechanism could also be driven by unsaturated species such as indenyl-type edges that have low H/C ratio, so a high H/C ratio is only a secondary indicator. This preliminary exploration reveals that understanding how hydrogen is gained and lost by the edge as well as ring topology will be critical for understanding the importance of this pathway.

In summary, mechanisms involving both physical and chemical processes were reviewed. These processes present a means to increase the collision efficiency of polyaromatic inception routes. The zipper mechanism, where crosslinked pericondensed PAH stack and dehydrogenate, is not considered to be possible. Internal rotors that enhance polyaromatic inception present an interesting suggestion that requires further calculations. Bridges

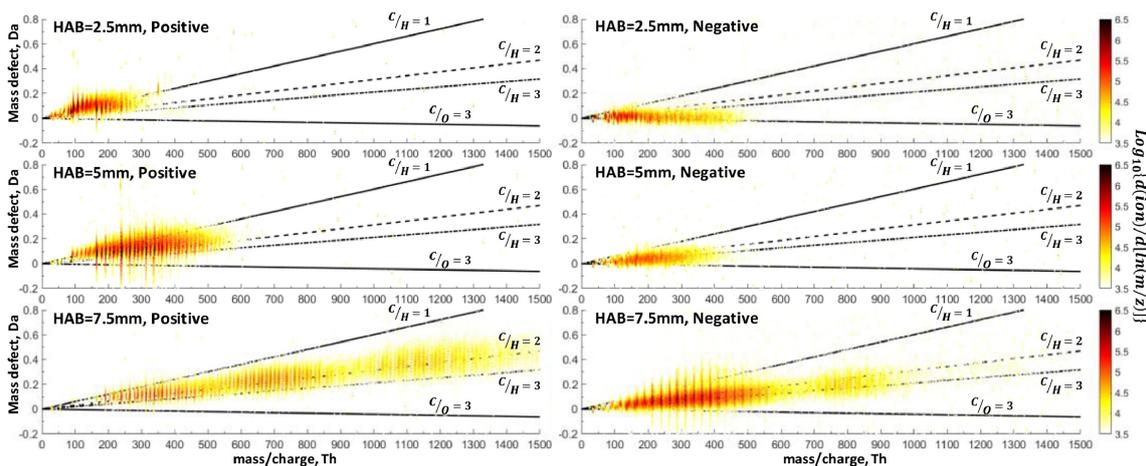


Figure 48: Mass defect vs mass to charge ratio of flame ions (positive left, negative right) sampled in an ethylene/air flame from a McKenna burner [65]. Used with permission from Elsevier ©.

formed between aromatic units have long been explored – their downsides include them being prone to radical-induced fragmentation and requiring a higher H/C ratio than what is seen. There is an interesting overlap here with rim-bonding, where two benzyl type radicals will form a $-\text{CH}_2\text{CH}_2-$ bridge. Excimers were shown to be in low concentration and unimportant for driving nanoparticle formation, however, excimers were still shown for bridge species. Multicentre-bonds were described between delocalised π -radicals due to phenanenyl-type hexagonal networks. Low binding energies were found suggesting minimal enhancement. Localisation of π -radicals was found to occur for zig-zag edges with diradicaloid character leading to [4+4] cycloaddition. Localisation was also found for odd-numbered carbon networks with strong rim-bonding for these species with the topology of the aromatic network and the saturation of the edge to be critical for understanding this pathways to nanoparticle formation. These localised electronic states allow for true diradicals to form, suggesting a polymerisation reaction may be possible with multiradical reactive PAH. Finally, preliminary evidence for protonation being important for soot formation was also shown.

5 Summary and outlook

5.1 Mechanism comparison

Physical nucleation of PAH is only possible for large PAH (667 Da) with significantly higher molecular mass than the species seen to cluster in mass spectrometry studies [65, 190]. Previous work [489] reveals that physical nucleation of pericondensed aromatics, such as pyrene, is unable to explain the formation of soot. We therefore conclude that the model of irreversible dimerisation of pyrene can describe aspects of soot formation, yet not because pyrene is actually dimerising – it points to another mechanism with similar concentrations of the critical species and similarly high collision efficiencies. Therefore,

we see this model as acting as a surrogate for the real soot formation model.

