

# An adsorption-precipitation model for the formation of injector external deposits in internal combustion engines

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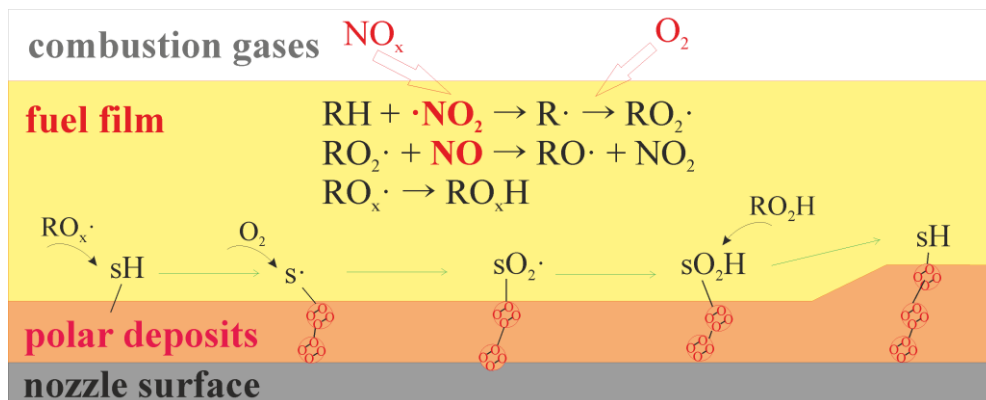
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## Abstract

The occurrence of deposits on fuel injectors used in gasoline direct injection engines can lead to fuel preparation and combustion events which lie outside of intended engine design envelope. The fundamental mechanism for deposit formation is not well understood. The present work describes the development of a computational model and its application to a direct injection gasoline engine to describe the formation of injector deposits and their effect on engine operation. The formation of fuel-derived deposits at the injector tip and inside the nozzle channel is investigated. After the end of an injection event, a fuel drop may leak out of the nozzle and wet the injector tip. The model postulates that the combination of high temperature and  $\text{NO}_x$  produced by the combustion leads to the initiation of a reaction between the leaked fuel and the oxygen dissolved in it. Subsequently, the oxidation products attach at the injector wall as a polar proto-deposit phase. The rate of deposit formation is predicted for two limiting mechanisms, adsorption and precipitation. The effects of the thermal conditions within the engine and of the fuel composition are investigated. Branched alkanes show worse deposit formation tendency than n-alkanes. The model was also used to predict the impact of injector nozzle deposit thickness on the rate of fuel delivery and on the surface temperature of the injector wall.



## Highlights

- Injector leakage causes accumulation of fuel near the nozzle post-injection.
- The leaked fuel degrades under the action of  $\text{NO}_x$  and  $\text{O}_2$  in the quench layer.
- Radical chain oxidation mechanism involving branching reaction with  $\text{NO}$  is proposed.
- The pressure drop during the power stroke causes the leaked droplet to boil.
- The boiling triggers receding of the droplet toward the nozzle and precipitation.

# Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Mechanisms of deposit formation</b>	<b>5</b>
2.1	Conditions in the fuel film and the quench layer	6
2.1.1	Engine model	6
2.1.2	Leakage of fuel and temperature of the fuel film	7
2.1.3	Modelling the quench layer	9
2.2	Degradation of the fuel film	11
2.2.1	Gas transfer	13
2.2.2	Evolution of the film composition during a cycle	14
2.3	Rate of deposit formation	16
2.3.1	Re-suspension-filtration-precipitation mechanism	17
2.3.2	Surface oxidation-adsorption mechanism	18
2.3.3	Experimental determination of the rates of deposit formation and removal	22
<b>3</b>	<b>Effect of the deposit on the engine performance</b>	<b>23</b>
3.1	Nozzle channel deposits and channel plugging	23
3.2	Injector tip deposits and wall temperature	24
<b>4</b>	<b>Discussion</b>	<b>27</b>
	<b>References</b>	<b>30</b>
S1.	Engine parameters and cylinder conditions	34
S2.	Rate parameters of the liquid phase oxidation	37
S3.	Gas transfer to the liquid film	40
S4.	Nozzle channel deposits: relationship between flow reduction and deposit thickness, and processing of the experimental data	41
S5.	The multilayer heat transfer problem	43
S6.	List of symbols and abbreviations	45

# 1 Introduction

Modern engines use injectors that must insert a fuel jet of extreme velocity in the hot cylinder with good precision in terms of amount of fuel, timing and spray shape. The accurate timing of the injection depends on the efficient sealing of the fuel pathway, realized by the injector needle sitting onto the entrance of the nozzle channel. This seal is never perfect, and under the action of the high injection pressure ( $\Delta p \sim 100$  MPa; cf. the S6 supplement for a list of symbols), fuel droplets leak out of the nozzle after the end of the injection, wetting the nozzle channel and tip [1,2]. The droplets remain exposed to heat and combustion gases for certain period, and before evaporating completely, degrade. The degradation products remain at the injector wall, eventually developing into carbonaceous deposits.

Injector deposits existed since the invention of the injector, but they became a significant problem only with the recent advances in the injector technology, both in diesel [3,4] and gasoline [5-7] engines. The combined requirements for high precision and small nozzle radii ( $R_n \sim 50$   $\mu\text{m}$ ) mean that even a very thin *nozzle channel deposit* layer ( $\sim 1$   $\mu\text{m}$ ) can result in a serious dysfunction of the injector. The *nozzle tip deposits* cause distortion of the optimum spray pattern [3,6,8] and may heat up to very high temperatures. The *needle ball and seat deposits* [6] can spoil the seal, leading to increased leakage rate.

The studies of the injector deposits meet with serious difficulties. The first obstacle is that the *deposition process is very slow*. The accumulation of observable amount of deposits requires many hours of engine operation [1]. For this reason, many studies and standardized tests of fuels and machinery are accelerated – e.g., the fuel is artificially additized with a fouling agent that produces deposits [9-11], or the degradation is investigated at increased partial pressure of  $\text{O}_2$  [12]. The second obstacle is that, once formed, the *deposits experience complicated evolution* [13]. This causes uncertainty in the literature regarding their composition – the deposit that is initially formed has little to do with the deposit one finds after 30 hours of engine operation, exposure to high temperature, combustion gases, lubricant mist, and corrosion products. A third obstacle is that the field deposits are often caused by problems specific to a particular fuel or engine (e.g., specific combination of additives). Hence, it is likely that there is no one general mechanism of formation of the injector deposits.

Yet, there are several general features of the deposit formation that seem to be valid not only at the injector surface but anywhere in the engine. First, the engine deposits are formed in a *liquid hydrocarbon* phase, and the existence of fuel (or lubricant) in liquid state is a requirement for them to occur [1,14-17]. Second, the deposits are a polydisperse mixture of polar oxidized hydrocarbons (HCs) with dispersed organic and inorganic salts [3,6,18-20]. Third, the deposit growth process occurs at a hydrophilic surface in contact with a hydrophobic fluid. For the injector, this is the interface *polar deposit/liquid fuel*; with brand new injectors, it could be the metal oxide|liquid fuel or the metal oxide|lubricant interface instead. Generally, every component of the injector that is in contact with hot liquid fuel inevitably forms deposits. Fuel degradation is observed already in the common rail and its filters [21]. The *internal injector deposits* found on the needle and the pressure control valve [22] are a serious problem in diesel engines. They are similar in nature to the filter soapy deposits – this suggests they are mostly a filtration problem and we do not consider them here. We are mainly interested by the *external injector deposits* [3-6], which are common with gasoline direct injection engines, where they accumulate at the injector tip, inside the nozzle channel and even deeper inside the nozzle, on the needle ball and seat [6,23]. The problem is not so pronounced with diesel injectors, probably because diesel fuels normally do not form deposits inside the nozzle channel [3]. Most of the deposited material at the tip is fuel-derived, bearing chemical similarities with

fuel gum [23], but blended with lubricant elements of percentage increasing with the increase of the distance from the nozzle hole [6,12]. The chemistry of the fuel affects the injector deposits very significantly, especially when polar blends are used. Thus, for gasoline, an ethanol blend results in lower deposit propensity [6,24]; on the opposite, the relatively polar biodiesel blends in diesel lead to more deposits, and in addition, unlike normal diesel, biodiesel forms deposits also inside the channel [3].

The initial young deposit, or proto-deposits, could be a viscous liquid (e.g., [13]) of high oxygen content distributed in products of the low-temperature oxidative degradation of the fuel (such as alkylhydroperoxides, aldehydes, ketones, alcohols, ethers and acids, found in the tip deposits – e.g., [4]). Aromatic species native to the fuel are also found in the deposit [4,25]. In contrast, in the final stages of its evolution, the deposit loses the organic oxygen – for example, the fresh deposit at the diesel injector tip contains 20 w% oxygen [3], while the older one located further away from the nozzle is of lower O-content (~10 w%). The deposit evolution leads also to increased aromatic content, porosity, advanced polymerization; lubricant- and corrosion-derived material stick to the deposit, eventually forming together with the organics the familiar reinforced composite material that is so hard to remove.

The precursors of the external gasoline injector deposits, according to Ref. [6], are polar compounds present in the fuel, peroxides, and ash. It has been claimed that two main chemical routes contribute to the formation and the evolution of the injector deposits – low-temperature autoxidation [6,12,26] and high-temperature pyrolysis [6,12], with subsequent isomerization and polymerization of the fuel [12]. Indeed, there is a strong correlation between the outcome of various standardized liquid phase oxidation bench tests and rate of deposit formation [27] (indicators in use are the induction time for the onset of the intensive consumption of oxygen for gasoline in a closed reactor at 100°C and 1 atm O<sub>2</sub>, and the mass of the oxidation products formed at 110°C for 6 h in air). On the other hand, the formation of polyaromatic hydrocarbons occurs at  $T \sim 350^\circ\text{C}$  [6] and is probably a secondary process. The substrate may influence these processes by acting as a catalyst [6]. A separate process that contributes to the deposit mass is the deposition of lubricant-derived salts (ash), which we will not consider here.

Venkataraman and Eser [4] reported interesting data on the microstructure of the *tip deposits*. The material contains clusters of spherical particles forming densely packed aggregates, with large voids between the aggregates. The clusters appear to have uniform size distribution. This suggests the deposit phase grows *in the bulk* of the liquid phase, with subsequent precipitation. The vaporization of the fuel is the process that induces the precipitation. This agrees (at least broadly) with the mechanism of Kinoshita et al. [5] for the formation of gasoline injector deposits. *Nozzle channel deposits*, on the other hand, appear more compact – probably, upon each injection, the turbulent flow removes the loosely attached particles stemming from the bulk phase and only truly interfacial processes contribute to the rate of formation.

While there are studies of the fuel degradation mechanism under steady laboratory conditions (e.g. [28,29]; brief review can be found in [1]), to our knowledge, only one study [1] attempts to model the degradation under engine conditions. There are several major differences between engine and laboratory conditions, summarized in **Table 1** and explained in more detail in the following sections. Engine conditions complicate additionally the experimental investigation of the injector deposits, leading to incomprehensible and sometimes contradictory results in the literature – as summarized by Xu et al. [6], “...*The mechanism of GDI injector deposit formation is not completely understood. The only proposed mechanism available in the literature concerns the deposit precursors, the  $T_{90\%}$  parameter of the fuel, and injector nozzle temperature. There is a lack of agreement of the role of nozzle temperature and  $T_{90\%}$  in GDI injector formation...*” A lot of information about the deposition can be gained on theoretical

grounds – the general mechanism of fuel degradation is known in detail [30,31], and one can predict the fate of the fuel droplet exposed to the cylinder gases with semi-quantitative accuracy. In particular, modelling would allow better comprehension of the role of the distillation characteristics and the wall temperature sought by Xu et al. [6]. The conditions at the injector tip (variations of pressure, temperature, gas phase composition) are easier to predict theoretically than followed experimentally. Modelling can be used also to understand some of the basic effects that deposits have on engine operation – the effect of the nozzle channel deposits on the injection flow rate [3,6,12] and the effect of the tip deposits on the tip temperature are particularly interesting.

**Table 1:** Peculiarities of fuel degradation under cylinder compared to laboratory conditions.

<b>Laboratory conditions</b>	<b>Cylinder</b>
initiation by $O_2$ , or forced initiation by $R_2O_2$	initiation by $NO_2$ , branching by $NO$
<i>steady process:</i> constant or slowly changing temperature $T$ and initiation rate $v_i$ , quasi-stationary regime for $RO_2$ .	<i>cyclic process:</i> fast variations of $T$ , fast variations of $v_i$ , cyclic accumulation of $RO_2$ .
continuous process, significant time for reaction and conversion	cyclic, milliseconds for reaction, small conversion for one cycle

Our aim in this study is to make an attempt to rationalize the existing observations for the deposit formation process, by simulating the degradation of various model fuels under engine conditions. Simulation of an engine operating cycle in the cylinder is performed to define all relevant physicochemical conditions in the required detail. We also investigate the effect the injector deposits have on the engine performance and compare the model results with qualitative and quantitative data available in the literature. Order of magnitude estimates allow us to discard some of the seemingly possible hypotheses for the mechanism of deposition and to formulate a model that does not contradict the observations.

## 2 Mechanisms of deposit formation

In accordance with the brief review above, we assume that the deposit formation is the result of the following sequence of events. After the injection, a fuel droplet leaks out of the injector [1,2]. At the peak of the cylinder pressure, this droplet is below its boiling temperature and its temperature is close to that of the injector wall,  $T_{wall}$ . During the power stroke, the cylinder heats up, the droplet is bombarded by radicals produced by the combustion process and degrades. As pressure decreases late in the stroke, the droplet starts to boil. The non-volatile degradation products either precipitate in the fuel film (as hypothesized in Ref. [5]) or adsorb at the surface.

The observations in Ref. [4] suggest that the tip deposit is made of the precipitated material. On the other hand, whatever material precipitates in the nozzle channel will be washed away with the next injection, and only the material which is directly adsorbed at the wall can withstand the turbulent shear of the fuel flow within the nozzle. These two modes of accumulation can be considered as two limiting cases: the precipitation mechanism gives the largest possible rate of deposit formation; the adsorption mechanism gives the smallest one.

## 2.1 Conditions in the fuel film and the quench layer

### 2.1.1 Engine model

A virtual model of a real direct injection spark ignition test engine is constructed using the *SRM Engine Suite* software [32]. The simulation uses the *stochastic reactor model* (SRM) – a zero-dimensional model based on a discretization of the probability density function transport models [33]. It splits the cylinder charge into an ensemble of *stochastic particles* that represents the distribution of the composition, temperature, pressure etc. within the cylinder. This method is very suitable for problems involving complicated chemical processes occurring in turbulent environment. The implemented mechanism of the combustion process in the gas phase involves 208 species and 1002 reactions (provided in Ref. [34]). The turbulent mixing process is modelled with the *Euclidean minimum spanning tree* technique [35]. The software contains also sub-models of a number of relevant processes in the engine, including the stochastic heat transfer, the piston movement, the spark ignition, the direct injection [36] and many others. It has been validated against data for a variety of gasoline and diesel, spark and compression ignition engines, with fuels of different composition, cf. e.g. Refs. [36-38].

The parameters of the engine are listed in **Table 2** (a more detailed description is given in S1). The engine operates with stoichiometric mixture. Full load conditions were modelled (2840 rpm, 23.8 kg/h air per cylinder). Early injection strategy is applied: in the real engine, the injection starts at -311 crank angle degrees (CAD) with respect to the top dead centre (or 49° after the TDC of the gas exchange strokes) – i.e. the fuel is injected while air intake valve is still open. Atomization and mixing are presumably already complete when the inlet valve closes near the bottom dead centre (BDC). Only the range from -180 to 180 CAD is simulated (where 0° is the TDC between compression and expansion strokes). The contribution of the intake and exhaust strokes to the engine parameters (indicated & break mean effective pressure – IMEP & BMEP, heat transfer, exhaust composition etc.) were accounted for only approximately and their contribution to deposit formation rate will be neglected below.

**Table 2:** Model DISI engine parameters (for 1 cylinder).

Parameter	Value		
Displaced volume	400 cm <sup>3</sup>		
Compression ratio	10		
Speed, $\nu$	2840 rpm		
Air mass	23.8 kg/h		
Fuel mass	1.6 kg/h		
Equivalence ratio	1		
Spark timing	-19 CAD		
	simulation	experiment	difference
Fuel	PRF95	E10	
BMEP	0.63 MPa	0.6 MPa	5%
IMEP	0.775 MPa	0.67 MPa	-16%
MFB50	14 CAD	10 CAD	
Maximal cylinder pressure	3.7 MPa	3.7 MPa	< 1%

Fuel in the model engine is PRF95 (95 w% isooctane, 5 w% n-heptane) and was used to calculate representative thermal boundary conditions for the later study. Exhaust is present in the initial charge and is essential for the correct calculation of the relevant engine experimental parameters (pressure profile, in particular). 6% of the oxygen present in the cylinder after the



inlet valve closes is in the form of CO<sub>2</sub>, H<sub>2</sub>O, CO and NO left from the previous cycle (the precise initial composition is given in S1). Another major effect of the presence of the hot exhaust is the elevated initial temperature (82°C) of the charge at inlet valve closure.

The virtual engine represents well the maximum pressure (less than 1% error) and the MFB50 – 50% mass fuel is burned at +14 CAD (calculated) vs. +10 CAD (experimental). IMEP and BMEP are also reasonable, in view of the fuel difference and the approximated calculation of the exhaust & intake strokes contribution (IMEP prediction error –16%). The test engine data refers to E10 gasoline with 10% ethanol blend, but as far as the two fuels have similar lower heating value and octane number, the pressure profile and the characteristics that are compared in Table 2 can be expected to be similar.

### 2.1.2 Leakage of fuel and temperature of the fuel film

The rate of leakage of fuel out of the nozzle of a diesel injector has been shown to vary during a cycle [2] and this is likely to be the case for gasoline injectors, even though they operate at lower injection pressures. The authors are not aware of data in the literature quantifying the variation of fuel dribble rate with time (cf. Ref. [1] for an attempt to model it). Discharge of fuel after the intended injection event is an undesirable phenomenon, as it results in uncontrolled addition of fuel in the cylinder in a poorly prepared state. The typical value of the leaked amount is 0.1% of the injected fuel mass [39]. Leakage causes deposits, but the opposite may also be the case: it was found that deposits can cause severe leakage [7], probably due to their occurrence at the needle seat and ball [6].

An important feature of the leakage in the engine is that the conditions are usually such that the fuel is below its boiling temperature  $T_b$  when the piston is near the TDC and the pressure is high, but then, as pressure falls later in the combustion stroke, the leaked droplet reaches its boiling point. If this is the case, we will speak about *deposition in the boiling regime*. The boiling was observed experimentally in an injector test rig in Ref. [40]. Hexadecane was injected in the rig; after the end of the injection, a fuel droplet leaked out of the nozzle exit while the conditions were still near the peak pressure (~5 MPa). The droplet grew until it started to boil visibly at about +50 CAD. A few CA degrees later, the droplet had vaporized completely, leaving behind a black residue [40]. This residue can be assumed to be the proto-deposit phase from which the deposits arise.

The point of boiling is thus of obvious importance for the deposition process. In this initial work, to determine it, we assume that the fuel behaves as a single-component liquid (which is reasonable for PRF95), and its boiling temperature  $T_b$  is related to the cylinder pressure  $p$  through the Clapeyron's equation:

$$T_b = T_{b0} \left( 1 - \frac{RT_{b0}}{\lambda_b} \ln \frac{p}{p_0} \right)^{-1} \quad (1)$$

Here  $T_{b0}$  is the boiling temperature of the fuel at standard pressure ( $p_0 = 101325$  Pa) – for PRF95,  $T_{b0} \approx 373$  K [41].  $R$  is the universal gas constant;  $\lambda_b$  is the heat of vaporization  $\approx 35.1$  kJ/mol for PRF95 [41]. The simulated cylinder pressure profile in the SRM engine and the respective change of the boiling temperature with time are shown in **Figure 1**.

A typical gasoline injector surface temperature ( $T_{wall}$ ) is in the range 120-190°C [42]; therefore, during each cycle, the boiling temperature of the leaked droplet changes from well below the average surface temperature to well above it. This suggests the following evolution of the injector dribble:

(i) early in the compression stroke, where  $T_b < T_{\text{wall}}$ , the fuel film will be boiling, and its temperature will remain equal to  $T_b$  as long as liquid phase is present. No or little accumulation of liquid fuel is possible.

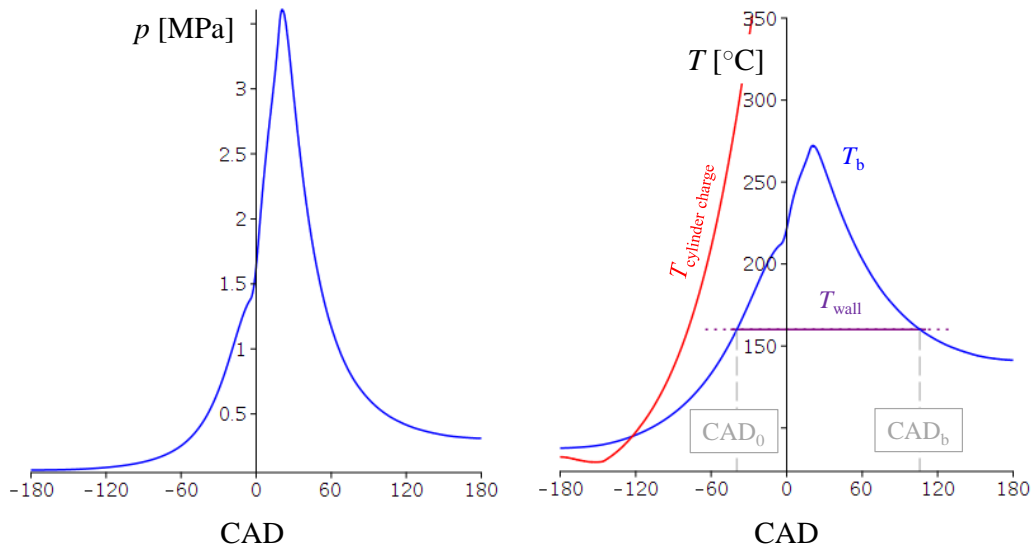
(ii) As the pressure increases, so does  $T_b$ , until the point where  $T_b = T_{\text{wall}}$  is reached (*start of the accumulation* –  $\text{CAD}_0$  in Figure 1). At  $\text{CAD}_0$ , boiling ceases; fuel film temperature will remain equal to  $T_{\text{wall}}$ . This situation will continue until after the pressure peak, where  $p$  decreases and  $T_b$  drops below  $T_{\text{wall}}$  again.

(iii) At this point, the fuel will swiftly vaporize and the non-volatile residue will precipitate at the wall (*point of boiling and precipitation* –  $\text{CAD}_b$  in Figure 1).

Thus, during the whole process, the temperature of the fuel film around the injector nozzle, if such film is present, will be approximately equal to the smaller of  $T_b$  and  $T_{\text{wall}}$ , i.e.

$$T^{\text{F}} = \min(T_b, T_{\text{wall}}), \quad (2)$$

where  $T^{\text{F}}$  is the temperature controlling the rate of fuel degradation, and, respectively, the rate of deposit formation. Thus, both wall temperature and boiling characteristics are important for the deposition, in agreement with the experimental findings [5,6,12].



**Figure 1.** *Left:* variation of cylinder pressure  $p$  as function of crank angle degrees (CAD) during the engine cycle (SRM Engine Suite simulation). *Right:* variation of boiling temperature  $T_b$  (blue line), calculated via Eq (1), simulated temperature of the combustion gases ( $T_{\text{cylinder charge}}$  – red line), and average injector wall temperature ( $T_{\text{wall}}$  – purple line, set to  $160^\circ\text{C}$ ) during the engine cycle. Between  $\text{CAD}_0$  and  $\text{CAD}_b$  (where  $T_b > T_{\text{wall}}$ ), leaking fuel accumulates. This fuel vaporizes completely when the boiling point drops below  $T_{\text{wall}}$  (outside the range  $\text{CAD}_0$  to  $\text{CAD}_b$ ).

The deposit model described in the present work mainly concerns the initial stage of the fuel degradation process (the one that occurs in the liquid phase). It will be assumed below that this stage starts at  $\text{CAD}_0$  and finishes at  $\text{CAD}_b$  – i.e. during the accumulation of leaked fuel at the injector tip. The points  $\text{CAD}_0$  and  $\text{CAD}_b$  are controlled by the fuel boiling point  $T_b$ . During the fuel film accumulation,  $T^{\text{F}} = T_{\text{wall}}$ . For a multicomponent fuel, instead of a single boiling point  $\text{CAD}_b$ , a *range* of boiling will occur (e.g. [17], *sec.4.5.4* of Ref. [43]), which will contribute to the degradation process significantly – for the sake of simplicity, we will leave this question aside.

Within the SRM engine model, the injector wall temperature is an independent variable, unrelated to the cylinder pressure profile and therefore, unrelated to the  $T_b$  vs. CAD characteristic. Consequently, the dependence of  $\text{CAD}_0$  and  $\text{CAD}_b$  on the injector wall

temperature follows directly from **Figure 1** (the blue line in **Figure 1-right** is a plot of the inverse function  $T_{\text{wall}}(\text{CAD})$ , as illustrated in Figure S1 in S1). In the normal range of gasoline injector wall temperatures,  $\text{CAD}_0$  ranges between  $-72$  and  $-20^\circ$  and the point of boiling,  $\text{CAD}_b$ , is larger than  $+69^\circ$ . At low wall temperatures (below  $141^\circ\text{C}$  for the case in Figure 1), or for fuels of low volatility, conditions are possible where the leaked fuel never boils – in this case, instead of the boiling regime, a qualitatively different and supposedly slower regime of deposit formation can be expected to occur (*cold injector regime*, cf. Figure S1). In the other limit – where wall is very hot ( $T_{\text{wall}} > 272^\circ\text{C}$  for the case in Figure 1) or fuel is volatile – the fuel will boil throughout the cycle without accumulation, and thus it will not stay exposed for significant periods to the action of radicals produced by the combustion gases. This case would correspond to a third, *hot injector* regime of deposition (Figure S1). Once the droplet approaches the hot injector regime, the deposit formation rate should decrease again – indeed, at high injector temperatures, less deposition is sometimes observed [42]. These two regimes will not be considered here.

A complicated question that is relevant to the rate of deposition stands: what is the volume of the leaked droplet? Even if the leakage rate is constant, which is hardly the case [2,39,1], the droplet size will be increasing during the high pressure period between  $\text{CAD}_0$  and  $\text{CAD}_b$  (although the evaporation rate may be a limiting factor). After  $\text{CAD}_b$ , as the fuel will boil, the volume is expected to decrease swiftly to zero. In the absence of data, we assume that the volume of the droplet is constant between  $\text{CAD}_0$  and  $\text{CAD}_b$  (while  $T_{\text{wall}} < T_b$ ), and is negligibly small otherwise. The respective average thickness of the fuel film (or droplet height) is assumed to be  $\sim 100 \mu\text{m}$  while  $T_{\text{wall}} < T_b$ , as follows from direct observations [40], i.e.

$$h^F/[\mu\text{m}] = 100 \times \eta(\text{CAD} - \text{CAD}_0) \times \eta(\text{CAD}_b - \text{CAD}), \quad (3)$$

where  $\eta$  is the Heaviside step function.

### 2.1.3 Modelling the quench layer

The fuel film at the injector tip exchanges matter with the cylinder charge through the cold quench layer in direct contact with the film. The transport of combustion products from the bulk gas to the quench layer is a complicated phenomenon involving numerous unavailable characteristics of the turbulent transport. The boundary conditions are also unclear, due to many possible surface reactions. The composition of this layer is of paramount importance for the degradation process. Due to the low temperature and the high oxygen concentration in the quench layer, the reactivity and the concentrations of radicals there change drastically compared to the cylinder bulk. Therefore, even in case of efficient mixing, the mean composition of the cylinder will be very different from the one next to the injector wall.

To model the quench layer, we use a modification of the zone functionality of the SRM Engine Suite [44]. The cylinder charge is separated in two zones, a main one (*cylinder bulk*) and an auxiliary wall zone (*injector quench layer*). In our modification, the mass of the quench layer zone is set to a negligibly small fraction of that of the cylinder charge ( $1/50000$  – the exact value does not affect the results). The temperature of the quench layer zone is fixed to  $T_{\text{wall}}$  of the injector surface. The two zones are allowed to exchange mass as described in Ref. [44]. The species transported from the combustion gases to the cold quench layer react in the auxiliary zone, following the implemented reactions [34].

This rough quench layer model has a single transport parameter: the pair mixing fraction  $\xi$  [44], controlling the mass exchange between the two zones. This parameter is proportional to the turbulent transport intensity. It is an empirical constant of unknown “best” value; we were able to bound its value within three orders of magnitude ( $10^{-6}$ – $10^{-4}$ ) outside which the quench

layer composition is unreasonable (if  $\xi \rightarrow 0$ , the composition of the quench layer is almost equal to the one of the initial charge; if  $\xi \rightarrow \infty$ , the composition of the cylinder becomes equivalent to that in the quench layer). When  $\xi = 5 \times 10^{-5}$  the order of magnitude of the final deposition rates in a few test cases was reasonable compared to the experimental values. We further used this value for all simulations. We estimated that this value of  $\xi$  corresponds to characteristic time of mixing during the power stroke of the quench layer and the cylinder charge of the order of 100 ms, cf. S1. In the absence of experimental data, the value of  $\xi$  has not been further adjusted. It is also implicitly assumed in our model that during intake and exhaust strokes, the mixing is much more efficient (due to the lower gas density and the intensive gas convection), and most of the quench layer content is exchanged with fresh charge when the inlet valve closes.

In the mechanism we consider below, the fuel degradation follows the known routes for low-temperature oxidation of hydrocarbons [30,31]. The mechanism of oxidation of alkanes is quite general; the specificity of each system lays mostly in the *initiation stage*, where radical chains are generated by an external source of radicals of certain intensity measured with an *initiation rate*  $v_i$  [30,31]. This stage requires careful analysis when it comes to deposit formation. In particular, one must identify the nature of the initiator.

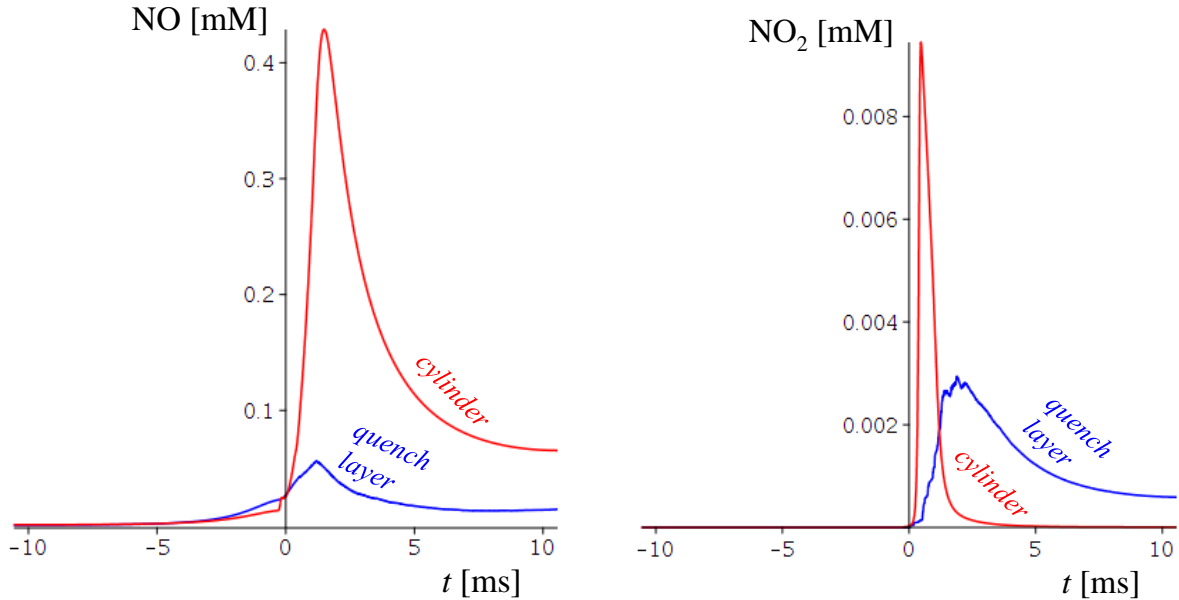
A common assumption in the literature is that the radical chain leading to fuel degradation is initiated by the dissolved oxygen [1,28,29]. In the lubricant literature, however, it has been established that the lubricant degradation is initiated by gas phase radicals transported through the quench layer and penetrating into the lubricant film [45-49]. It is posited here that the same mechanism plays a role in the degradation of the fuel film at the injector wall. Therefore, our first task is to investigate the possible radical chain initiators in the quench layer.

We used our quench layer model to shortlist the species that can initiate a radical chain in the fuel film. The two criteria for shortlisting were high concentration and high reactivity (data for the initiation rate of various initiators is available [31]; in most cases, we assumed that the ratio between the fuel film and quench layer concentration of the order of 1, in the absence of data). The gas species we could identify as problematic are the following:  $\text{NO}_2$ ,  $\text{NO}$ ,  $\text{HO}_2\cdot$ ,  $\text{CH}_3\cdot$ ,  $\text{C}_3\text{H}_5\cdot$ ,  $i\text{-C}_4\text{H}_7\cdot$ ,  $\cdot\text{CH}_2\text{CHO}$ ,  $\text{CH}_3\text{O}\cdot$ ,  $\text{CH}_3\text{O}_2\cdot$ ,  $\text{C}_8\text{H}_{17}\text{O}_2\cdot$ ; oxygen was also considered. Among these species, the estimated rate of initiation was the highest for  $\text{NO}_2$ , significantly more than the total contribution of all other species. The second most important initiator is the oxygen. Certain very reactive species present in the quench layer (such as  $\text{CH}_3\text{O}\cdot$ ) contribute insignificantly to the initiation compared to  $\text{NO}_2$  in part due to depletion (cf. S3).

In addition to  $\text{NO}_2$ , we found that nitric oxide  $\text{NO}$  also contributes significantly to the degradation process. From our quench layer model it follows that  $\text{NO}$  has quite high concentration near the injector wall at the considered stoichiometric conditions, especially near the pressure peak – the dependence on time during an engine cycle is shown in **Figure 2-left**. However, its role is not of an initiator. We found no data for possible hydrogen abstraction reactions from the fuel hydrocarbons by  $\text{NO}$ . Therefore, we investigated other possible reactions discussed in the literature and found one that reaches a significant rate – this is  $\text{RO}_2\cdot + \cdot\text{NO} \rightarrow \text{RO}\cdot + \cdot\text{NO}_2$ , cf. e.g. [50,31]. It is essentially a branching step since it converts the peroxide radical,  $\text{RO}_2\cdot$ , which is not very reactive under the conditions in the fuel film, to a very reactive alkoxy radical  $\text{RO}\cdot$ .

The simulations suggest that late in the combustion stroke, the concentration of  $\cdot\text{NO}_2$  in the quench layer is higher than that in the bulk of the cylinder, **Figure 2-right**. This excess  $\cdot\text{NO}_2$  is produced by the nitric oxide: when the latter is transported to the quench layer, it reacts with the oxygen there. Note that the quench layer contains much more  $\text{O}_2$  than the cylinder (the simulated profiles are given in Figure S2 in S1) – the oxygen remains at high concentration

throughout the cycle as no combustion occurs in the quench layer and the time for exchange is long during the power stroke. In the relevant temperature range, according to our model, the quench layer concentrations of  $\cdot\text{NO}$  and  $\cdot\text{NO}_2$  are only weakly dependent on the wall temperature (apart from the trivial dilution effect due to  $C \propto 1/T_{\text{wall}}$ ) – this is illustrated Figure S3 in S1.



**Figure 2:** Simulated evolution of the concentration of nitric oxide (*left*) and nitrogen dioxide (*right*) in the quench layer at the injector wall (blue lines). The respective concentrations in the cylinder bulk are shown for comparison (red).  $T_{\text{wall}} = 160^{\circ}\text{C}$ .

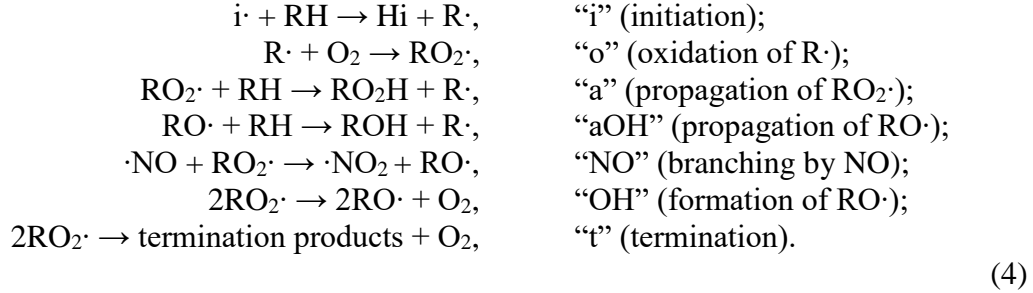
There must be a significant amount of the alkanes in the quench layer (as much a molar fraction of 1 right next to the surface when the fuel is at its boiling temperature). The hydrocarbon vapours will dilute the gases in the quench layer, leading to decrease of  $[\text{O}_2]$  and  $[\text{NO}_x]$  there, which can slow down the degradation. On the other hand, the vaporized fuel in the quench layer will degrade itself, contributing to the deposition and compensating in part for the dilution effect. At the peak of the pressure (around which the most of the deposition occurs), we expect both effects to be small. Therefore, for simplicity, we neglected the effect. Another complication we neglect is that there exist other possible ways to initiate the oxidation. One mechanism that can be important for the deposits *inside* the nozzle channel is oxidation initiated by shear stress (e.g., *sec. 1.10.1* in Ref. [51], [52]).

## 2.2 Degradation of the fuel film

The chemical pathways for low-temperature oxidative degradation of hydrocarbons are known in some detail [30,31]. A number of studies modelled the process with accent on fuels [1,28,53,54]. However, we are not aware of any studies of fuel degradation under reciprocating engine conditions. There are major differences between a typical fuel degradation laboratory test and the degradation of the fuel film at the nozzle tip under the violent cylinder conditions during a cycle, summarized in **Table 1**.

For a gasoline film at the injector tip, the fuel temperature is in the range  $T^F = 90\text{--}190^\circ\text{C}$ . The concentration of the oxidation products in the fuel at CAD<sub>b</sub>, where the droplet boils away, remains well below 1% (as the leaked fuel droplets have only few milliseconds to degrade) – this is a first significant difference to laboratory tests, Table 1. The major radical species involved in this early stage of the liquid phase oxidation, apart from NO<sub>x</sub>, are the alkyl radicals R·, the peroxide radicals RO<sub>2</sub>·, and the alkoxy radicals RO· [30,31].