We can now systemically consider chemical mechanisms. Figure 49 shows the bond energies between the various reactive edge types that have been detailed in this review (full details can be found in [325] and [344]). The bond energies are used to consider the thermal stability of the first crosslink critical for each chemical mechanism. It has already been established that bond energies above -40 kcal/mol are found to be readily broken in flames (such as β -scission [414] and PAH dimerisation [511]). Thermal fragmentation is described by the energy barrier between the bound and the transition states. However, we found the Bell-Evans-Polanyi relationship is still observed (the barrier was linearly proportional to the bond energy, for the weakly bound species) and that for many structures the reaction was barrierless or small [344]. Therefore, the bond energy threshold of -40 kcal/mol is considered an appropriate proxy for stability of bonds within a flame.

	aryl σ -radical		localised π -radical		delocal. π -radical	diradicaloid		rim-based pentagon	cPAH	low aromaticity			Classes
	A1)	A2)	B1)	B2)	C)	D1)	D2)	E)	F1)	F2)	F3)	Structures	
aromatic aryl-linked hydrocarbons (AALH)	-130.4	-125.3	-97.3	-91.0	-73.6	-63.7	-78.2	-53.5	-41.3	-38.3	-36.2	A1)	
		-120.8	-92.6	-86.8	-69.0	-57.6	-73.3	-49.8	-38.4	-33.7	-33.8	A2)	
aromatic rim-linked hydrocarbons (ARLH)			-61.9	-34.0	-39.9	-32.2	-43.8	-24.5				B1)	
				-50.9	-33.4	-28.6	-14.8					B2)	
aromatic multicentre-linked hydroc. (AMLH)					-17.0	-12.1	-23.6					C)	
aromatic zigzag-linked hydrocarbons (AZLH)						-29.6						D1)	
							-16.5					D2)	

bond energy (kcal/mol)
-190 -40

Figure 49: Bond energy between various small aromatic molecules [325].

The grid suggests a naming strategy based on the reactive species; A) σ -radicals, B) localised π -radicals, C) delocalised π -radicals and D) diradicaloids:

- Aromatic aryl-linked hydrocarbons (AALH), involving aryl-type σ -radicals A), of which the clustering of hydrocarbons radical chain reactions (CHRCR) mechanism [234] is a subset with aryl-radicals A) attacking delocalised π -radicals C). What are usually called aliphatic/aromatic linked hydrocarbons [100] are also represented by A)+E) and A)+F2) reactions. Strong, thermally stable bonds are formed.
- Aromatic rim-linked hydrocarbons (ARLH), involving localised π -radicals B). Strong bonds are only formed with other localised π -radicals, however, as the aromatic network enlarges dispersion interactions could allow for a physical+chemical mechanism. Multiradicals could also form that would allow for a chain reaction to proceed.

- Aromatic multicentre-linked hydrocarbon (AMLH), involving delocalised π -radicals PAH C). These react with themselves through pancake bonds but are also able to form non-stacked σ -dimers, which are shown in this table.
- Aromatic zig-zag-linked hydrocarbons (AZLH), involving diradicaloids D). These react through cyclisations but can also polymerise weakly.

The forward rate constant was also computed for the small aromatics [344]. The maximum rate was $10^{12} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$ for aryl-radical recombination. Previous work from Frenklach and Mebel showed that even with a forward rate of this order there is still insufficient nucleation flux for nanoparticle formation [152]. This leaves us with the uncomfortable conclusion that no chemical mechanism involving these small aromatics can explain soot nucleation.