We consider the oxidation of an alkane that propagates through intermolecular reactions rather than through intramolecular [55-57] ones – i.e. we assume that the considered alkane does not have the structural component H-CR<sup>1</sup>-CH<sub>2</sub>-CR<sup>2</sup>-H, where R<sup>1</sup> and R<sup>2</sup> are alkyl groups (this is valid for heptane and isooctane). The reactions we consider are:



By RH we denote the most reactive type of C-H bonds in the fuel film. Therefore, for n-alkanes and branched alkanes that do not contain tertiary C-atoms, [RH] is the concentration of the alkane times the number of secondary C-H bonds per molecule. For branched alkanes possessing tertiary C-atoms, [RH] is the alkane concentration times the number of tertiary C-H bonds per molecule (it must be valid that the tertiary C-H bonds are isolated, otherwise intramolecular propagation will contribute to the process [55,56]). For the considered mixture of isooctane and heptane,  $[RH] = 1 \times [C_8H_{18}]$ , as the isooctane contains a single tertiary C-H.

Let us now consider the rates of the reactions (4), starting with the *initiation*. In the engine, there are several possible initiators:  $i \cdot$  may stand for O<sub>2</sub>, ·NO<sub>2</sub>, HO<sub>2</sub>· etc. Assuming that all of them react with RH according to the bimolecular reaction (4)-i, for the total rate of production of R· we obtain

$$v_i = \sum_i k_i [i \cdot] [RH]. \tag{5}$$

The radical formation by O<sub>2</sub> may actually follow a third order rate law [31] ( $2RH + O_2 \rightarrow 2R \cdot + H_2O_2$ ). In Eq (5), the film temperature (and therefore  $k_i$ ) and especially  $[i \cdot]$  are time-dependent (Figure 1 & Figure 2), which is a second major difference to laboratory conditions, cf. Table 1. Among the species in the quench layer, the nitrogen dioxide is by far the most important initiator. The rate of initiation by [O<sub>2</sub>] (which is the one considered in the literature [1,28,29]) is much slower – using the rate parameters from Table S2 in S2, even if [NO<sub>2</sub>]/[O<sub>2</sub>] is of the order of 10<sup>-5</sup> as it follows from our simulations, the initiation rate due to NO<sub>2</sub> is still hundreds of times larger ( $k_{i,NO_2}[NO_2] \gg k_{i,O_2}[O_2]$  in the range 100-220°C). Initiation by [O<sub>2</sub>] may become important only at elevated temperatures and lean mixtures, especially if fuel does not contain tertiary C-H bonds – but even in this case, the NO<sub>2</sub> initiation should normally dominate. In addition, according to Mayo et al. [53], O<sub>2</sub> is of decreased solubility in fuel at  $T$  higher than 190°C, complicating further the hypothesis for O<sub>2</sub>-initiation.

*Oxidation.* The rate of the radical oxidation (4)-o is [30,31]:

$$v_o = k_o [R \cdot] [O_2]. \tag{6}$$

The process is very fast, as long as O<sub>2</sub> is not depleted. Little depletion is expected in the quench layer (Figure S2 in S2) – there, O<sub>2</sub> is even of increased concentration due to the compression.

*Bulk intermolecular hydrogen abstraction*, Eq (4)-a & aOH. Both major radical species present in the fuel, RO· & RO<sub>2</sub>·, are able to propagate the radical chain by abstracting a hydrogen atom from a nearby hydrocarbon molecule:

$$v_a = k_a[\text{RO}_2\cdot][\text{RH}] \quad \text{and} \quad v_{\text{aOH}} = k_{\text{aOH}}[\text{RO}\cdot][\text{RH}]. \quad (7)$$

The propagation of the third radical R· ( $\text{R}^1\cdot + \text{R}^2\text{H} \leftrightarrow \text{R}^1\text{H} + \text{R}^2\cdot$ ) has no effect on the process when a single hydrocarbon reacts (products are the same as the reacting species). However, it can have an equilibrating effect in case of mixture of HCs, which may be important for the deposition process. Seemingly, this reaction has not been studied in the literature, which might mean it is relatively slow. It is mentioned as a stage of the combustion of CH<sub>4</sub> by Emanuel' and Knorre [58].

*Bulk termination*: the reactions (4)-t & OH are simplified [30,31], but most parameters reported in the literature for the termination process refer to them. Their rates are:

$$v_t = k_t[\text{RO}_2\cdot]^2 \quad \text{and} \quad v_{\text{OH}} = k_{\text{OH}}[\text{RO}_2\cdot]^2. \quad (8)$$

Instead of  $k_{\text{OH}}$ , the  $a$ -parameter is often used (a measure of the ratio between the cage termination and cage alcohol propagation), related to the rate constants above as  $k_{\text{OH}} = k_t(1 - a)/a$  (Table S2).

Finally, the *branching reaction* (4)-NO is of rate [50]:

$$v_{\text{NO}} = k_{\text{NO}}[\text{RO}_2\cdot][\text{NO}]; \quad (9)$$

as most radical-radical reactions, it is only weakly dependent on the temperature.

**The values of the rate parameters** reported in the literature are, unfortunately, contradictory and the rate constants may vary by orders of magnitude depending on the source. A common mistake in the literature is the use of rate parameters referring to *one alkane molecule* together with parameters referring to *one reactive hydrogen atom* – for example, the values within a single table in Refs. [30,31] can refer to both definitions, without clear indication of which one is used. A second problem is the high percent of misquotations, vitiating the existing data collections. In Table S2, we collected relatively reliable data for the Arrhenius parameters of the reactions above (most of which are average values for several alkanes), that allow the calculation of the oxidation rate of normal and branched alkanes with sufficient accuracy for the aims of this work.

### 2.2.1 Gas transfer

The concentrations of the relevant reactive gases in the quench layer (which we interpret as concentrations at the location of the interface fuel|gas) is related to the film concentration through Henry's law,

$$[i\cdot] = K_{\text{H},i}[i\cdot]^{\text{G}}, \quad (10)$$

where  $[i\cdot]$  is the concentration in the film (again at the location of the surface, in case of bulk heterogeneity),  $[i\cdot]^{\text{G}}$  is assumed to be the simulated quench layer concentration, and  $K_{\text{H},i}$  is Henry's constant of the species  $i\cdot$ . Using this concentration in the rate laws above involves several strong approximations. First, a Fuchs layer may develop in certain cases. This would modify Eq (10) with a Hertz-Knudsen term (discussed in S3). The second assumption is that the concentration  $[i\cdot]$  is homogeneous – actually, the radical needs some time to diffuse through the liquid. This second assumption will hold if the convective diffusion in the leaked droplet is fast enough. If the transport process was driven by pure diffusion, for the period between CAD<sub>0</sub> and CAD<sub>b</sub> ( $\tau_{\text{degr}} \sim 5$  ms), the diffusion length is  $L_i \sim (D_i \tau_{\text{degr}})^{1/2} \sim 1$  μm, where  $D_i$  is the diffusion coefficient of  $i\cdot$  in the fuel phase ( $\sim 10^{-10}$  m<sup>2</sup>/s). As  $L_i$  is small compared to the film thickness  $h^{\text{F}}$ , only a relatively thin portion of the film would have been saturated under these conditions.

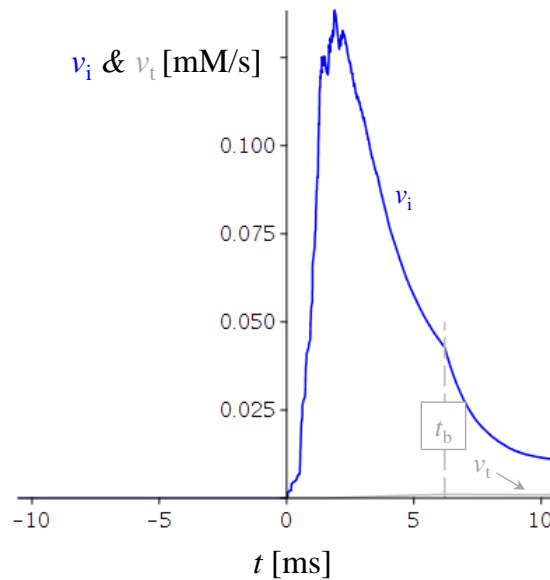


However, during the accumulation stage, a massive Marangoni flux develop, driving liquid from the hotter three phase contact to the colder evaporating free surface (we investigated a similar process in Ref. [59]). The characteristic time of this flow is of the order of  $\eta^F R^F / \sigma^F$  ( $R^F$  – size of the droplet,  $\eta^F$  and  $\sigma^F$  – viscosity and surface tension of the fuel); its value is much less than ms for all reasonable values of these parameters, which means that the convective transfer from the surface to the bulk of the droplet is fast enough to equilibrate the distribution of  $i\cdot$  (unless they are not extremely reactive, cf. S3).

The values of Henry’s constants for the relevant gases at the considered temperatures for alkane liquid phase are not available in the literature, except for  $O_2$  [31]. For Henry’s constant of  $NO_x$ , we used the value  $K_H = 1$ , a rough estimate based on Refs [60,61]. In view of the approximate quench layer concentrations of  $[NO_x]^G$  we use (see Sec. 2.1.3), the absence of precise data for  $K_H$  should be unimportant for the final results, unless  $K_H$  has significant temperature dependence – such a dependence might affect the trends of the rate vs. temperature dependence which we discuss in the following sections.

### 2.2.2 Evolution of the film composition during a cycle

Comparison of the reaction times with the period  $\tau$  of the cycle (related to the engine speed as  $\tau = 2/\nu$ ) would show that the assumption for quasistationary state holds for the two more reactive radical species produced during the oxidation process,  $RO\cdot$  and  $R\cdot$ . However, this is not the case with the least reactive peroxide radical  $RO_2\cdot$ . Actually, our analysis shows that at the investigated conditions,  $[RO_2\cdot]$  remains low and in result, the rates  $v_i$  and  $v_{OH}$  (that are proportional to  $[RO_2\cdot]^2$ , Eq (8)) are low compared to  $v_i$ . We will demonstrate this rigorously post factum, after solving the kinetic problem under the assumption for small  $[RO_2\cdot]$  and using an iteration to test the assumption.



**Figure 3:** Initiation and termination rates in the film,  $v_i$  and  $v_t$  (blue and grey), as function of time  $t$ . Eqs (5),(8)&(14) were used (with initiation by  $NO_2$ ).  $T_{wall} = 160^\circ C$ . The comparison shows that  $v_i \gg v_t$ , meaning that the oxidation is in accumulation (non-steady) regime with respect to  $RO_2\cdot$ . After the boiling point  $t_b$ , the rate  $v_i$  has a cusp – before it, film’s temperature is equal to  $T_{wall}$ , and after it – to  $T_b$ .



According to reaction scheme (4) with  $[\text{RO}_2\cdot]^2$  neglected, the condition for quasistationary state for  $\text{RO}\cdot$  and  $\text{R}\cdot$  reads

$$\begin{aligned} d[\text{R}\cdot]/dt &= v_i + v_a + v_{\text{aOH}} - v_o \approx 0; \\ d[\text{RO}\cdot]/dt &= v_{\text{NO}} - v_{\text{aOH}} \approx 0. \end{aligned} \quad (11)$$

Substituting here Eqs (6)-(7), and solving for  $[\text{R}\cdot]$  &  $[\text{RO}\cdot]$ , one obtains the relation of these concentrations to  $[\text{RO}_2\cdot]$  and  $v_i$ :

$$\begin{aligned} [\text{RO}\cdot] &= \frac{k_{\text{NO}}[\text{NO}]}{k_{\text{aOH}}[\text{RH}]} [\text{RO}_2\cdot]; \\ [\text{R}\cdot] &= \frac{v_i + (k_a[\text{RH}] + k_{\text{NO}}[\text{NO}])[\text{RO}_2\cdot]}{k_o[\text{O}_2]}. \end{aligned} \quad (12)$$

The mass balance for  $\text{RO}_2\cdot$  under the considered conditions reads:

$$d[\text{RO}_2\cdot]/dt = v_o - v_a - v_{\text{NO}} = v_i, \quad (13)$$

where we used the first of Eqs (11). This rate is not zero, so accumulation regime holds for  $\text{RO}_2\cdot$ . The concentration of the peroxide radical follows from the integration of Eq (13):

$$[\text{RO}_2\cdot] = \int_{t_0}^t v_i dt, \quad (14)$$

where  $t_0$  is the moment of the beginning of the degradation process ( $t_0 = \tau \times \text{CAD}_0/720^\circ$ ). In contrast, in the steady laboratory regime, where  $[\text{RO}_2\cdot]^2$  is significant and  $v_i = 2v_t$ , one obtains for  $[\text{RO}_2\cdot]$  the classical result [53,30,31]:

$$[\text{RO}_2\cdot]_{\text{st}} = (v_i/2k_t)^{1/2}. \quad (15)$$

The initiation rate  $v_i$  is calculated via Eq (5) (with  $i \cdot \equiv \text{NO}_2$ ) in **Figure 3**, using the rate parameters from Table S2,  $T^F$  for the temperature of the film and the simulated evolution of  $[\text{NO}_2]$  in the quench layer (Figure 2-*right*). The initiation rate follows the trend of the concentration  $[\text{NO}_2]$  in the quench layer and thus has a maximum near the pressure maximum.

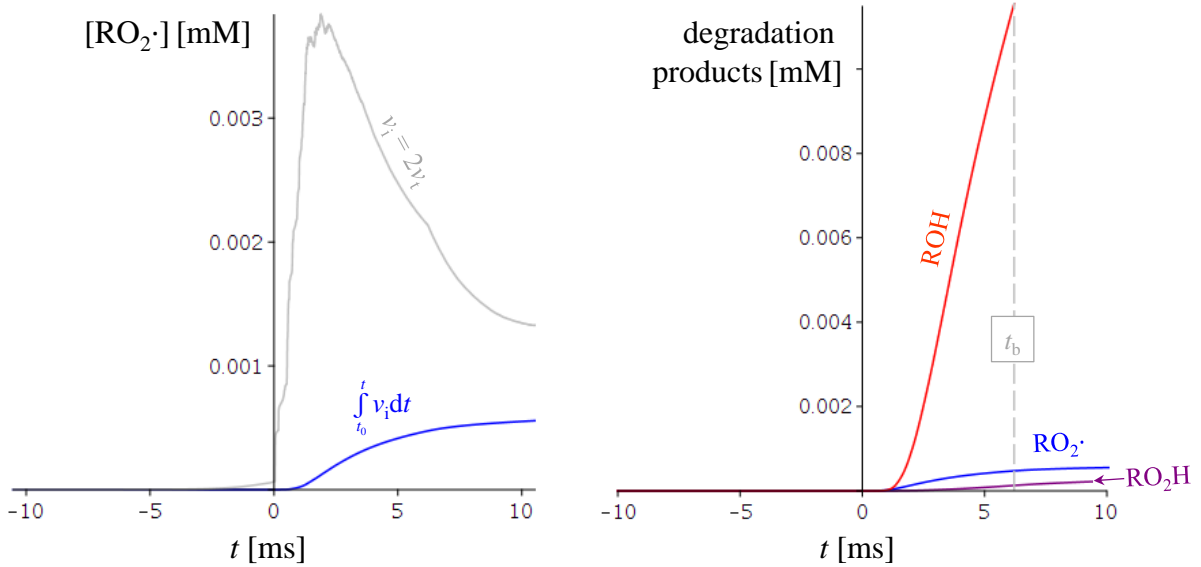
The initiation rate is further integrated according to Eq (14) to yield the concentration  $[\text{RO}_2\cdot]$  during a cycle – **Figure 4**, blue line. Using it, we can calculate the termination rate  $v_t = k_t[\text{RO}_2\cdot]^2$  in first iteration – it is given in Figure 3 (grey line). As seen, the validity of the assumption  $v_t \ll v_i$  is confirmed. Thus, we reach another significant difference between laboratory conditions and cylinder (Table 1): in a bench test,  $\text{RO}_2\cdot$  has enough time to accumulate and to react through the termination reaction (4)-t, resulting into deposition process that is quasi-stationary with respect to  $\text{RO}_2\cdot$  (so Eq (15) is valid). If the process were following this regime, the concentration of  $\text{RO}_2\cdot$  would be proportional to  $v_i^{1/2}$ , as shown in Figure 4, grey line. Instead, the time for accumulation of the quantity of  $\text{RO}_2\cdot$  needed for significant rate of termination is of the order of tens of ms, longer than the period of the cycle. Therefore,  $[\text{RO}_2\cdot]$  must be calculated with Eq (14) (accumulation regime). This difference results in completely different dependences of the total oxidation rate in the two regimes on the conditions of the system ( $T$ ,  $v_i$  etc.). At the end of the cycle, the radicals  $\text{RO}_2\cdot$  are transferred to the proto-deposit phase (see Sec. 2.3.1 below), and with the next cycle, the whole process starts again – therefore, we refer to the engine-relevant regime as to *cyclic accumulation* of  $\text{RO}_2\cdot$ .

Once  $[\text{RO}_2\cdot]$  is known, one can proceed with the calculation of the concentration of the non-radical products of the reaction scheme (4). The rate of formation of the alcohol is equal to  $d[\text{ROH}]/dt = v_{\text{aOH}}$ , and that of the peroxide is  $d[\text{RO}_2\text{H}]/dt = v_a$ . Integration yields

$$[\text{ROH}] = [\text{RH}] \int_{t_0}^t k_{\text{aOH}}[\text{RO}\cdot] dt;$$

$$[\text{RO}_2\text{H}] = [\text{RH}] \int_{t_0}^t k_a [\text{RO}_2\cdot] dt, \quad (16)$$

where Eqs (7) have been used and  $[\text{RO}\cdot]$  is calculated via Eq (12). The evolution of the two concentrations during a cycle is given in Figure 4-*right*. As seen, the main product of the considered initial stage of the oxidation is the alcohol, and at the considered temperature, it reaches concentration of at most 0.02 mM (3 ppm) before the boiling point. The second most important product is the peroxide radical – in the accumulation regime,  $\text{RO}_2\cdot$  has concentration that is higher even than the one of the hydroperoxide  $\text{RO}_2\text{H}$ .



**Figure 4:** *Left* – concentration of  $\text{RO}_2\cdot$  in the film vs. time. Blue line: cyclic accumulation regime, Eq (14); grey line:  $[\text{RO}_2\cdot]_{\text{st}}$  that would hold if the stationary regime were acting, Eq (15).  $T_{\text{wall}} = 160^\circ\text{C}$ . *Right:* composition of the fuel film as function of time.

### 2.3 Rate of deposit formation

We investigate two mechanisms of deposition. The first one is relevant to the conditions at the injector tip, and involves solid particles (as Refs. [4,5] suggest). In this situation, we assume that the oxidized products accumulated in the fuel droplet are deposited at the injector surface once  $\text{CAD}_b$  is reached. The process involves **(i)** re-suspension of the deposit produced in the previous cycle by the injection and the dribble; **(ii)** adsorption of the oxidation products onto the extended surface of the suspension (i.e. *filtration* of the fuel by the suspended polar particles), and **(iii)** precipitation of the suspended particles after the droplet boils. The nozzle channel deposits cannot be produced by such mechanism as the solid particles will be swept off completely by the next injection. In this case, we assume another scenario, where the slower process of direct oxidation of the interface deposit|fuel is responsible for the deposition.