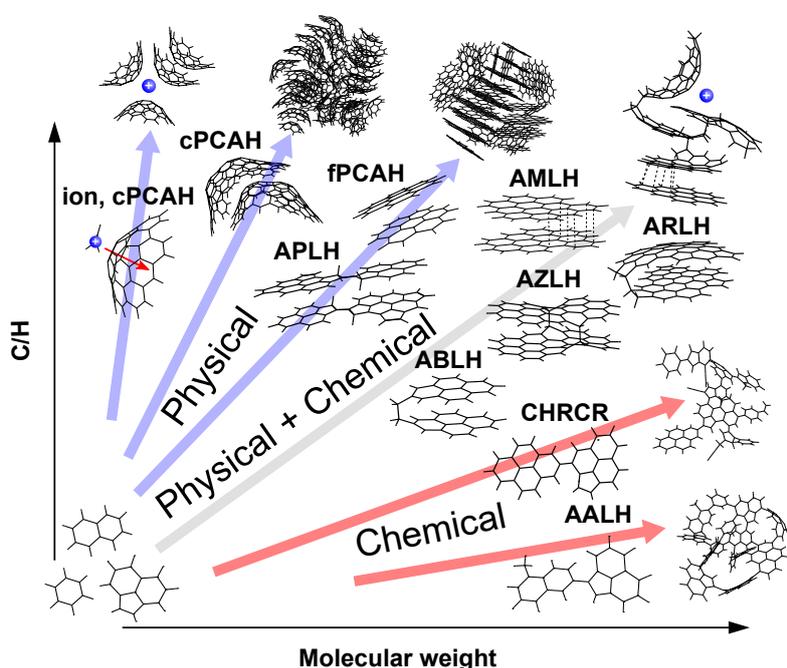


Figure 50: Schematic of various soot nanoparticles arranged as a function of their C/H ratio and molecular weight.

In Section 4.6 a “middle way” was presented between physical and chemical mechanisms. This can be schematically shown based on the C/H versus molecular weight diagram introduced by Violi in 2007 [39] (see Figure 50). It is important to consider that these mechanisms might not be independent. To illustrate this, a structure with multiple types of bonding is shown in the top right of the figure, with a curved species and ion included to indicate that electrical condensation could also enhance the inception of reactive species.

5.2 Outlook

These final comments will concentrate on fundamental gaps in experimental and modelling approaches as well as more practical steps that can be taken to reduce the emission

of these species from combustion.

5.2.1 Experimental outlook

To guide the discussion around fundamental gaps in current knowledge we have plotted some representative data for experimentally observed species in a H/C vs molecular mass graph that was initially plotted by Wagner, Jander and Homann in 1990 [226] (see Figure 51).