### 2.3.1 Re-suspension-filtration-precipitation mechanism

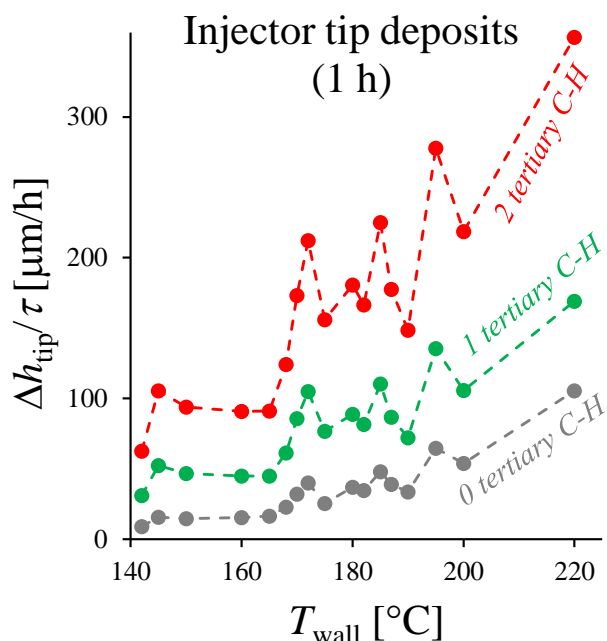
The morphology of the tip deposits – involving small primary particles, aggregates, large voids [4] – suggests that the deposit particle formation occurs in the bulk of the fuel film. Direct nucleation and subsequent precipitation is hardly possible, as the oxidation products are of very low concentration (few ppm, Figure 4) right before the point of boiling. A more consistent hypothesis is that the deposit left from the previous cycle is acting as a filter for the fuel, adsorbing the polar material produced by the oxidation. First, the droplet wets the porous deposit; the strong Marangoni flow during leakage re-suspends the particles precipitated during the previous cycle. Once  $CAD_b$  is reached, most of the fuel vaporizes, bringing about an increase in the concentrations of the oxidation products and the suspended particles. Under these conditions, the solid particles adsorb the oxidation products, acting as a filter. At  $CAD > CAD_b$ , as  $V^F$  decreases to zero, the three phase contact line recedes toward the nozzle hole. The suspended particles precipitate near the three phase contact line, probably following the coffee ring mechanism [62]. Possibly, a fraction of the particles is transferred inside the nozzle channel, but we neglect this. During the period where the surface is dry, the newly adsorbed material ages and degrades further (e.g., under the action of the  $RO_2\cdot$  radicals). Such a mechanism provides an explanation for the observed co-existence of fresh and aged material in the tip deposits [4]. It also gives good ground for the understanding of the mechanism of action of the fuel anti-deposit additives [6,19,63], which, by functionality, are dispersants.

If this re-suspension-filtration-precipitation mechanism is followed, one can assume that the amount of deposit produced in each cycle is approximately equal to the amount of oxidized products formed in the droplet until  $CAD_b$  is reached. The early oxidation products ( $ROH$ ,  $RO_2\cdot$ , and  $RO_2H$ ) separate as a polar phase (*proto-deposit*), adding mass to the pre-existing deposit each time the leaked droplets vaporize. We assume in addition that whatever further reactions occur in the polar proto-deposit phase, they do not lead to significant change of the deposit volume (neglecting the possible gasification process and the addition of lubricant-derived material). The moles of deposit precursors formed during one cycle is  $n^D = V^F \times ([ROH] + [RO_2\cdot] + [RO_2H])|_{t=t_b}$ , or per unit area,  $n^D/A^D = h^F \times ([ROH] + [RO_2\cdot] + [RO_2H])|_{t=t_b}$ . Here,  $h^F = V^F/A^F$  is the average thickness of the fuel film (fuel volume/covered area of the injector surface,  $\sim 100 \mu m$ ). If the average molar mass of the deposit precursors is  $M_d$  (about equal to the molar mass of  $ROH$ ) and the density of the deposit is  $\rho^D \sim 300 \text{ kg/m}^3$  (porous carbonaceous material), then, upon each cycle, the thickness of the deposit layer increases with

$$\Delta h_{tip} = \frac{M_d}{\rho^D} h^F \times ([ROH] + [RO_2\cdot] + [RO_2H])|_{t=t_b} . \quad (17)$$

For the three concentrations in the brackets, Eqs (14)&(16) are used. Thus, the increase of the deposit thickness is proportional to the amount of fuel leaking out of the nozzle ( $h^F$ ) and the produced concentration of the deposit precursors until the point of boiling.

Dividing  $\Delta h_{tip}$  by the period  $\tau$  of the cycle we obtain the average rate of deposit formation for the considered mechanism. It is illustrated in **Figure 5** (isooctane is in green), as a function of the wall temperature. The scatter is due to the stochastic nature of our simulations. Note that  $\Delta h_{tip}$  produced per cycle can hardly be constant for hours (despite the units we chose for the figure) – the formation rate changes as the deposit builds up, since the carbonaceous layer insulates the injector wall and leads to increased wall temperature (Sec. 3.2 below). In addition, Eq (17) is giving the formation rate only. Deposit is also removed from the wall by various processes, which normally limit the thickness to a certain stationary thickness [42,14,17] – see Sec. 2.3.3.



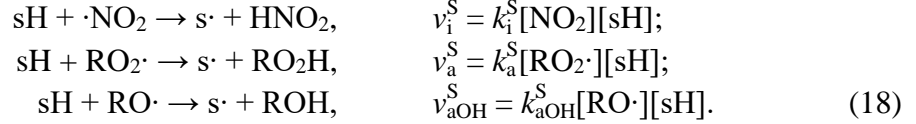
**Figure 5:** Rate of deposit formation at the tip (cycle-averaged) as a function of the wall temperature. For the effect of the alkane structure, 2,5-dimethylhexane (2 tertiary C-H bonds), isooctane (1 tertiary C-H) and 3-ethyl-3-methylpentane (0 tertiary C-H) are compared.

Let us now consider the effect of the chemical structure of the alkane components in the fuel on the deposition rate. One must distinguish between thermal stability and oxidative stability of a fuel component: thermally stable HCs are often easily oxidized [64], and from practice it is known that gasoline containing more branched alkanes (increasing the octane number) is actually causing worse deposits. This is at least in part due to the increased number of tertiary C-H bonds that are easy to oxidize. The mechanism above allows one to give a quantitative expression of this phenomenon, and use the values of the deposition rate to evaluate the propensity of various HC components in the fuel to form deposits. Let us consider three examples for alkanes: 3-methyl-3-ethylpentane, containing no tertiary C-H bonds; isooctane, containing one tertiary bond; and 2,5-dimethylhexane, containing two isolated tertiary bonds. We assume that the combustion of these species (mixed with 5 w% heptane) leads to the same quench layer composition as in Figure 2. The tip deposit formation rate will be affected by their structure: the 2,5-dimethylhexane is oxidized twice as fast as the isooctane, due to the additional tertiary C-H bond. Therefore, 2,5-dimethylhexane has value of  $\Delta h_{\text{tip}}$  twice as high as isooctane, cf. Figure 5-red line. The 3-methyl-3-ethylpentane is oxidized only through its six secondary bonds, for which the hydrogen abstraction is slow (Table S2). The result is that this compound has the slowest tip deposit formation rate, Figure 5-grey line. In the following section, we will show that the rate differences are even more pronounced with the nozzle deposit formation rate.

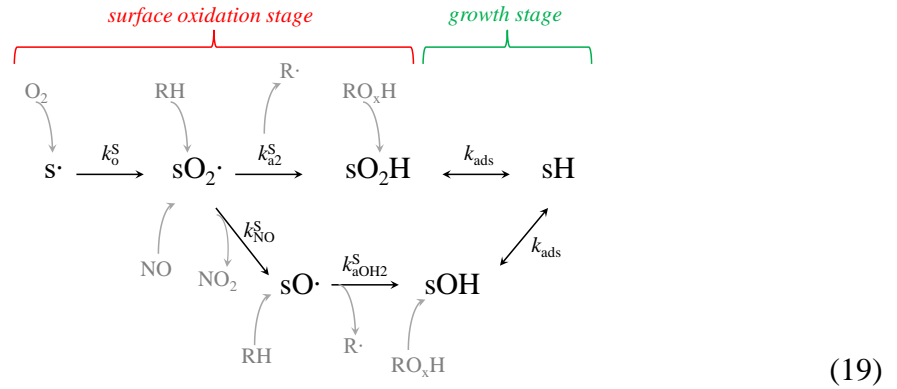
### 2.3.2 Surface oxidation-adsorption mechanism

Any suspended particles in the fuel trapped inside the nozzle channel will be swept by the next injection. Therefore, another mechanism of deposit formation must be acting for the nozzle channel deposits. Our hypothesis is that deposition occurs through direct growth at the deposit/fuel interface, proceeding in two steps: surface oxidation and addition of polar degradation products via adsorption (cf. Figure S4 in S2).

To model the oxidation of the surface of the deposit, we first make the hypothesis that all reactions that are possible in the bulk of the fuel are also principally possible at the polar deposit|fuel interface. This seems plausible, in view of the chemistry of this interface. The amphiphilic molecules (ROH, RO<sub>2</sub>H) at the interface must be oriented with the polar head group toward the polar deposit phase, and with the hydrocarbon tail toward the fuel. Thus, on the fuel side, the interface deposit|fuel will be dominated by CH, CH<sub>2</sub> and CH<sub>3</sub> groups. Let the surface concentration of the reactive C-H bonds be [sH], where “s” indicates *surface site*. A deposit-bound C-H bond can react with the radical species dissolved in the fuel, following the reactions similar to those in the bulk phase, Eq (4). Thus, the attack of the radicals ·NO<sub>2</sub>, RO<sub>2</sub>· & RO· will result in hydrogen abstraction and formation of a surface-bound alkyl radical s·:



Here,  $k_i^S$ ,  $k_a^S$  &  $k_{\text{aOH}}^S$  are rate constants that are the surface equivalent of the respective  $k_i$ ,  $k_a$  and  $k_{\text{aOH}}$  in the bulk. It can be assumed that  $k_x^S$  has value of the same order of magnitude as the one of the respective  $k_x$  in the bulk (where “x” stands for i, a or aOH), provided that the same type of C-H bonds take part in the reaction – we present some arguments for that in S2. Once the hydrogen is abstracted from the surface site, s· is oxidized to form a polar site (peroxide or alcohol, sO<sub>2</sub>H or sOH):



All steps but the last one are surface analogues of a respective bulk reaction in Eq (4). In the last step, an oxidized molecule from the fuel film *adsorbs reversibly* to the surface polar site, resulting in the growth of the deposit and the regeneration of the hydrophobic site sH ( $\text{sO}_x\text{H} + \text{HO}_x\text{R} \leftrightarrow \text{sO}_x\text{H}---\text{HO}_x\text{R}$ , which is equivalent to sH). Note the difference between  $k_a^S$  (that refers to the reaction between  $\text{sH} + \text{RO}_2\cdot$ ) and  $k_{a2}^S$  (that refers to  $\text{sO}_2\cdot + \text{RH}$ ): different CH bonds may be involved in these two reactions. The whole process can be divided in three steps: surface initiation ( $\text{sH} \rightarrow \text{s}\cdot$ ), surface polar site formation ( $\text{s}\cdot \rightarrow \text{sO}_x\text{H}$ ) and the growth step  $\text{sO}_x\text{H} + \text{HO}_x\text{R} \rightarrow \text{sH}$ . The overall “deposit formation” reaction is  $\text{sH} + \text{O}_2 + \text{RO}_x\text{H} \rightarrow \text{sH}$ . A schematic of the process is given in Figure S4. An alternative of the last step in Eq (19) is *irreversible adsorption* to occur by a surface termination reaction, e.g.,  $\text{sO}_2\cdot + \text{RO}_2\cdot \rightarrow \text{sO}_2\text{R} + \text{O}_2$ , where  $\text{sO}_2\text{R}$  is again equivalent to sH. Note that in the case of reversible adsorption, in order the deposit to continue growing, one must assume that at certain stage during aging the reversibly adsorbed oxidation products react further to form irreversibly bound species.

A question that stands is the possibility for the exchange reactions  $\text{s}\cdot + \text{RH} \leftrightarrow \text{sH} + \text{R}\cdot$ ; unlike the respective bulk equivalent, the outcome of this process is not trivial. An analysis of the possible effect from it is presented in S2.

As the hydrogen abstraction is a very slow reaction, it can be assumed that the rate-determining process in the scheme (18)-(19) is the surface initiation (18). Under this

assumption, the rate of the overall process of addition of  $\text{RO}_x\text{H}$  to the surface is  $v_{\text{ads}} = v_i^S + v_a^S + v_{\text{aOH}}^S$ . Using Eqs (18)&(12), one obtains:

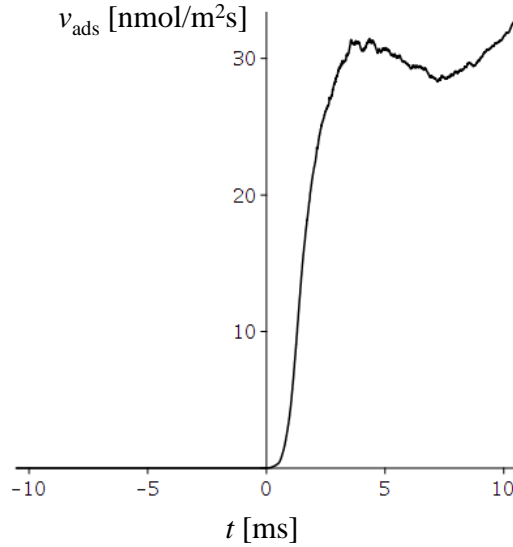
$$v_{\text{ads}} = \left\{ k_i^S [\text{NO}_2] + \left( k_a^S + \frac{k_{\text{aOH}}^S k_{\text{NO}}}{k_{\text{aOH}} [\text{RH}]} [\text{NO}] \right) [\text{RO}_2 \cdot] \right\} [\text{sH}]. \quad (20)$$

For alkanes that have several tertiary bonds, we can assume that  $k_x^S \approx k_x$  (both constants refer to the rate parameters of tertiary RH in Table S2). The same assumption can be made for the case of no tertiary atoms in the molecule (but with the rate parameters from Table S2 for secondary atoms). However, for isooctane (1 tertiary atom), the degradation products that adsorb, e.g., isooctanol, have hydrophobic chain that does not contain tertiary C-H bonds. In this case, the bulk abstraction constant  $k_{\text{aOH}}$  in Eq (20) refers to the tertiary bond of the isooctane, but the surface abstraction constants  $k_i^S$  &  $k_{\text{aOH}}^S$  should refer to its secondary bonds. Finally, for isooctane, the rate constant  $k_a^S$  should refer to a tertiary  $\text{RO}_2 \cdot$  radical (isooctylperoxy radical) attacking a secondary C-H at the deposit surface, cf. S2.

The concentrations  $[\text{NO}_2]$ ,  $[\text{NO}]$  and  $[\text{RO}_2 \cdot]$  in Eq (20) are those in Figure 2 & Figure 4. For  $[\text{sH}]$  we assume the value

$$[\text{sH}] = x_{\text{active}} r_W / N_A a_{\text{sH}}; \quad (21)$$

here  $r_W$  is the ratio between the actual area of the rough deposit surface and the projected area – known as the Wenzel factor in the colloid field [65], and is a measure of the surface roughness. We assume the value  $r_W = 10$  for it, typical for porous materials. For the *area per C-H bond*  $a_{\text{sH}}$  at the interface of the deposit, we assume a value similar to the one at the surface of an alkane – about  $10 \text{ \AA}^2$ . The quantity  $x_{\text{active}}$  stands for the fraction of reactive C-H bonds at the surface among all C-H bonds. For isooctane, the surface of the deposit is assumed to be covered by the tertiary isooctanol, which has 5  $\text{CH}_3$  groups and 1  $\text{CH}_2$  group; therefore, the fraction of the more reactive secondary C-H bonds is  $x_{\text{active}} = 2/17$ .  $N_A$  is Avogadro's number.



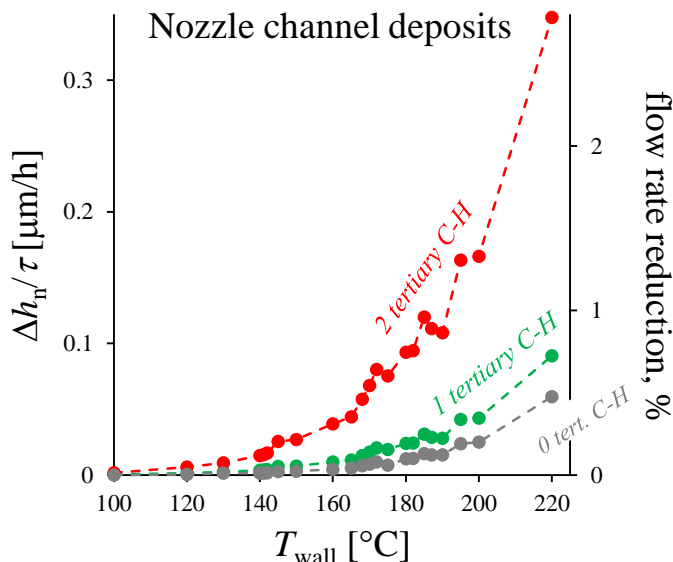
**Figure 6:** Momentary rate of deposit formation in the nozzle channel as function of time during compression and power strokes, according to Eq (20). Isooctane,  $T_{\text{wall}} = 160^\circ\text{C}$ .

The change of the adsorption rate during a cycle is calculated in **Figure 6**. For the considered case, the leading term in Eq (20) is the one proportional to  $[\text{NO}]$ . Unlike the tip deposits, we assume that the nozzle deposit accumulation continues after the point of boiling,

as it is unlikely that the fuel in the nozzle vaporizes completely at  $CAD_b$  (the nozzle is constantly fed by fresh leaked fuel). The accumulated deposit during a whole cycle is:

$$\Delta h_n = \frac{M_d}{\rho^D} \int_{t_0}^{t_{\text{end}}} v_{\text{ads}} dt, \quad (22)$$

where  $t_{\text{end}}$  denotes the end of the combustion stroke. Dividing  $\Delta h_n$  by  $\tau$ , we obtain the cycle-averaged rate of deposit formation in the nozzle channel. The result is illustrated in **Figure 7** (isooctane is in green).



**Figure 7:** Average rate of deposit formation via the surface oxidation-adsorption mechanism in the nozzle channel as a function of the injector wall temperature, according to Eq (22). The right ordinate axis corresponds to the flow reduction percentage due to the deposit, which is proportional to  $v_n$ , see Sec. 3.1.

We further considered the relation between nozzle channel deposit formation rate and the alkane structure, on the example of the same 3 alkanes analysed in Figure 5 (where their tip deposit propensity was investigated). We assume the following values of the relevant structural parameters in Eqs (20)-(22). For the least reactive 3-methyl-3-ethylpentane, the fraction of secondary bonds at the surface is  $x_{\text{active}} = 1/4$  and all rate constants in Eq (20) refer to secondary C-H bonds. The result for the rate  $\Delta h_n/\tau$  is the grey line in Figure 7. For the isooctane, the surface of the deposit is actually relatively passive, as the single ternary bond of  $i\text{-C}_8\text{H}_{18}$  is already oxidized and the surface oxidation process can be initiated only via the secondary C-H bonds. For this reason, with regard to the nozzle channel surface oxidation-adsorption mechanism, the isooctane is predicted to be of similar deposit propensity to that of the 3-methyl-3-ethyl pentane (compared to their rather different  $\Delta h_{\text{tip}}/\tau$  values in Figure 5). In contrast, a deposit made by 2,5-dimethylhexane degradation products grows significantly faster, as the surface has a fraction  $x_{\text{active}} = 1/17$  of tertiary bonds (note that for the values of  $\Delta h_n/\tau$  for 2,5-dimethylhexane in Figure 7, we added the initiation rate due to H-abstraction via the  $4/17$  fraction of secondary C-Hs as well, since it is not negligible).

Let us remark that the outcome of the surface oxidation is the transformation of the initial oxidation products (ROH, RO<sub>2</sub>H) to a bifunctional species at the interface deposit|fuel. This polyfunctionality means ability to polymerize [51] – and the aging processes definitely involve polymerization. This is the reason why the most dangerous alkanes in the fuel identified via the value of the deposition rate in the channel would contain at least two tertiary C-H bonds. In this



way of thoughts, alkanes that are able to react through intramolecular propagation mechanism will form polyfunctional products already in the bulk. The adsorption of such a product will immediately create a polar site (cf. Figure S4-right). For example, a likely product of the intramolecular oxidation is the alcohol-peroxide  $\text{HO}_2\text{ROH}$  [30,56]; it can adsorb at a polar surface site via  $\text{sOH} + \text{HO}_2\text{ROH} \leftrightarrow \text{sOH}\cdots\text{HO}_2\text{ROH} \sim \text{sOH}$ . In such case, the slow surface initiation step is skipped. Thus, alkanes containing the structural element  $\text{H-CR}^1\text{-CH}_2\text{-CR}^2\text{-H}$  can be expected to have higher propensity for deposit formation than those with isolated tertiary bonds.

Eq (22) involves several major approximations. The concentration of the oxidation products and  $\text{NO}_x$  in the fuel before  $\text{CAD}_b$  must be lower in the nozzle compared to the tip, due to the increased diffusion length; lower temperature can also be expected. In addition, leakage feeds the base of the nozzle with fresh cold fuel, diluting the reactive species. On the other hand, late in the cycle, as the leaked droplet boils and retreats to the nozzle hole, the reaction volume decreases significantly yielding the opposite effect – in the time interval between  $t_b$  and  $t_{\text{end}}$ , the concentration of  $[\text{RO}_2\cdot]$  in the nozzle channel is probably increasing. Exhaust and intake strokes may also contribute to the deposition in the channel [1]. The modelling of these effects requires better understanding of the leakage process, as well as of the deposition of oxidized products at the tip during boiling. We use Eqs (22) as an order of magnitude estimate, hoping that the above effects cancel each other.

### 2.3.3 Experimental determination of the rates of deposit formation and removal

The process of removal of the deposits [14,17] is largely unrelated to their formation, and is a matter of a different study, yet one has to account for it when dealing with the experimental data. Two different regimes should act for the deposit removal at the tip and in the nozzle. The deposit in the channel is removed mechanically, by the turbulent shear stress during each injection [42]. The deposit at the tip, on the other hand, is rather thick and leads to thermal insulation of the injector surface, and therefore, to increased wall temperatures (Sec. 3.2 below). At high temperature [66], and especially in the presence of certain catalysts [67], gasification of the deposit occurs. Probably, a number of other mechanisms are also operating [14], in particular, removal via flaking and cracking [13] is likely for the injector deposits.

Let us give an example of the effect of the removal rate on the deposition, limiting ourselves to a discussion on the empirical result of Aradi et al. [42] who showed that their experimental data for the decrease of the fuel discharge through the nozzle agree with the following rate law:

$$\frac{dh_n}{dt} = v_n - k_r h_n; \quad (23)$$

here,  $v_n$  is the rate of deposit formation and  $k_r h_n$  is the rate of deposit removal. Both  $v_n$  and  $k_r$  are empirical quantities in the model of Aradi et al. Our surface oxidation-adsorption model in Sec. 2.3.2 indeed predicts that the rate of formation is independent of  $h_n$ , thus confirming the hypothesis of Aradi et al., and we can calculate  $v_n$  as

$$v_n = \Delta h_n / \tau, \quad (24)$$

where  $\Delta h_n$  is the increment of the deposit thickness per cycle due to the surface oxidation, Eq (22), and  $\tau$  is the period of the engine cycle. The solution to Eq (23) for  $h_n(t)$  (under the assumption that  $v_n$  is constant) reads:

$$h_n = \frac{v_n}{k_r} (1 - e^{-k_r t}). \quad (25)$$



In order to compare the experimental results from Ref. [42] with our calculated deposit formation rates, we re-evaluated all data of Aradi et al. in Table S3 in S4 (we had to correct a small mistake in the regression data in *table 5* of [42], as explain in S4). The value of the nozzle radius is required for the determination of the absolute value of  $v_n$ ; such was not provided in [42], therefore, we assumed  $R_n = 50 \mu\text{m}$  (as for the real engine we are modelling). Aradi et al. studied the effect of the fuel formulation on  $k_r$  &  $v_n$  at  $T_{\text{wall}} = 173^\circ\text{C}$ . The order of magnitude of  $v_n$  that follows from their data is in the range 0.6-1.6  $\mu\text{m/h}$  for non-additized fuels (cf. S4). The lowest rate, 0.6  $\mu\text{m/h}$ , refers to fuel of low alkene content and it is about 6 times larger than our theoretical estimate in Figure 7 for the most reactive alkane. The fuel of 12.9% alkene content has formation rate of  $v_n = 1.6 \mu\text{m/h}$ . The third fuel containing 19.9% alkene and 153 ppm S-compounds is more stable ( $v_n = 0.9 \mu\text{m/h}$ ) – the reasonable explanation for this is the well-known antioxidant effect of the sulfur compounds in this concentration range [68]. As for the removal rate constant  $k_r$ , for non-additized fuel its value is 0.1-0.6  $\text{h}^{-1}$ .

### 3 Effect of the deposit on the engine performance

The investigations of the effect of the injector deposits on the engine performance are not many [6,12,69-71] As a result, the mechanism of their adverse action is not completely understood. The best studied effect of the nozzle channel deposits seems to be the restricted fuel flow through the nozzle [6,12], which we consider briefly in Sec. 3.1. In Sec. 3.2, we investigate an effect of the tip deposits that can be readily analysed theoretically: the alteration of the injector wall temperature by the deposit layer.

#### 3.1 Nozzle channel deposits and channel plugging

The deposits alter the cross-section of the nozzle channel and lead to decreased discharge. The Reynolds number of the nozzle flow is of the order of  $Re \sim 10000-20000$ ; in this range, the Bernoulli law can be used in the form [72]:

$$Q = C_d \pi (R_n - h_n)^2 \sqrt{2\Delta p / \rho^F}. \quad (26)$$

Here,  $R_n$  is the nozzle radius in the absence of deposits,  $\Delta p$  is the injection pressure,  $\rho^F$  is the density of the fuel, and  $C_d$  is the discharge coefficient, which is approximately equal to the ratio between the smallest cross-section of the nozzle channel and the *vena contracta* area of the flow. In general,  $C_d$  depends on both the channel geometry and the mean roughness  $\varepsilon$  of the wall. The nozzle channel deposit affects both  $R_n$  and  $\varepsilon$ , probably with non-monotonous combined effect on  $Q$ .

Aradi et al. [42] proposed the use of the reduction of the flow rate  $1 - Q/Q_0$  as a measure of the deposit thickness. Indeed, in case that  $h_n \ll R_n$ , a linear relationship holds between the two quantities. The linear formula can be derived by expanding Eq (26) into series at  $h_n \ll R_n$ . The result is:

$$1 - \frac{Q}{Q_0} = \left( \frac{2}{R_n} + \frac{\partial \ln C_d}{\partial R_n} - \frac{\partial \ln C_d}{\partial \varepsilon} \frac{d\varepsilon}{dh_n} \right) h_n \approx \frac{2h_n}{R_n}. \quad (27)$$

The factor  $2/R_n$  is related to the proportionality of  $Q$  to  $(R_n - h_n)^2$  for the turbulent flow, see Eq (26). The dependence of  $C_d$  on  $h_n$  is unclear: according to Colebrook-White equation [73], the

derivative  $\partial \ln C_d / \partial R_n \approx 0.5/R_n$ , but using the correlation of Shapiro et al. [74,72], it is  $0.05-0.1/R_n$ , cf. S4. As for the  $\varepsilon$ -term in Eq (27), the roughness will decrease dramatically as the first deposits grow inside the grooves of the steel wall, but once they are homogeneous, the deposit|fuel interface can be expected to be of relatively constant roughness so  $d\varepsilon/dh_n \approx 0$ . Curiously, from here it follows that a brand new injector could require certain time for deposits to accumulate in the grooves before normal operation is achieved. Neglecting the last two terms in Eq (27), i.e. assuming that  $Q \propto (R_n - h_n)^2$  as Aradi et al. did [42,75], we obtain the approximate  $1 - Q/Q_0 \approx 2h_n/R_n$ .

The substitution of Eq (25) for  $h_n(t)$  in Eq (27) yields the reduction of the discharge rate as function of  $t$  due to the accumulation of the deposits. For its limit at large times ( $k_r t \gg 1$ ), one obtains:

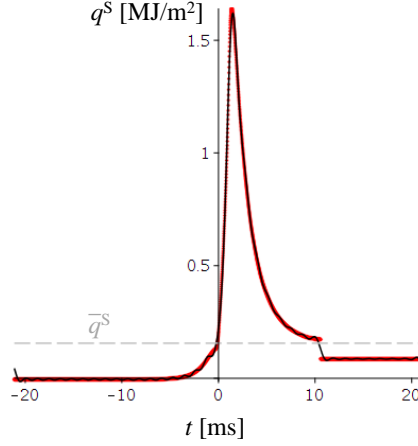
$$1 - \frac{Q}{Q_0} = \frac{2v_n}{R_n k_r} (1 - e^{-k_r t}) \xrightarrow{t \gg 1/k_r} \frac{2v_n}{R_n k_r} . \quad (28)$$

Thus, the reduction of the flow rate at  $t \gg 1/k_r$  is proportional to  $v_n/k_r$ . Assuming further that  $k_r \approx 0.5 \text{ h}^{-1}$  (see Table S3) independently of the temperature, we can draw the reduction of the flow rate as function of the wall temperature using the results for  $v_n$  from Sec. 2.3.2. According to Eq (28),  $1 - Q/Q_0 \propto v_n$ , therefore, we can use the second ordinate axis placed on the right side of Figure 7 to draw the result. The trend compares qualitatively well with the measured reduction in *fig. 3* of Kinoshita et al. [5]. As in the case of the data of Aradi et al., our calculated rates for alkanes are several times smaller than the experimental ones from [5]. This is unsurprising: real fuels were used in both Refs. [5,42], that contain HC species more reactive than alkanes.

## 3.2 Injector tip deposits and wall temperature

Nozzle temperature is a major factor for the deposition process [5,6], as discussed already in Sec. 2.1.2, 2.3.1 & 2.3.2. It is correlated with the inlet air and fuel temperatures, engine speed and load [12], but another major factor is the thickness of the deposit layer at the wall (compare to other engine deposits, e.g. [76]). The *average* temperature of the injector surface increases as the tip deposits accumulate and insulate the injector. Another very significant effect, which, to our knowledge, has not been considered in the literature, is that the deposit insulation leads also to a drastic increase of the temperature variations during each cycle.

Let a deposit layer of thickness  $h_{\text{tip}}$  exist between the hot combustion gases and a metal layer of thickness  $h^M$ ; the outer wall of the metal is fixed to a temperature  $T_{\text{out}}$ . The interface metal|deposit is located at  $z = 0$ , and the deposit|air is at  $z = h_{\text{tip}}$ . The interface deposit|air is subject to a time dependent heat flux  $q^S(t)$ . This heat flux from the chamber to the injector wall is an output of the SRM Engine Suite software (based on Woschni's correlation [77]). The dependence of  $q^S$  on time is illustrated in **Figure 8**; it is a periodic function of period  $\tau$  (twice the reciprocal rpm). The values of  $q^S(t)$  during the exhaust and the intake strokes are estimated roughly: it is assumed that  $q^S(t) = q^S(-180 \text{ CAD})$  from  $-360$  to  $-180 \text{ CAD}$ , and  $q^S(t) = q^S(180 \text{ CAD})/2$  from  $+180$  to  $+360 \text{ CAD}$  (the precise profile in this range of CA degrees has little effect on the final results for the wall temperature).



**Figure 8:** Heat flux from the cylinder charge to the injector wall during a cycle as a function of time. Red: simulation data; black– the Fourier series (29),  $N = 36$ . Grey – the average flux  $\bar{q}^S$ , Eq (30).

The surface temperature that corresponds to  $q^S(t)$  in Figure 8 can be found using the Fourier series technique [78,77]. The Fourier series of  $q^S$  reads

$$q^S(t) = \bar{q}^S + \sum_{n=1}^N q_{c,n}^S \cos n\omega t + \sum_{n=1}^N q_{s,n}^S \sin n\omega t, \quad (29)$$

where

$$\bar{q}^S = \frac{1}{\tau} \int_{-\tau/2}^{\tau/2} q^S dt, \quad q_{c,n}^S = \frac{2}{\tau} \int_{-\tau/2}^{\tau/2} q^S \cos n\omega t dt, \quad \text{and} \quad q_{s,n}^S = \frac{2}{\tau} \int_{-\tau/2}^{\tau/2} q^S \sin n\omega t dt \quad (30)$$

are the Fourier coefficients of  $q^S(t)$ . The angular frequency  $\omega$  is related to the period as  $\omega = 2\pi/\tau$ . As it follows from Eq (30), the coefficient  $\bar{q}^S$  is precisely the average heat flux to the wall (0.156 MW/m<sup>2</sup> for the data in Figure 8).

We seek for the evolution of the temperature profile,  $T(z,t)$ , in the deposit and in the metal during the cycle. It is the solution to the one-dimensional heat transfer equation  $\partial T/\partial t = \chi \partial^2 T/\partial z^2$  for the two layers, subject to boundary conditions **(i)**  $T^M|_{z=-h^M} = T_{\text{out}}$ , **(ii)**  $\kappa^D \partial T^D/\partial z|_{z=h_{\text{tip}}} = q^S(t)$ , and **(iii-iv)** continuity of  $T$  and the heat flux at  $z = 0$ . Here,  $\chi$  is the temperature diffusivity of the metal or the deposit, related to the heat conductivity  $\kappa$  as  $\chi = \kappa/c$ , where  $c$  is the heat capacity per unit volume of the metal or the deposit. The solution to this problem is derived in S5. For the temperature in the deposit, it reads:

$$T^D = \bar{T}^D(z) + \sum_{n=1}^N T_{c,n}^D(z) \cos n\omega t + \sum_{n=1}^N T_{s,n}^D(z) \sin n\omega t, \quad (31)$$

and the expression for  $T^M$  the metal phase is similar. Here, the  $z$ -dependent  $T$ ,  $T_{c,n}$  and  $T_{s,n}$  are the Fourier coefficient of the temperature, that are simply related to the respective coefficients (30) of  $q^S(t)$ , cf. S5. In particular, for  $T$  it is valid that:

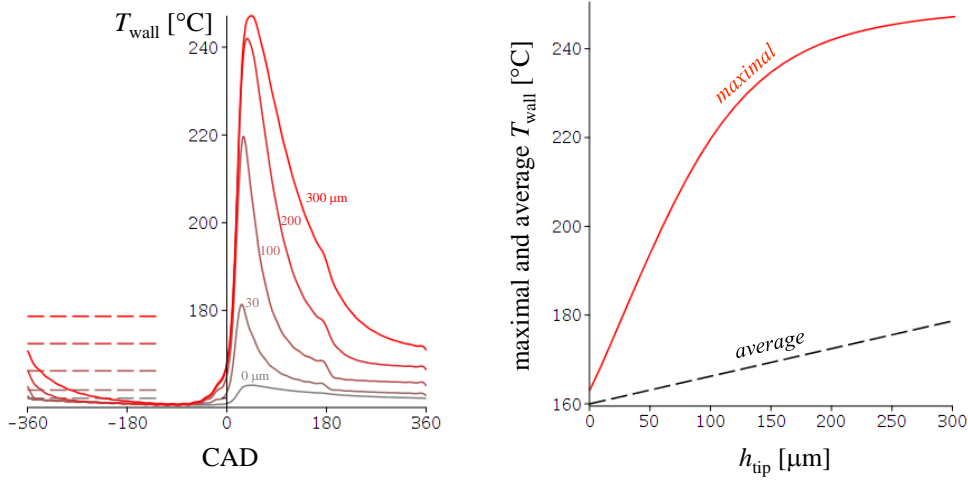
$$\bar{T}^M = T_{\text{out}} + \frac{\bar{q}^S}{\kappa^M} (z + h^M) \quad \text{and} \quad \bar{T}^D = \bar{T}_{\text{wall}} + \frac{\bar{q}^S}{\kappa^D} (z - h_{\text{tip}}), \quad (32)$$

where  $T_{\text{wall}}$  is the average wall temperature, given by the expression

$$\bar{T}_{\text{wall}} = T_{\text{out}} + \frac{h^M}{\kappa^M} \bar{q}^S + \frac{h_{\text{tip}}}{\kappa^D} \bar{q}^S. \quad (33)$$

By definition, the 0<sup>th</sup> Fourier coefficients  $T^M$  &  $T^D$  given by Eqs (32)-(33) set the time-averaged profile of the temperature. Assuming that  $\bar{q}^S$  is not strongly dependent on the injector wall

temperature, we can use Eq (33) to predict immediately the effect of the deposit layer on the wall temperature: it increases it with  $\Delta T_{\text{wall}} = h_{\text{tip}} \bar{q}^S / \kappa^D$ . Using the values  $\kappa^D = 2.5 \text{ W/Km}$  [76] and  $\bar{q}^S = 0.156 \text{ MW/m}^2$ , we obtain an increase of the surface temperature of  $\bar{q}^S / \kappa^D = 6.2 \text{ K}$  per  $100 \mu\text{m}$  deposit.



**Figure 9:** *Left* – wall temperature in the presence of deposit during a cycle at various values of  $h_{\text{tip}}$ . The dashed lines indicate the respective  $T_{\text{wall}}$ . *Right:* dependence of the average (black dash) and the maximal wall temperature (red solid) on the thickness of the tip deposit.

The time-dependent terms in Eq (31) do not contribute to the average  $T$ . They allow, however, the evolution of the temperature profile during a cycle to be calculated. The whole space profile of  $T^D$  &  $T^M$  is discussed in S5. Setting  $z = h_{\text{tip}}$  into Eq (31), we obtain the time evolution of  $T_{\text{wall}}$ . It is plotted in **Figure 9-left** for several values of the thickness  $h_{\text{tip}}$ , using the following parameter values: average temperature of the metal surface  $160 \pm 2^\circ\text{C}$ ;  $\chi^D = 11.6 \times 10^{-6} \text{ m}^2/\text{s}$  (assuming heat capacity as for coke);  $\kappa^M = 54 \text{ W/Km}$  and  $\chi^M = 15.3 \times 10^{-6} \text{ m}^2/\text{s}$  as for iron [77]. As seen in the figure, in the absence of deposit, the wall temperature does not change significantly with time ( $T_{\text{wall}} = 160 \pm 2^\circ\text{C}$ , grey line). A relatively thin tip deposit of thickness  $30 \mu\text{m}$  increases the average temperature by less than  $2^\circ\text{C}$ . However, the amplitude of the oscillations around the average increases significantly – the maximal temperature reaches  $181^\circ\text{C}$ , which is about  $20^\circ\text{C}$  increase compared to the one of the neat injector wall. The maximal temperature continues to increase about linearly with  $h_{\text{tip}}$ , until deposit of thickness of the order of  $150\text{-}200 \mu\text{m}$  is accumulated (**Figure 9-right**). After this, a plateau is reached, corresponding to the characteristic amplitude ( $\approx \pm 40^\circ\text{C}$ ) of the oscillations of  $T_{\text{wall}}$  at the surface of a thick deposit, where “thick” means  $h_{\text{tip}} \sim 2\chi^D/\omega \approx 400 \mu\text{m}$ .