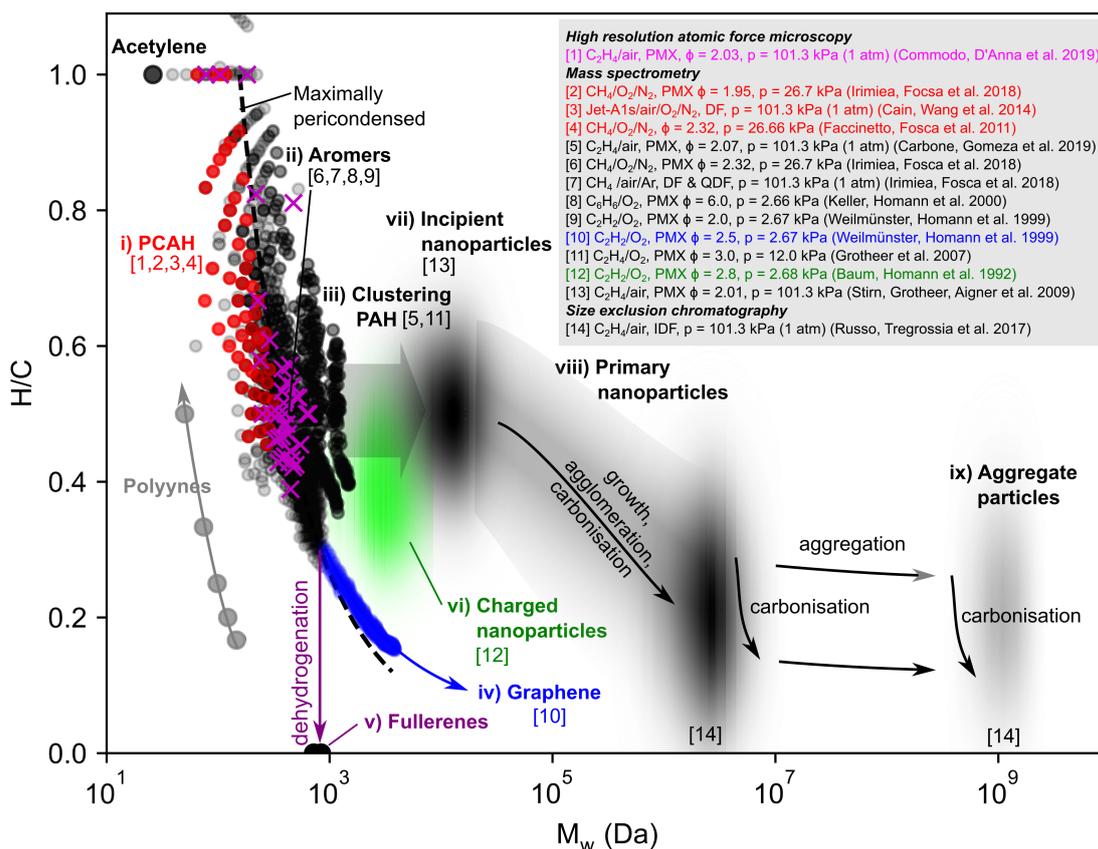


Figure 51: The variety of transformation of hydrocarbons towards soot formation. The inset shows the various data sources [25, 58, 65, 88, 134, 181, 189, 220, 243, 425, 521].

The molecular masses of the different species are determined directly from either HR-AFM [88, 444], mass spectrometry data [25, 58, 65, 134, 181, 189, 190, 220, 221, 243, 521] or size exclusion chromatography [425] from hydrocarbon flames. In modern high resolution mass spectrometers, the H/C ratio can be determined directly assuming only carbon and hydrogen are present. The H/C ratio of the other nanoparticles, primary particles and aggregate particles are determined from elemental analysis with the ranges chosen to cover the observed values. Arrows show the pathways from precursors to particles for which experimental data or a correlation exists, unless otherwise mentioned below. It

is helpful to make use of molecular mass data from mass spectrometry instead of mobility diameter in order to directly compare molecular growth and nanoparticle formation. However, for the primary and aggregate soot modes this requires using size exclusion chromatography results that have greater uncertainty.

Looking at Figure 51, the first and most evident trend is a decrease in hydrogen content of the carbonaceous species as the mass increases. This follows from the entropically driven nature of soot formation due to H₂ evolution [511]. The initial formation of polyynes from acetylene is well understood [186] and growth does not extend much beyond 10 carbon atoms due to radical induced fragmentation and cyclisation into pericondensed aromatic hydrocarbons (PCAH). **i) PCAH** primarily form via the HACA growth mechanism and recombination reactions [187]. More work is needed to understand the variety of isomers of PCAH. The generally accepted view that HACA growth proceeds through only 6-membered rings has recently been challenged computationally [255] and experimentally [88, 231, 234], with the presence of pentagonal rings being more prevalent than previously thought. These new insights require more detailed understanding of methyl additions [188, 531], ring enlargements [549], aromaticity [303], curvature [409] and fragmentation routes. Finally, synchrotron methods such as double imaging Photoelectron Photoion Coincidence Spectroscopy method (i²PEPICO) promise better isomer discernment for larger PAH with pentagonal rings [347] as well as resolution improvements in PI-MS experiments.

A second large distribution of species with mass near 500 Da has also been detected in many different flame environments [11, 112, 134, 189, 221, 224, 243, 243, 428, 547] – called “**ii) aromers**” by Homann [208]. It is not entirely clear how these form but suggestions include crosslinking of σ -radicals [208] or localised π -radical recombinations that then cyclodehydrogenate to form nearly pericondensed structures. Evidence for such a crosslinking reaction recently was shown from hierarchical clustering analysis of SIMS-TOF MS providing strong evidence that the aromers arise from crosslinking of small aromatics with 4–8 hydrogen atoms lost during subsequent cyclisation [135]. Curvature integration is also not fully understood. The curvature integration seen experimentally [323] cannot be explained through HACA growth alone [152, 292] and therefore pathways such as crosslinking that allow for embedded pentagonal rings are required [420, 492].

In low-pressure flames certain pathways that do not lead to soot have been explored. HACA growth can be continued in low pressure acetylene flames to form large **iv) graphene** structures [521]. **v) Fullerenes** can form in benzene/oxygen flames [164]. The fullerenes are suggested to form due to multiple crosslinks of small aromatics, producing aromers large enough to be significantly curved to become fullerenes during dehydrogenation. It is still unclear how aromatics close to form fullerenes. Computational work suggests that hydrogen must be mostly lost from the aromatics before they can curl and close to form carbon cages [429]. Experimental work recently showed the formation of hydrogenated fullerene C₆₆H₄ with heptagonal rings in hydrocarbon flames [484], suggesting closure before complete dehydrogenation. It is still unclear whether subsequent dehydrogenation and C₂ loss could explain the formation of the symmetric fullerene C₆₀ – as has been proposed for plasmas in the “shrinking hot giant model” [321, 422]. The synthesis of aerosolised graphene is also of industrial significance. It is still unclear how low pressure acetylene/oxygen flames [521] and microwave reactors [105] are able to produce planar

graphene and avoid fullerene or soot formation.

vi) Charged nanoparticles are formed in acetylene flames (but not significantly in benzene flames). One possible explanation for this observation is an ion, cPAH electrical condensation mechanism. This could explain the correlation Homann found with the larger aromer species and these nanoparticles [210] and why their mass is low – ion-dipole interaction can only stabilise a few cPAH. However, this is simply conjecture and detailed fragmentation studies using mass spectrometry are required to understand the nanoparticles’ constituents. More work is also needed to understand how electrical condensation involving cPAH can influence chemical mechanisms as briefly shown in Figure 50, but it appears that it is not the critical route for nanoparticle formation in atmospheric flames [514].

iii) Clustering PAH have only been observed with a periodicity of ~ 500 Da [65, 190] suggesting that these larger aromers are the reactive structures that lead to soot formation. From HR-AFM it appears that reactive edges are in partial equilibrium with hydrogen radicals and hydrogen gas [88, 325] leading to a significant fraction of localised π -radicals and σ -radicals. More work is needed to understand which sites are in high enough concentrations to rapidly form the <4 nm **vii) incipient nanoparticles** in the flame [31].

Further processes lead to larger > 4 nm **viii) primary nanoparticles**. The primary nanoparticle mode is found to increase in mass until it becomes the primary soot particle mode seen in aggregates around 10–20 nm in size [88]. We will not discuss the further processes involved in formation of aggregate soot particles as this is not the focus of this review, but will mention again that the liquid-like halos are thought to be due to sampling artifacts (see Figure 29). It is clear that much is still to be understood about nanoparticle formation requiring further experimental studies to fill in the gaps.

5.2.2 Modelling outlook

Modelling also requires significant developments going forward in order to better understand and describe soot formation. Reproducibility in modelling combustion kinetics has always been a strength within combustion science [177]. Starting with CHEMKIN—A Chemical Kinetics Software Package, developed by Sandia National Laboratories in the 1960s, standardisation of the kinetic and thermodynamic data format allowed for the widespread use of such software packages for modelling combustion. This was further facilitated by the software being open and made available on the world wide web (an informative historical description can be found by Council [91] and we have also recently reviewed the various databases available online at present [342]). These approaches have allowed experimental and increasingly powerful computational approaches to provide insights into soot formation. A recent example of the power of these techniques is the paper from Frenklach and Mebel on comparing various reactive aromatics in forming soot [152]. However, these approaches are limited by the size of the mechanisms that can be developed by hand [308]. Automation, therefore, has developed naturally as kinetic mechanisms for realistic fuels begin to contain thousands of reactions and thus require software to construct. One such example is the Reaction Mechanism Generator (RMG) [158, 176] that employs rules based on species fragmentation patterns to predict reaction pathways and thermodynamics to develop mechanisms. RMG also performs au-

tomated electronic structure calculations for specific classes of reactions [32] (another example being EStokTP: Electronic Structure to Temperature- and Pressure-Dependent Rate Constants [66]). The use of freely available software has always allowed for robust collaboration in soot modelling, starting with Frenklach's MoMIC soot library for CHEMKIN [418]. With new open data initiatives it is an imperative that software and data are made available with publications to continue the reproducibility for which this community has become known. For example, recent efforts from the Internal Sooting Flame (ISF) Workshop to standardise experimental flame configurations allowed simpler collaboration and comparisons with models.