The predicted high peak of the temperature of the injector during a cycle in the presence of deposit has numerous consequences. One is that the peak temperature is high enough for gasification of the deposit to occur [67,66], suggesting a probable removal mechanism. The temperature oscillations also complicate the modelling of the process of formation of deposits. In Sec. 2.1.2 & 2.3.1, we worked under the assumption that  $T_{\text{wall}}$  is constant during the cycle. According to Figure 9, this is a reasonable approximation only in case that the surface is fresh and no more than  $5\text{-}10 \mu\text{m}$  of deposit film is accumulated – i.e. the results for  $\Delta h_{\text{tip}}/\tau$  are valid only for the initial stages of the deposition process. Once enough deposit has been accumulated, the temperature peaks may result into serious acceleration of the deposition process at the tip of the injector. At the surface of a thick deposit, the boiling range will also change dramatically compared to the one in Figure 1. The analysis of this more complicated situation is left for another study.

## 4 Discussion

We presented a model of the fuel degradation process under engine conditions, and a model of the formation of external injector deposits. The medium in which the process of deposit formation takes place is identified as the fuel drop leaking out of the nozzle after each injection (Sec. 2.1.2). The initiator of the radical chain in the liquid fuel is identified as  $\text{NO}_2$  produced in the combustion gases (Sec. 2.1.3), in agreement with the hypothesis of many researchers for the similar process of lubricant film degradation in the cylinder [45-49]. In addition, we identified one branching reaction by which  $\text{NO}$  contributes to the liquid phase oxidation:  $\text{RO}_2 \cdot + \cdot\text{NO} \rightarrow \text{RO} \cdot + \cdot\text{NO}_2$  [50,31].

The variations in the temperature and the composition of the leaked droplet are predicted. Two interesting features are found. First, as the pressure in the cylinder decreases during the power stroke, the fuel droplet reaches its boiling temperature and vaporizes, retreating simultaneously to the nozzle hole, Sec. 2.1.2. This is the probable trigger of the precipitation of deposits at the tip of the injector. Second, a cyclic accumulation regime of oxidation holds: the time between the formation and the removal of the leaked droplet is very short (few ms), which is not enough for the peroxide radicals to reach their stationary concentration (15). Due to the branching reaction with  $\text{NO}$  and the slow termination rate, the overall rate of the oxidation process is very different from the one in the classical studies of oxidation under laboratory conditions [30,31,53].

We formulate two mechanisms for the deposition of the oxidation products formed in the leaked droplet. The first one acts at the tip of the injector (Sec. 2.3.1), and involves cycles of **(i)** convective *re-suspension* (due to the injection and thermal Marangoni flow) of the deposit particles that precipitated in the previous cycle; **(ii)** *filtration* – the suspended particles filter the fuel by adsorbing the oxidized products; **(iii)** *precipitation* of the particles triggered by the boiling (perhaps following the coffee ring mechanism).

The accumulation of particles inside the nozzle channel is unlikely, as each injection will sweep them away completely. Therefore, we formulated a second mechanism for the formation of the nozzle channel deposits (Sec. 2.3.2), involving **(i)** *direct oxidation of the interface* polar deposit|fuel, with formation of polar sites at the surface, and **(ii)** *adsorption* of degradation products from the film at these polar sites.

In the absence of suitable quantitative data, the main criteria for validity of these mechanisms are the self-consistency and the agreement with the qualitative observations from the literature. The two mechanisms provide explanation of a number of known experimental facts: **(i)** the role of the distillation characteristics of the fuel for the deposition process [5] (through their direct relation to the point of boiling, Figure 1); **(ii)** the role of the injector wall temperature [42] (which controls the rate of the fuel droplet degradation); **(iii)** we obtain reasonable order of magnitude of the rates of formation (Sec. 2.3.3), and **(iv)** correct trend of the rate of formation as a function of the wall temperature (compare Figure 7 and Ref. [5]); **(v)** why certain thermally stable HC components in the fuel result in worse deposit problem (Sec. 2.3.1&2.3.2). We should add here that **(vi)** the degradation mechanism provides the correct order of magnitude of the oxygen concentration in the young deposit – each molecule in the deposit contains 1-2 oxygen atoms, which is in agreement with the high O-content found in young deposits (10-20 w% [3]).

The mechanisms also allows one to understand why are various anti-deposit measures effective: why the additives used to fight with the tip deposits have the functionality of dispersants [19,67,63]; why are antioxidants added to the fuel [19]; why reducing roughness is important [6] (cf. Eq (21)). A decrease of the residual fuel that leaks out of the injector after the

injection is a working strategy against deposits [6]: valve-covered orifices have been used to disallow fuel to escape injectors after the injector event ends. A stepwise increase of the diameter of the hole in the end of the channel helps avoiding deposits [79] – this can be explained with the altered conditions of the leakage and with the hindered diffusion of the dangerous gas-phase species towards the liquid film in the narrow part of the channel. Similarly, there are designs where aluminium caps are protecting the nozzle tip from combustion gases [80,81]. The mechanism explains why anti-deposit coatings only delay the onset of injector deposits [6] – most of the growth process occurs at the deposit|fuel interface, and once the injector surface is covered by even a very thin deposit layer, the surface chemistry of the injector itself becomes irrelevant for the process.

We present also models of some of the adverse effects the deposits have on engine's performance. First, the nozzle channel deposits lead to plugging of the nozzle channel [6,12]. The relation between the reduction of the flow rate and the deposit thickness is approximately linear, with slope equal to  $2/R_n$ , Eq (27). This result allows data for the reduction to be used for the calculation of the absolute value of the deposit thickness, Sec. 3.1. To our knowledge, these data were used only for qualitative conclusions previously. Second, we investigated the effect of the injector tip deposits on the injector wall temperature, Sec. 3.2. Due to the heat insulation of the wall, the temperature of the injector surface increases with the deposit thickness. Our analysis shows that this effect is not prominent, Figure 9-*right*. The deposits have, however, a very strong amplifying effect on the temperature oscillations during a cycle. Thus, if the temperature at the neat metal surface oscillates within a range of 4 K, a deposit of thickness 200  $\mu\text{m}$  will increase this range to 80 K, Figure 9-*left*.

Due to the complexity of the system, our modelling involves by necessity a long list of approximations. Many of the relevant phenomena are modelled only roughly, and others are completely neglected. Let us give a brief summary of the main approximations, outlining meanwhile our plans for future work. The transfer of NO and NO<sub>2</sub> to the film is modelled only roughly, using the empirical pair mixing fraction  $\xi$  [44]. In view of the complicated boundary conditions of the turbulent mass transfer process, we are pessimistic regarding the advance of a more realistic approach. The evolution of the volume of the fuel droplet is nearly neglected (we model it as a stepwise function of time); a better model would require reliable experimental leakage data. In several points of the model, the fuel is assumed to behave as a single component alkane. In particular, we neglect the detailed distillation curve and the related enrichment with less volatile components during boiling [43,17]. A model involving a mixture will lead to qualitatively new characteristics of the process, e.g., instead of point of boiling, the leaked droplet will pass through a boiling stage that would continue for few ms, during which fuel degrades. Next, we neglected completely the role of the lubricant. The tip deposits may contain 10-50% lubricant-derived ash [6,23]; lubricant elements were found even deep inside the nozzle channel [12,23]. This ash is dispersed inside the characteristic sticky organic porous matrix (the “*oxygen skeleton*” [82]) produced by the fuel degradation and certainly plays an important role – at the very least, it reinforces the deposit, making it hard. We also neglect completely the natural polar components and the polar additives that all fuels contain; we intend to consider this question in a separate study. The role of the fuel blends is far more complicated, since these blends are usually polar components (e.g., ethanol for gasoline, esters in biodiesel) that change drastically the conditions of the liquid phase oxidation (fuel solvent ability, in particular). Next, once the leaked droplet boils away, we consider no details about the further evolution of the non-volatile residue; a related question – we do not consider the removal rate, apart from the empirical  $k_r h_n$  term in Eq (23). The mechanism by which the next droplet re-suspends the deposit is not considered. It is likely that each next fuel droplet dribbling out of the nozzle dissolves some material deposited by the previous droplet, which we neglect, i.e. we assume

that the deposition is irreversible. With regard to the nozzle channel deposits, the crudest approximation we use is for the transport of mass and heat from the tip droplet to the nozzle channel (cf. Ref. [1]). The oxidation mechanism is simplified; for example, at these levels, the nitrogen oxides in the quench layer can participate in other interesting reactions [31] – unfortunately, we do not dispose of the values of the respective rate parameters. Additionally, in order to consider real fuels, we need to add in our model the possibility for intramolecular propagation, alkene and alkylarene oxidation, bulk formation of polyfunctional degradation products and mechanisms of their adsorption and polymerization. Metal catalysis is probably also a factor [6].

With regard to the effects of the deposits on the engine performance, many possibilities to make our models in Sec. 3 more realistic exist. For example, one can consider how the turbulent shear affects the nozzle channel deposits, which can result in a primitive model of the  $k_t$  parameter in Eq (23). Another question of importance is, how the evaporating fuel film affects the heat transfer through the wall? The fuel wets the deposit, changing its heat transfer parameters, and it also consumes heat during evaporation.

Another interesting question is, how the engine operating conditions affect the deposition process? Our SRM engine model allows the pressure profile, the profile of the heat flux to the wall and respectively – the wall temperature to be simulated at various engine loads, and their effect on the deposition rate can be followed. This is not straightforward to do, however, as one must deal with the dependence of the  $\xi$ -parameter and the leaked droplet volume on the speed of the engine. In the same line of thoughts, it is known that the oxidation processes, the adsorption of gases etc. continue long after the deposit is formed, even after the engine is switched off (e.g. *sec. 5.2* in Ref. [63]). It is also known that the trapped residue contributes to the deposition process [77] – currently, our residue model is simplified (cf. S1).

The model we developed can be transferred to several interesting similar problems. For example, it has been found that liquid phase oxidation occurs in the spray droplets at a rate that is several orders of magnitude higher than the oxidation of bulk fuel [83], probably again under the action of  $\text{NO}_x$ . It seems possible that a solid residue can be left after the spray droplets boil, which can contribute to soot formation and HC emissions. Our model can be used to investigate this problem with only minor modifications. The degradation of the impinged fuel film at the piston [43,44] should also follow a similar mechanism.

Finally, let us mention that we considered neither the formation of the seat and needle ball deposits nor their effect on the HC emissions. The reason is that the data for these deposits is scarce [6]. We believe that the seat and ball deposits are responsible, at least in part, for these HC emissions. The obvious effect from them is worse sealing – roughly, if the seal has thickness  $h_s$ , the presence of the sparsely distributed deposits observed in Ref. [6] of certain thickness  $h_{\text{seat}}$  would result in the increase of the seal thickness to  $\sim h_s + 2h_{\text{seat}}$ , leading to an increased leakage rate (proportionally to  $(h_s + 2h_{\text{seat}})^3$  [84]). Indeed, increased leakage has been observed recently with fouled injectors [7]. Leakage is a major contributor to the HC emissions. If its rate is 1 g per kg fuel [39], then at least  $\frac{1}{4}$  of the leaked fuel will be released directly in the exhaust. For the data in Table 2, this corresponds to  $0.4 \text{ g HC emissions per } 23.8+1.6 = 25.4 \text{ kg mixture}$ , or 16 wppm, which is significant (typically, HC emissions are of the order of 50 wppm). The increase of the leakage with few percent due to the injector deposits will contribute to the HC emissions an amount similar to the observed one. In diesel engines, the impinged fuel film due to the adverse effect of the deposit on the spray characteristics is another source of HC emission.



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## Supplementary information

### S1. Engine parameters and cylinder conditions

In this supplement, we are giving additional details about the engine model used for the SRM simulations. All the characteristics that are not provided here or in the text are unchanged compared to the default DISI case in SRM Engine Suite (such as spark characteristics, heat transfer model, friction model and others), described in Refs. [37,44]. In addition to the data in Table 1, the following basic characteristics of the cylinder have been used (set to those in the real test engine we model): bore = 79 mm; stroke = 81.4 mm; manifold intake pressure = 70 kPa; exhaust port pressure = 126 kPa. All simulations involved 240 bulk cylinder stochastic particles and 20 quench layer stochastic particles.

The injection event has little effect on the outcome of the simulation due to the early injection strategy chosen with the real engine we are modelling. In the real engine, the injection event occurs during the intake stroke, at -311 CAD, while inlet valve is still opened. Presumably, at the time of the inlet valve closure, the fuel is already atomized completely. Under the early injection strategy, the precise timing of the injection is unimportant for most engine characteristics. For simplicity, we simulate only the closed-volume part of the cycle, i.e. the compression and power strokes, and set the injection event between -180 and -150 CAD, as well as set the characteristic turbulent mixing time at a relatively small value (1 ms). This guarantees that the mixture is well-mixed long before TDC, without significant compositional stratification, and ensures independence of all relevant simulated quantities on the injection characteristics. The inlet valve closure and exhaust valve opening are assumed to occur at -180 and +180 CAD, respectively.

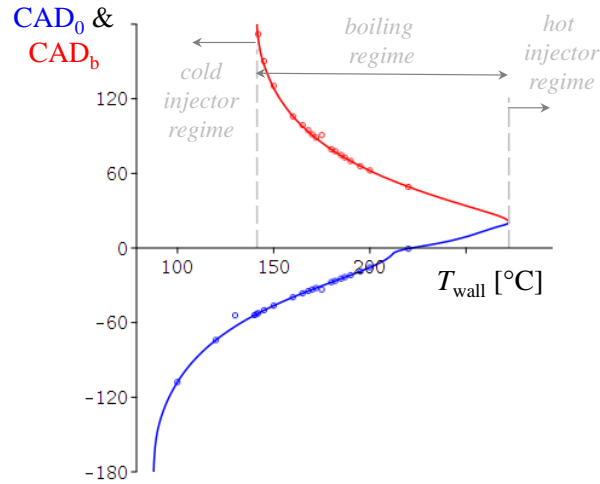
An important feature of the test engine is that, as most gasoline engines, it operates with a substantial amount of residue charge. The amount of the residue was calculated by solving an integral mass balance, using the known characteristics of the real engine, namely, the air & fuel consumption of the engine; the manifold intake pressure and temperature (37°C – which is assumed to be the air temperature before mixing with the hot exhaust); the exhaust manifold pressure and temperature (assumed equal to those of the trapped residue before mixing it with the cold air). When writing the mass balance, we also took into account that the evaporated fuel contributes to the pressure of the cylinder charge. The exhaust in our simulation has 5 components: N<sub>2</sub>, H<sub>2</sub>O, CO<sub>2</sub>, CO and NO – these were the components of highest concentration in the exhaust obtained in a preliminary simulation performed without trapped residue being accounted for. These data allowed us to calculate the composition of the cylinder charge at the start of the simulation, given in **Table S1**.

**Table S1:** Composition of the initial charge.

component	w%
N <sub>2</sub>	76.656
O <sub>2</sub>	21.603
CO <sub>2</sub>	1.121
H <sub>2</sub> O	0.576
CO	0.038
NO	0.006

An important consequence of the presence of trapped residue is the increased temperature of the charge upon inlet valve closure. It was calculated approximately, by assuming that the mixing between the fresh charge and the trapped residue is adiabatic. The result was 82.2°C. Many results of the simulation (pressure profile, deposition rates) were found to have a non-negligible dependence on both the residue components amount and the initial temperature.

We will now present some of the simulation results of secondary importance. In **Figure S1**, the simulated values of  $CAD_0$  and  $CAD_b$  are shown as function of the wall temperature. As seen, they follow closely the average dependence of the boiling temperature vs. CAD (the small variations are due to the stochastic nature of our simulations). The possible regimes of accumulation of the leaked fuel are delineated with the grey dash lines (cf. Sec. 2.1.2).

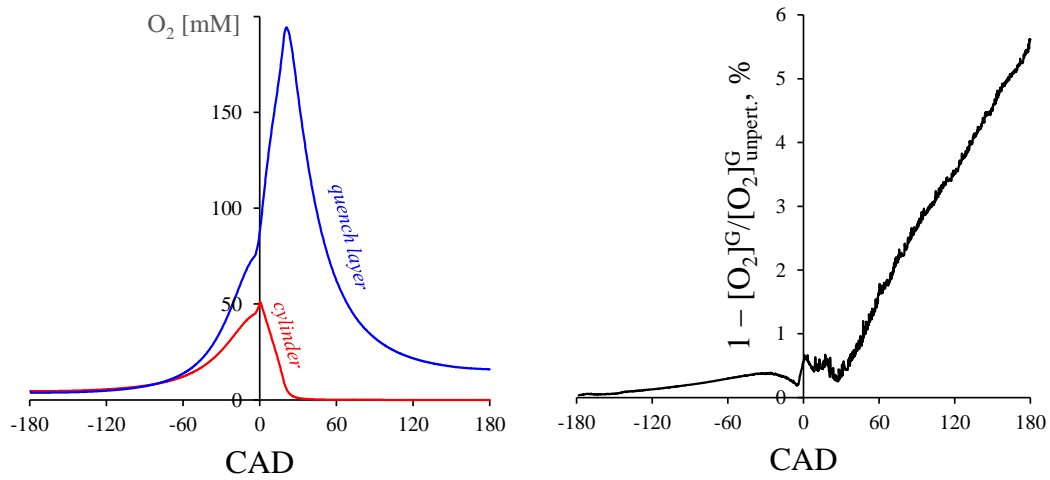


**Figure S1:** Points of boiling and precipitation as function of the injector wall temperature. The points are the results of full simulations; the curve is the rotated boiling temperature curve in Figure 1-right at 160°C.

In **Figure S2**, the evolution of the oxygen concentration in the quench layer is illustrated. The quench layer is at temperature fixed to  $T_{wall}$  (160°C for the example). The oxygen has little time to escape during the power stroke ( $\sim 5$  ms), i.e. the molar part of  $O_2$  in the quench layer does not change significantly. However, cylinder pressure increases and compresses the quench layer, leading to significant increase of  $[O_2]^G$  there, Figure S2-left. In Figure S2-right, we calculate the reduction of the amount of  $O_2$  in the quench layer during a cycle in comparison with the theoretical  $O_2$  concentration *unperturbed* by diffusion,  $[O_2]_{unpert.}^G$ , given by  $x_{O_2}(CAD = -180^\circ) \times p/RT_{wall}$ , where  $x_{O_2}(CAD = -180^\circ)$  is the initial value of the molar part of the oxygen. During the compression stroke, there is little change of the quench layer composition as quench layer and cylinder charge have similar fractions of  $O_2$ . During the power stroke, the oxygen in the cylinder is depleted (Figure S2-left), and diffusion from the quench layer to the bulk starts. For the few milliseconds until the exhaust valve opens, about 6% of the present  $O_2$  leaves the quench layer. As the time for a stroke is 10.6 ms, one can estimate that the time needed for half of the oxygen to leave the quench layer is of the order of 100 ms (which is obviously related to the chosen value of the empirical parameter  $\xi$ , cf. Sec. 2.1.3). We assume that, during the exhaust and the intake stroke where gas velocity in the bulk is very large, the quench layer is substituted with a fresh gas. Probably, this is not completely fulfilled in reality.