Another challenge of modelling soot is the multiscale nature of the problem. Different scales often require different numerical approaches and this has made comparison between models challenging to date. For example, as PAH grow it becomes unfeasible to describe every possible reaction path in a kinetic mechanism; this has been tackled by switching to stochastic approaches such as kinetic Monte Carlo (KMC) simulation of aromatic growth (e.g. the KMC-ARS in MOpS [410] – <https://github.com/ucamceb-como/MOpS/>, SNAPS [286] from Violi *et al.* and implementations from Frenklach *et al.* [526, 528]). In terms of KMC this requires all of the jump processes and their associated rates to be explicitly stated and the approximations used to couple kinetic mechanisms and KMC to be disclosed in publications. Reproduction of PAH isomers that are now experimentally attainable from HR-AFM and PI-MS needs to be demonstrated with such codes. Various scales also require model reduction to allow for kinetic mechanisms to be applied to larger scale simulations, such as computational fluid dynamics (CFD) simulations. This is known as surrogate model creation, where the goal is to create a smaller kinetic mechanism that captures the main features of the combustion phenomena with a simpler model than the full mechanism or model [365, 400]. A variety of approaches for model reduction are available including support vector machines, polynomial response surface models, interpolations, radial basis functions, splines and artificial neural networks, to name a few. The importance of finding the optimal approximation for reducing a particular problem was recently highlighted [160]. Experimental approaches to model reduction are also attractive. The Hybrid Chemistry (HyChem) approach to fuel pyrolysis allows experimentally derived fragmentation patterns to be coupled to small hydrocarbon mechanisms providing a significant reduction in mechanism size [516].

This sort of multiscale modelling of soot formation, however, has led to highly customised software developed independently by various groups (see Figure 52 for our approach). This is due to challenges associated with linking of various data structures and numerical approaches. One of the early projects that sought to solve this problem was the Collaboratory for Multi-scale Chemical Science (CMCS) project started in 2001 [381] and led by members of the combustion community in the USA. This project used the recently developed semantic web tools (developed in computer science to extend the internet into a machine readable and writable platform) to link and connect models and data for combustion applications. The approach was memorably presented by Frenklach at the 2006 International Symposium on Combustion with his PrIME database [150, 541]. While the entire framework developed in the CMCS project did not ultimately become widely used [441] the project led to critical infrastructure for modelling soot including the Active Thermochemical Tables (ATcT), the Basis Set Exchange (BSE), Group Additivity Thermodynamic Properties (GATP – now used in RMG to good effect) and the highly

successful GRI-Mech kinetic mechanism [471].