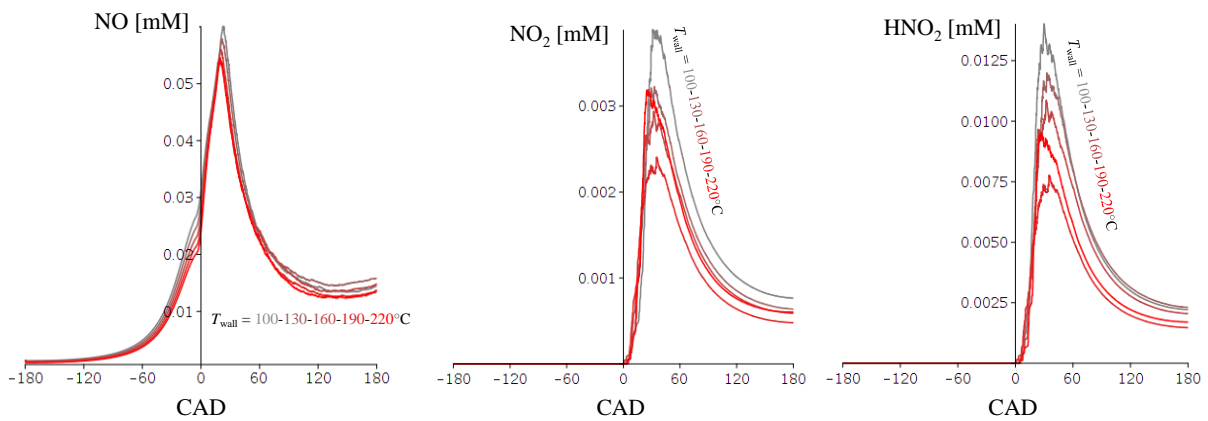
Let us mention that the precise concentration of the oxygen in the quench layer or in the film is irrelevant for the rate of deposition (which is valid also for most classical cases of liquid phase oxidation rates [30,31,53]). Under exceptional conditions (very low  $O_2$  concentration where depletion effects can be observed, or very high concentration where the reaction  $RH +$

$O_2 \rightarrow R\cdot + HO_2\cdot$  contributes to the initiation rate),  $[O_2]$  in the quench layer must also be monitored. For the considered study case, the exact value of  $[O_2]$  is of little importance.



**Figure S2-left:** Concentration of  $O_2$  in the cylinder and in the quench layer as a function of CAD. **Right:** reduction of the fraction of  $O_2$  in the quench layer during a cycle due to the transport toward the bulk. About 6% of the oxygen escapes the quench layer for the time of the power stroke.

In **Figure S3**, the evolution of three major N-containing components ( $NO$ ,  $NO_2$  and  $HNO_2$ ) of the quench layer is illustrated at several values of  $T_{wall}$ . The concentration of these species decrease with  $T_{wall}$  due to the ideal gas law (concentration  $\propto 1/T_{wall}$ ). Only at high wall temperatures (above  $190^\circ C$ ), the concentration of  $NO_2$  and  $HNO_2$  increases as  $NO$  reacts faster with the oxygen in the quench layer.



**Figure S3:** Concentration of  $NO$ ,  $NO_2$  and  $HNO_2$  in the quench layer at several values of  $T_{wall}$ .

## S2. Rate parameters of the liquid phase oxidation

All Arrhenius rate parameters used in this work are summarized in Table S2.

**Table S2:** Bulk phase oxidation – rate parameters (per active site).

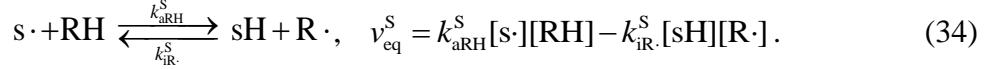
Reaction	Rate parameters	References
<b>Radical oxidation</b>		
$R_2CH\cdot + O_2 \rightarrow R_2CHO_2\cdot$ , alkane phase, 298 K	$k_o = 1.7 \times 10^9$ 1/sM, $E_o \approx 0$	<sup>(a)</sup> [31/p.67, table 2.4]
$R_3C\cdot + O_2 \rightarrow R_3CO_2\cdot$ , cyclohexane phase, 300 K	$k_o = 4.9 \times 10^9$ 1/sM, $E_o \approx 0$	[31/p.67, table 2.4]
<b>RO<sub>2</sub>· propagation</b>		
$RO_2\cdot + R_3CH \rightarrow RO_2H + R_3C\cdot$	$k_{a0} = 1.58 \times 10^9$ 1/sM, $E_a = 66.7$ kJ/mol	[30/p.34]
$RO_2\cdot + R_2CH_2 \rightarrow RO_2H + R_2CH\cdot$	$k_{a0} = 10^9$ 1/sM, $E_a = 69.9-72.8$ kJ/mol	[30/p.34]
<b>RO· propagation</b>		
$R_3CO\cdot + R_3CH \rightarrow R_3COH + R_3C\cdot$	$k_{aOH} = 2.51 \times 10^9$ 1/sM, $E_{aOH} = 22.8$ kJ/mol	[30/p.51]
$R_3CO\cdot + R_2CH_2 \rightarrow R_3COH + R_2CH\cdot$	$k_{aOH} = 1.58 \times 10^9$ 1/sM, $E_{aOH} = 25.9$ kJ/mol	[30/p.51]
<sup>(b)</sup> $k_a/(2k_t)^{1/2}$		
$R_3CH$	$[k_a/(2k_t)^{1/2}]_0 = 5900$ 1/s <sup>1/2</sup> M <sup>1/2</sup> , $E = 50.6$ kJ/mol	[31/p.60]
$R_2CH_2$	$[k_a/(2k_t)^{1/2}]_0 =$ $= 4.7 \times 10^5$ 1/s <sup>1/2</sup> M <sup>1/2</sup> , $E = 66.9$ kJ/mol	[57]
<b>RO· formation</b>		
$2R_3CO_2\cdot \rightarrow 2R_3CO\cdot + O_2$	$a = 0.17$	[55]
$2R_2CHO_2\cdot \rightarrow 2R_2CHO\cdot + O_2$	$a = 0.5$	[57]
<b>NO<sub>2</sub> initiation</b>		
$R_3CH$	$k_{i0} = 5.9 \times 10^9$ 1/sM, $E_i = 73.6$ kJ/mol	[31/p.141, table 3.10]
$R_2CH_2$	$k_{i0} = 1.2 \times 10^{10}$ 1/sM, $E_i = 86.6$ kJ/mol	[31/p.141, table 3.10]
<b>O<sub>2</sub> initiation</b>		
$R_3CH$	$k_{i0} = 1.5 \times 10^{12}$ 1/sM, $E_i = 159.0$ kJ/mol	[31/p.169, table 4.1]
$R_2CH_2$	$k_{i0} = 7.94 \times 10^{12}$ 1/sM, $E_i = 167.4$ kJ/mol	[31/p.169, table 4.1]
<sup>(c)</sup> <b>NO branching</b>		
$RO_2\cdot + \cdot NO \rightarrow RO\cdot + \cdot NO_2$	$k_{NO} = 5 \times 10^9$ 1/sM	[50]

<sup>(a)</sup> Average value for cyclohexane, hexadecane & heptadecane.

<sup>(b)</sup> The values of the ratio  $k_a/(2k_t)^{1/2}$  are more reliable than those for  $k_a$  or  $k_t$  alone; we used this ratio and the value of  $k_p$  to calculate  $k_t$ , but most probably the  $k_p$  values are inaccurate.

<sup>(c)</sup> Average for several alkanes in the gas phase in the considered temperature range; the temperature dependence is neglected.

Let us mention here one approximation involved in the surface oxidation mechanism proposed: that we did not consider the surface-bulk radical equilibration. This reaction is analogous to the bulk  $R_1\cdot + R_2H \leftrightarrow R_1H + R_2\cdot$  process mentioned in Ref. [58]. It reads:



Unlike the respective bulk-bulk equilibration, the result from the above reaction is non-trivial even for one-component fuel. Unfortunately, the equilibration parameters are hard to estimate due to the absence of data for the respective bulk ones. Therefore, we assumed that the process is of very slow rate and does not contribute to the outcome of the oxidation. As an example of the possible outcome of the process, let us consider another limiting case – the one in which the process (34) is very fast, and in which the forward and the reverse rate constants are equal to each other. This leads to the simple relation  $[s\cdot]/[sH] = [R\cdot]/[RH]$ .

Let us briefly consider also the approximation that each surface rate constant  $k_x^S$  has value close to the one of the analogous bulk process  $k_x$ . This assumption involves two questions: what is the relation between the activation energies  $E$  and the preexponential factors  $k_0$  in the rate constants of the surface and the bulk process. The activation energy is indeed a function of the state of the bonds involved in the reactions and their closest environment, which is not dramatically different in the fuel bulk and at the deposit|fuel interface. The main difference is the presence of increased number of O-containing functional groups in the polar deposit. These functional groups can activate the nearby C-H bonds [31], especially in the case of secondary C-H bond at the same carbon at which the polar group is attached, i.e.  $-\text{CH}(\text{O}_x\text{H})-$ , but also with first neighbours, i.e.  $>\text{CHC}(\text{O}_x\text{H})<$ .

With regard to the preexponential factor, a first argument for similar order of magnitude of the values of  $k_{x0}^S$  and  $k_{x0}$  is their equivalent dimensions. A more elaborate argument can be obtained from the basic theory of these preexponential factors. We will limit ourselves with a comparison between the surface reaction  $sH + A$ , where A is assumed to be in gas phase, and  $RH + A$  in the bulk of a gas. The number  $\nu_A$  of hits of molecules A to the wall is given by Maxwell's flux – within a numerical factor, it is valid that

$$\nu_A \sim N_A \sqrt{\frac{RT}{M_A}} [A]. \quad (35)$$

The respective rate  $\nu_A$  of the reaction between sH and A (in units  $[\text{m}^2/\text{s mol}]$ ) is [58]:

$$\nu_A \sim N_A \sqrt{\frac{RT}{M_A}} [A] \sigma_{HA} [sH] e^{-E/RT}, \quad (36)$$

where  $\exp(-E/RT)$  occurs due to the potential barrier  $E$ ;  $\sigma_{HA}$  is the cross-section of the reaction (treated as area per sH site which, if hit by A, can result in reaction). The dimensionless quantity  $\sigma_{HA}[sH]N_A$  is the fraction of area available for reaction. Thus, the preexponential factor of the surface reaction is:

$$k_{x0}^S \sim N_A \sqrt{\frac{RT}{M_A}} \sigma_{HA}. \quad (37)$$

The respective bulk quantity for the process  $RH + A \rightarrow \dots$  is given by [58]:

$$k_{x0} \sim N_A \sqrt{\frac{RT(M_{RH} + M_A)}{M_{RH}M_A}} \sigma_{HA}. \quad (38)$$

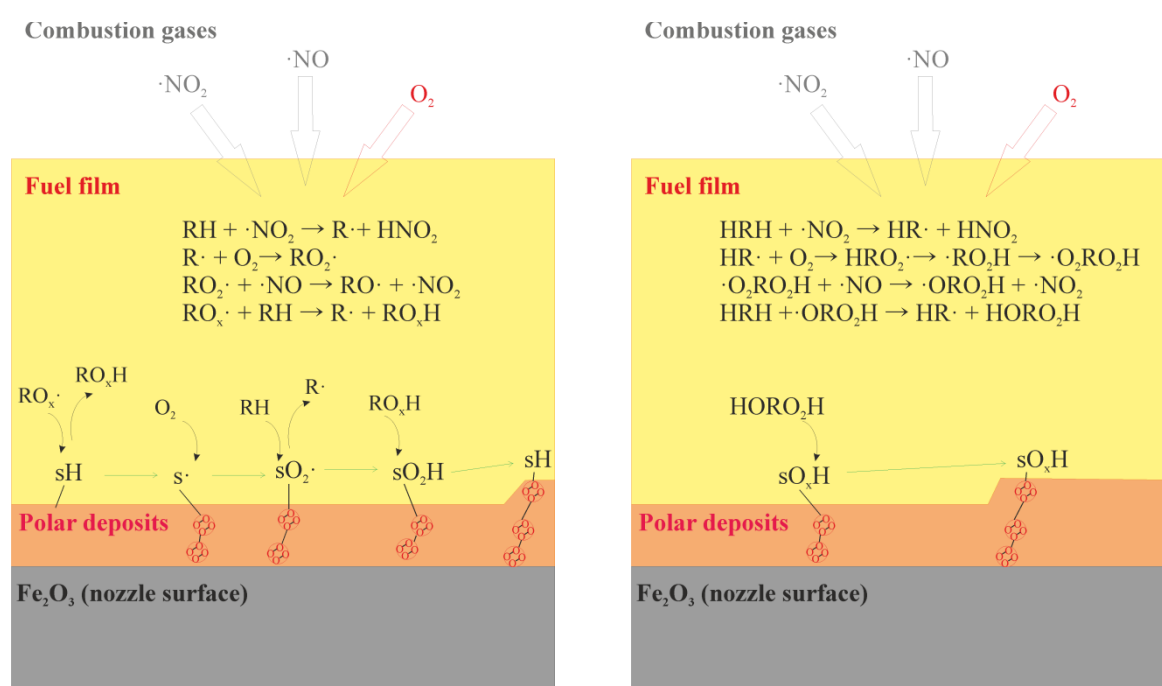


Thus, the ratio between the preexponential factors for the considered reaction, as it follows from Eqs (37)&(38), under the assumption that  $\sigma_{\text{HA}}$  of the reaction does not change in case that the reactive C-H bond is bound to the surface, is the following one:

$$\frac{k_{x0}}{k_{x0}^S} \sim \sqrt{1 + \frac{M_{\text{RH}}}{M_{\text{A}}}} \quad (39)$$

As the molar masses of RH and A are not too different, the bulk and the surface preexponential factors are expected to be of similar order of magnitude. Similar formula can be devised using the basic theory of liquid phase reactions, but with diffusion coefficient ratio instead of mass ratio.

Let us conclude this section with a schematic overview of the assumed mechanism for surface growth of the deposit – it is illustrated in **Figure S4-left**. In **Figure S4-right**, an idea is given of how this mechanism will alter in the case where most of the oxidation process follows intramolecular propagation reaction.



**Figure S4-left:** Mechanism of deposit formation through liquid phase oxidation. Combustion gases provide oxygen and radicals  $i\cdot$  that are transferred to the liquid fuel film, reaction (40), and initiate there the radical chain reactions (4). The major radicals in the fuel film ( $\text{RO}_2\cdot$ ,  $\text{RO}\cdot$  &  $\cdot\text{NO}_2$ ), start the process of surface oxidation through Eq (18), which leads to deposit oxidation and formation of a polar site  $\text{sO}_x\text{H}$  at the surface, Eq (19). Polar oxidation products adsorb at the active sites and lead to deposit growth. *Right:* in the case where polyfunctional oxidation products are formed in the fuel ( $\text{HO}_2\text{RO}_2\text{H}$ ) through intramolecular propagation, the site formation and the adsorption stages merge in one, skipping the slow surface initiation stage.

### S3. Gas transfer to the liquid film

The transfer process is:



If the film is homogeneous in composition (due to efficient turbulent convection, Marangoni effect etc.), the rate of the process is controlled by the following mass balance equation:

$$\frac{d(V^F[i \cdot])}{dt} = A^F j_{i,cond} - A^F j_{i,evap} - V^F v_i; \quad (41)$$

here,  $A^F$  and  $V^F$  are the area and the volume of the liquid film;  $j_{i,cond}$  is the current of radicals from the gas phase reaching the liquid/gas interface. If the turbulent convective flux of radicals in the combustion gases is fast enough,  $j_{i,cond}$  is given by Maxwell's flux

$$j_{i,cond} = [i \cdot]^G \sqrt{\frac{RT}{2\pi M_i}}. \quad (42)$$

Here,  $M_i$  is the molar mass of  $i \cdot$ ; the factor for the effective hits is assumed equal to one (for heavy  $i \cdot$  it may be smaller). In the case where convective flux through the gas is slow (the boundary layer thickness is of larger thickness than the one of the Fuchs layer),  $[i \cdot]^G$  will be lower than the bulk value. The current  $j_{i,evap}$  in Eq (41) stands for the radicals that evaporate back to the gas phase. Since if Henry's equilibrium is reached it is valid that  $j_{i,evap} = j_{i,cond}$ , we can express  $j_{i,evap}$  through  $j_{i,cond}$  and Henry's constant  $K_{H,i} = [i \cdot]_{eq}/[i \cdot]_{eq}^G$  of the radical as follows:

$$j_{i,evap} = \frac{1}{K_{H,i}} \sqrt{\frac{RT}{2\pi M_i}} [i \cdot]. \quad (43)$$

Assuming for simplicity that the fuel film thickness and area are not time dependent, we can write Eq (41) as

$$\frac{d[i \cdot]}{dt} = \sqrt{\frac{RT}{2\pi M_i}} \frac{[i \cdot]^G - [i \cdot]/K_{H,i}}{h^F} - v_i, \quad (44)$$

where we used  $h^F = V^F/A^F$ . It is evident from this equation that if  $h^F$  is small enough, the concentration  $[i \cdot]$  in the liquid phase will be close to the equilibrium value  $[i \cdot] = K_{H,i}[i \cdot]^G$ . On the other hand, a larger quantity of fuel will result in lower concentration of radicals and eventually, *slower* oxidation process. Various processes can complicate the above equation. It is derived under the assumption that the convective mass transfer is faster than the Maxwell current  $j_{i,cond} - j_{i,evap}$  (equivalently said, the transfer through the boundary layer is faster than the one through the Fuchs layer). Thermophoresis (thermodiffusion) is also neglected.

The initiation rate is given by Eq (5), which, if one initiator dominates the process, reads  $v_i = k_i[RH][i \cdot]$ . If during the degradation the temperature of the film is fixed to the constant  $T_{wall}$ , the solution to Eq (44) reads:

$$[i \cdot] = \frac{K_{H,i}}{\tau_M} \int_0^t [i \cdot]^G \exp\left[-(t-t')\left(\frac{1}{\tau_i} + \frac{1}{\tau_M}\right)\right] dt', \quad (45)$$

where we introduced the characteristic times  $\tau_M$  of Maxwell's transport and  $\tau_i$  of the initiation reaction as:

$$\tau_M = K_{H,i} h^F \sqrt{\frac{2\pi M_i}{RT}} \quad \text{and} \quad \tau_i = \frac{1}{k_i[RH]}. \quad (46)$$

Their orders of magnitude for  $\text{NO}_2$  are  $\tau_M \sim 0.5\text{-}1 \mu\text{s}$  and  $\tau_i = 5\text{-}50 \text{ms}$  in the range  $T_{wall} = 140\text{-}190^\circ\text{C}$ . As  $\tau^M$  is small compared to the time of the cycle ( $\sim 1 \text{ms}$ ), only a tiny range of times close to  $t' \sim t$  contributes to the integral (45), which allows us to simplify it:

$$[i\cdot] \approx \frac{K_{H,i}}{\tau_M} \int_0^t [i\cdot]_{t'=t'}^G \exp\left[-(t-t')\left(\frac{1}{\tau_i} + \frac{1}{\tau_M}\right)\right] dt' \approx \frac{\tau_i}{\tau_i + \tau_M} K_{H,i} [i\cdot]^G. \quad (47)$$

In addition,  $\tau_i \gg \tau_M$ , therefore

$$[i\cdot] = K_{H,i} [i\cdot]^G. \quad (48)$$

We present this derivation in order to analyse the limits of validity of Eq (48). There are two cases in which Eq (48) will fail. In certain cases – in particular, heavy radicals with high affinity to the fuel phase (large  $K_{H,i}$ ),  $\tau^M$  can have value comparable with the time for a cycle. Then, the Maxwell flux will not have enough time to equilibrate the gas and the liquid layers near the interface, leading to lower concentration of these radicals in the fuel. Also, very reactive radicals (such as  $RO\cdot$ ) may have  $\tau_i$  much smaller than  $\tau_M$ . In this case, instead of Eq (48), one must use Eq (47), which predicts much lower concentration of these radicals in the bulk compared to the equilibrium one. Both effects diminish the role of large, reactive radicals produced by the combustion.