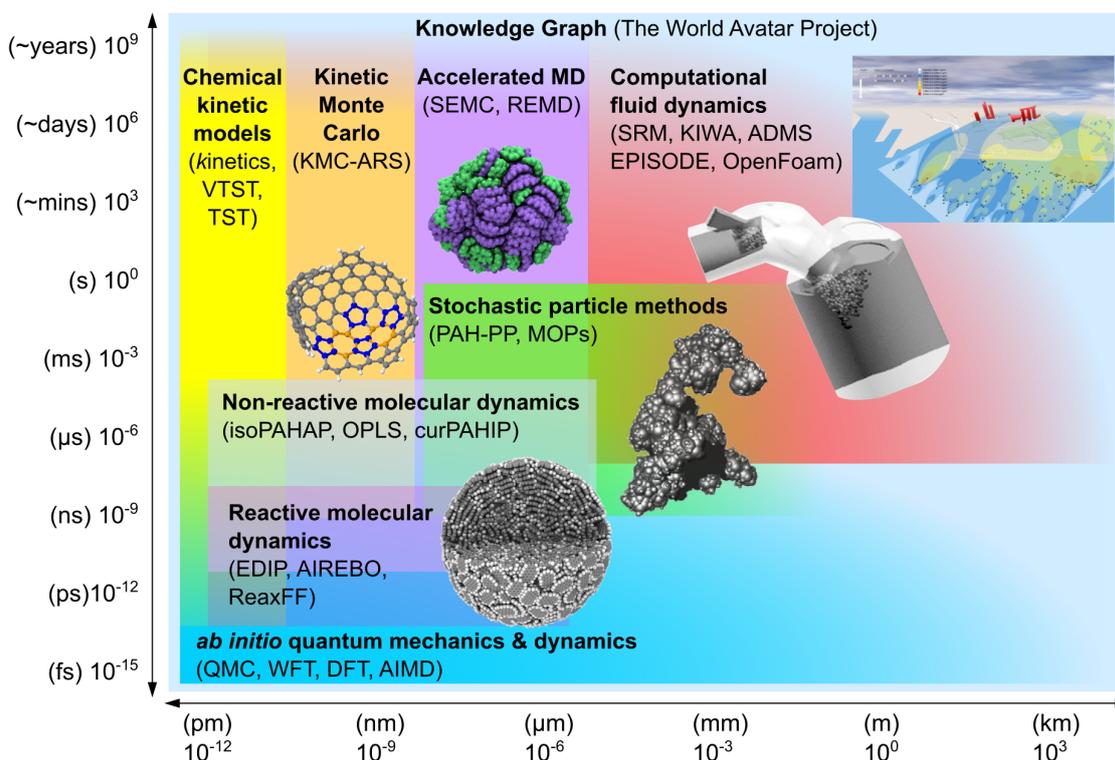


Figure 52: Linking spatial and temporal scales for modelling nanoparticle formation and pollution dispersion.

Since these initial efforts to build a web-based infrastructure for combustion science, considerable advances have been made in semantic web technologies, with current focus being on Knowledge Graph technologies. This recently led us to develop new and extended Knowledge Graph Ontologies for both the microscale; OntoKin [139] (for representing chemical kinetic reaction mechanisms including thermodynamics), OntoCompChem [272] (representing electronic structure calculations), OntoSpecies (representing molecular species), and for the macroscale; OntoCAPE [370] (representing chemical engineering plants and extended to decentralised eco-industrial parks in OntoEIP [551]), Weather Ontology [385] (representing wind, rain, temperature and humidity), OntoPowSys [113] (representing power systems) and OntoCityGML [128] (an extension of CityGML representing buildings and infrastructure [267]). While these approaches are in their infancy, they open up the possibility of rigorously and consistently linking models and data across spatial and temporal scales as demonstrated in Figure 52 as well as comparison between models and data [129]. One example was the recent virtual sensor for atmospheric pollutants emitted from ships that linked models and data from microscale kinetic mechanisms to models of engine performance and pollutant emissions, through to the atmospheric dispersion of these pollutants across Singapore [140]. Automation is captured by the OntoAgent ontology [552] which enables expansion and improvement of agents operating on the knowledge graph. We envisage that such a systematic approach will be critical for providing the infrastructure to develop the multiscale descriptions of combus-

tion to elucidate the formation of carbonaceous nanoparticles in flames.

5.2.3 Practical steps

The more practical aspects of reducing nanoparticle emissions from combustion devices require that these emissions are eliminated in flames or removed in aftertreatment systems. While we have shown experimental studies that are able to detect various nanoparticle modes, routine measurements of these smallest nanoparticle emissions from combustion devices are still not possible. As measurements improve, empirical models will be able to establish operating conditions to reduce nanoparticle emissions. However, fundamental understanding could provide more direct means to limit emission of these smallest combustion products. We will highlight one recent example of fuel mix design where the yield sooting index was used to provide a diesel fuel with reasonable cetane number but significantly lower sooting propensity [247]. These approaches could also be extended with particle size measurements for reducing nanoparticle emissions from engines. This is particularly important as new lean engine combustion systems are developed to eliminate soot mass but not necessarily soot nanoparticles. Similar insights into the effects of cool combustion, charge and ozone injection [235, 236], hydrogen and ammonia addition [29, 225] and biofuels [142, 432] on nanoparticle emissions are also required. Another approach is to consider aftertreatment systems. As mentioned in Section 2.2, many of the smallest nanoparticles are not filtered by aftertreatment systems [463] due to their low coagulation efficiencies [212]. Recent efforts to remove these nanoparticles with activated carbon or fibre filters need to be more extensively explored [253]. It is also unclear how nanoparticle filtration will improve as the soot cake develops [288].

Ultimately, the emission of carbonaceous nanoparticles needs to be a research and industrial priority for the future of combustion devices. We end this review with the comment from Miller, Pilling and Troe’s 2005 review [355]:

“Hopefully, whoever writes this review in 2054 will report that there is then a complete, quantitative understanding of the mechanism of soot formation in combustion.”

Recent modelling and experimental advances suggest such enlightenment might occur sooner than 2054.

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