#### S4. Nozzle channel deposits: relationship between flow reduction and deposit thickness, and processing of the experimental data

Let us first analyse the accuracy of the relation  $1 - Q/Q_0 \approx 2h_n/R_n$ , Eq (27). Toward this goal, we first consider the Colebrook-White equation (which has been proposed for long channels, but involves roughness explicitly). Its original formulation is via a non-linear equation for the Darcy friction factor  $f$ :

$$\frac{1}{\sqrt{f}} = -2 \lg \left[ \frac{\varepsilon}{7.4(R_n - h_n)} + \frac{2.51}{Re\sqrt{f}} \right]. \quad (49)$$

The relation between the discharge per unit area  $Q/\pi(R_n - h_n)^2$  (the average velocity of the fuel) and the driving force of the flow (the pressure gradient  $\Delta p/L$ , where  $L$  is the nozzle channel length) involves  $f$ :

$$\frac{\Delta p}{L} = \frac{f \rho^F}{4(R_n - h_n)} \left[ \frac{Q}{\pi(R_n - h_n)^2} \right]^2. \quad (50)$$

In the above, the Reynolds number stands for:

$$Re = \frac{2\rho^F (R_n - h_n)}{\eta^F} \frac{Q}{\pi(R_n - h_n)^2}. \quad (51)$$

Eqs (49)-(51) set system of equations that allows the calculation of  $Q$ ,  $f$  &  $Re$  if the roughness  $\varepsilon$  and the thickness  $h$  are known. The expansion into series of  $1 - Q/Q_0$ ,  $Q$  being the solution of Eqs (49)-(51) and  $Q_0$  being  $Q$  at  $h_n = 0$ , with respect to small  $h_n$  yields:

$$1 - \frac{Q}{Q_0} = \frac{5}{2} \frac{h_n}{R_n} - \frac{\frac{\varepsilon}{7.4R_n} + \frac{3}{2} \frac{0.628\eta^F}{R_n^{3/2} \sqrt{\rho^F \Delta p / L}}}{\left( \frac{\varepsilon}{7.4R_n} + \frac{0.628\eta^F}{R_n^{3/2} \sqrt{\rho^F \Delta p / L}} \right) \ln \left( \frac{\varepsilon}{7.4R_n} + \frac{0.628\eta^F}{R_n^{3/2} \sqrt{\rho^F \Delta p / L}} \right)} \frac{h_n}{R_n}. \quad (52)$$

For the typical parameters of fuel injection, the first term dominates; neglecting the second, we arrive at the relation  $1 - Q/Q_0 \approx 5h_n/2R_n$  (corresponding to  $\partial \ln C_d / \partial R_n \approx 0.5/R_n$  in Eq (27)). As for the  $\partial \ln C_d / \partial \varepsilon$  term in Eq (27), for a 50  $\mu\text{m}$  nozzle, from Eqs (49)-(51) it can be shown that it

is approximately  $\partial \ln C_d / \partial \varepsilon \approx -0.07 / \varepsilon$ . While the deposit is growing in the grooves of the metal surface, they decrease the roughness and it can be assumed that  $d\varepsilon/dh_n \approx -1$ . As  $\varepsilon \ll R_n$ , the roughness term in Eq (27) will dominate and so the deposits should cause a significant increase of the flow rate during this initial period. Once the surface is covered by deposits,  $\varepsilon$  of the deposit/fuel interface should not change with  $h_n$  and so  $d\varepsilon/dh_n = 0$ . Therefore, the result  $1 - Q/Q_0 \approx 2h_n/R_n$  can be used only after the metal grooves are already filled with deposits.

Another empirical formula that is often used for discharge through orifices [72] is:

$$C_d = \left[ 1.5 + 9.72 \frac{L_n^{1/2}}{(R_n - h_n)^{1/2} Re^{1/2}} \right]^{-1/2}. \quad (53)$$

For the typical range of values of  $Re$ ,  $L_n$  and  $R_n$  of a fuel injector, it yields  $\partial \ln C_d / \partial R_n \approx 0.05 - 0.1/R_n$ , lower than  $0.5/R_n$  following from Eq (52). Therefore, the error of the relation  $1 - Q/Q_0 \approx 2h_n/R_n$  that follows from Eqs (52)&(53) is less than 20%, which is acceptable for the purposes of this work.

We use this relation to transform the experimental data of Aradi et al. [42] for the rate of deposit growth from relative to absolute values. After careful investigation of *figures 17&13* of Aradi et al., we concluded that for the regression, they used the formula  $v_n/k_r \times (1 - e^{-v_n t})$  instead of their correct *eq 11* (our Eq (25)). In result, in the  $v_n$ -column (their  $k_1$ ) of *table 5* [42], what actually stands are the values of  $k_r$  (their  $k_2$ ). In the second,  $k_r$ -column (their  $k_2$ ) of *table 5*, the data refer actually to the quantity  $R_n k_r^2 / 2v_n$  (where the factor  $2/R_n$  occurs as  $h_n$  is made dimensionless via division by  $R_n/2$ , as it follows from *eq 10* in [42]). Thus, to compare their experimental results with our theoretical  $v_n$ , we must use  $k_1^2/k_2 \times R_n/2$ , with  $k_1$  and  $k_2$  from *table 5* [42]. Unfortunately, they did not provide value for  $R_n$ , so we assumed  $R_n = 50 \mu\text{m}$ . To compare our results with the experimental data, we recalculated the correct coefficients in **Table S3** for the data for non-additized fuels.

**Table S3:** The data of Aradi et al. [42] for the flow rate reduction due to nozzle channel deposits – calculation of the correct rate parameters  $v_n$  &  $k_r$ .

<sup>(a)</sup> Fuel	$T_{90\%}$ [°C]	Olefin [w%]	S [wppm]	<sup>(b)</sup> $k_1$ [h <sup>-1</sup> ]	<sup>(b)</sup> $k_2$ [h <sup>-1</sup> ]	<sup>(c)</sup> $k_r$ [h <sup>-1</sup> ]	<sup>(d)</sup> $v_n$ from Eq (27) [μm/h]
Fuel 7	161	19.9	153	0.568	8.759	0.568	0.9208
Howell- EEE	160	12.9	20	0.535	4.573	0.535	1.5648
Fuel 10	171	1.2	421	0.103	0.427	0.103	0.6211

<sup>(a)</sup> For details cf. Ref. [42].

<sup>(b)</sup> Values from *table 5* in Ref. [42].

<sup>(c)</sup> The correct  $k_r$ , equal to  $k_1$ .

<sup>(d)</sup> Deposit formation rate  $v_n$  (made in units μm/h) calculated as  $k_1^2/k_2 \times R_n/2$ . The unit conversion involves the relation (27),  $1 - Q/Q_0 \approx 2h_n/R_n$ .

## S5. The multilayer heat transfer problem

We solve the heat transfer problem set by Fourier's equations for the metal and the deposit phase:

$$\begin{aligned} -h^M < z < 0: \quad & \frac{\partial T^M}{\partial t} = \chi^M \frac{\partial^2 T^M}{\partial z^2} ; \\ 0 < z < h_{\text{tip}}: \quad & \frac{\partial T^D}{\partial t} = \chi^D \frac{\partial^2 T^D}{\partial z^2} . \end{aligned} \quad (54)$$

The heat current  $q^S$  coming from the gas phase is a periodic function. The Fourier series of it is:

$$\left( \kappa^D \frac{\partial T^D}{\partial z} \Big|_{z=h_{\text{tip}}} = \right) q^S = \bar{q}^S + \sum_{n=1}^N q_{c,n}^S \cos n\omega t + \sum_{n=1}^N q_{s,n}^S \sin n\omega t . \quad (55)$$

Here, the angular frequency  $\omega$  is related to the period  $\tau$  as  $\omega = 2\pi/\tau$ . The Fourier coefficients in Eq (55) are related to  $q^S(t)$  in Figure 8 as given by Eqs (30). This is the first boundary condition for Eq (54). The other three are:

$$\begin{aligned} z = 0: \quad & T^M = T^D \quad \text{and} \quad \kappa^M \frac{\partial T^M}{\partial z} = \kappa^D \frac{\partial T^D}{\partial z} ; \\ & z = -h^M: \quad T^M = T_{\text{out}}. \end{aligned} \quad (56)$$

The solution to the stated problem reads:

$$\begin{aligned} T^M &= \bar{T}^M(z) + \sum_{n=1}^N T_{c,n}^M(z) \cos n\omega t + \sum_{n=1}^N T_{s,n}^M(z) \sin n\omega t , \\ T^D &= \bar{T}^D(z) + \sum_{n=1}^N T_{c,n}^D(z) \cos n\omega t + \sum_{n=1}^N T_{s,n}^D(z) \sin n\omega t . \end{aligned} \quad (57)$$

Here, the Fourier coefficients of  $T(x,t)$  are related to those of  $q^S$ . The 0<sup>th</sup>-order coefficients are related via Eqs (32)-(33). The functional dependence of the four Fourier coefficients  $T_{c,n}^M$ ,  $T_{s,n}^M$ ,  $T_{c,n}^D$  and  $T_{s,n}^D$  on  $z$  follows from the Fourier series of Eqs (54). For the deposit phase,

$$\begin{aligned} T_{c,n}^M &\approx \left( c_{1,n}^M \cos \frac{z}{\delta_n^M} + c_{3,n}^M \sin \frac{z}{\delta_n^M} \right) e^{-|z|/\delta_n^M} ; \\ T_{s,n}^M &\approx \left( -c_{1,n}^M \sin \frac{z}{\delta_n^M} + c_{3,n}^M \cos \frac{z}{\delta_n^M} \right) e^{-|z|/\delta_n^M} ; \\ T_{c,n}^D &= \left( c_{1,n}^D \cos \frac{z}{\delta_n^D} + c_{3,n}^D \sin \frac{z}{\delta_n^D} \right) e^{-z/\delta_n^D} + \left( c_{2,n}^D \cos \frac{z}{\delta_n^D} + c_{4,n}^D \sin \frac{z}{\delta_n^D} \right) e^{z/\delta_n^D} ; \\ T_{s,n}^D &= \left( c_{1,n}^D \sin \frac{z}{\delta_n^D} - c_{3,n}^D \cos \frac{z}{\delta_n^D} \right) e^{-z/\delta_n^D} + \left( -c_{2,n}^D \sin \frac{z}{\delta_n^D} + c_{4,n}^D \cos \frac{z}{\delta_n^D} \right) e^{z/\delta_n^D} . \end{aligned} \quad (58)$$

Here, the characteristic lengths of the heat transfer in the metal and in the deposit phase are:

$$\delta_n^M = \sqrt{2\chi^M / n\omega} \quad \text{and} \quad \delta_n^D = \sqrt{2\chi^D / n\omega} . \quad (59)$$

The Fourier coefficients of  $T$  in the metal phase contain, in principle, a second term proportional to  $\exp(+|z|/\delta_n^M)$ , but the coefficients multiplying it can be shown to be negligible (proportional to the small  $\exp(-h^M/\delta_n^M)$ ) and are consequently neglected in Eq (58). Therefore, the oscillating part of  $T^M$  decays fast with  $z$ , which means that near the outer wall of the metal, the temperature follows almost exactly the stationary linear profile  $T^M(z)$ , cf. Eq (32).

The  $c$ -coefficients in Eq (58) follow from the Fourier series of the boundary conditions (55)-(56) (without the last). For each  $i$ , from the temperature continuity at  $z = 0$  it follows that:

$$-c_{3,n}^D + c_{4,n}^D = c_{3,n}^M \quad \text{and} \quad c_{1,n}^D + c_{2,n}^D = c_{1,n}^M. \quad (60)$$

From the heat flux continuity,

$$\begin{aligned} \frac{\kappa^D}{\delta_n^D} (c_{1,n}^D - c_{2,n}^D + c_{3,n}^D + c_{4,n}^D) &= \frac{\kappa^M}{\delta_n^M} (-c_{1,n}^M + c_{3,n}^M); \\ \frac{\kappa^D}{\delta_n^D} (-c_{1,n}^D + c_{2,n}^D + c_{3,n}^D + c_{4,n}^D) &= \frac{\kappa^M}{\delta_n^M} (c_{1,n}^M + c_{3,n}^M). \end{aligned} \quad (61)$$

The solution to Eqs (60)-(61) reads:

$$\begin{aligned} c_{1,n}^M &= \frac{2\kappa^D / \delta_n^D}{\kappa^D / \delta_n^D - \kappa^M / \delta_n^M} c_{1,n}^D; \quad c_{3,n}^M = -\frac{2\kappa^D / \delta_n^D}{\kappa^D / \delta_n^D - \kappa^M / \delta_n^M} c_{3,n}^D; \\ c_{2,n}^D &= \frac{\kappa^D / \delta_n^D + \kappa^M / \delta_n^M}{\kappa^D / \delta_n^D - \kappa^M / \delta_n^M} c_{1,n}^D; \quad c_{4,n}^D = -\frac{\kappa^D / \delta_n^D + \kappa^M / \delta_n^M}{\kappa^D / \delta_n^D - \kappa^M / \delta_n^M} c_{3,n}^D. \end{aligned} \quad (62)$$

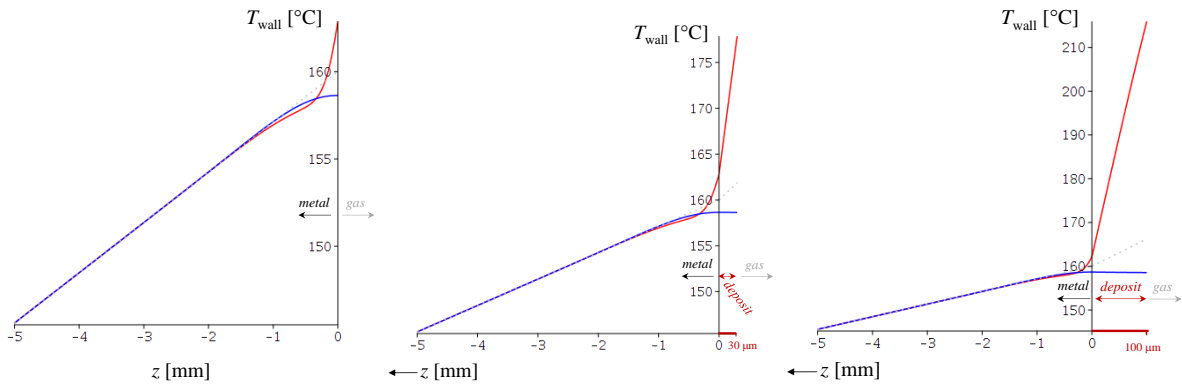
From the flux continuity (55) at  $z = h^D$ , the last two coefficients of the  $n^{\text{th}}$  order follow:

$$\begin{aligned} c_{3,n}^D &= \left(1 - \frac{\kappa^M \delta_n^D}{\kappa^D \delta_n^M}\right) \frac{(A_{+-} + A_{-+}) q_{s,n}^S - (A_{++} + A_{--}) q_{c,n}^S}{(A_{+-} + A_{-+})^2 + (A_{++} + A_{--})^2}; \\ c_{1,n}^D &= -\left(1 - \frac{\kappa^M \delta_n^D}{\kappa^D \delta_n^M}\right) \frac{(A_{++} + A_{--}) q_{s,n}^S + (A_{+-} + A_{-+}) q_{c,n}^S}{(A_{+-} + A_{-+})^2 + (A_{++} + A_{--})^2}, \end{aligned} \quad (63)$$

where

$$\begin{aligned} A_{++} &= \left(\sin \frac{h_{\text{tip}}}{\delta_n^D} + \cos \frac{h_{\text{tip}}}{\delta_n^D}\right) \left(\frac{\kappa^D}{\delta_n^D} + \frac{\kappa^M}{\delta_n^M}\right) e^{h_{\text{tip}}/\delta_n^D}; \\ A_{-+} &= \left(\sin \frac{h_{\text{tip}}}{\delta_n^D} - \cos \frac{h_{\text{tip}}}{\delta_n^D}\right) \left(\frac{\kappa^D}{\delta_n^D} + \frac{\kappa^M}{\delta_n^M}\right) e^{h_{\text{tip}}/\delta_n^D}; \\ A_{+-} &= \left(\sin \frac{h_{\text{tip}}}{\delta_n^D} + \cos \frac{h_{\text{tip}}}{\delta_n^D}\right) \left(\frac{\kappa^D}{\delta_n^D} - \frac{\kappa^M}{\delta_n^M}\right) e^{-h_{\text{tip}}/\delta_n^D}; \\ A_{--} &= \left(\sin \frac{h_{\text{tip}}}{\delta_n^D} - \cos \frac{h_{\text{tip}}}{\delta_n^D}\right) \left(\frac{\kappa^D}{\delta_n^D} - \frac{\kappa^M}{\delta_n^M}\right) e^{-h_{\text{tip}}/\delta_n^D}. \end{aligned} \quad (64)$$

The profile (57) is illustrated in **Figure S5**.



**Figure S5:** Profiles of the temperature for three values of  $h_{\text{tip}}$ : 0, 30, 100  $\mu\text{m}$ . The abscissa axis in the positive region of  $z$  is multiplied by 10 for clarity.

## S6. List of symbols and abbreviations

### Symbols

$a$	fraction of $\text{RO}_2\cdot$ that terminate during the reaction between two $\text{RO}_2\cdot$ , $a = k_t/(k_t + k_{\text{OH}})$
$a_{\text{sH}}$	average area per C-H bond at the surface
$\text{CAD}_0$	CAD of start of accumulation of leaked fuel
$\text{CAD}_b$	CAD of boiling and precipitation
$C_d$	discharge coefficient
$c$	heat capacity per unit volume of a material
$E$	activation energy in the Arrhenius law for $k$
$h^{\text{F}}$	fuel film thickness
$h^{\text{M}}$	thickness of the metal layer at the injector surface
$h_n$	thickness of the nozzle channel deposits
$h_{\text{tip}}$	thickness of the injector tip deposits
$\Delta h$	increase of the deposit thickness for the period of one cycle
$[\text{i}\cdot]$	concentration of the initiator in the fuel film
$[\text{i}\cdot]^{\text{G}}$	concentration of the initiator in the quench layer
$K_{\text{H}}$	Henry's constant
$k$	rate constant
$k_0$	preexponential factor in the Arrhenius law for $k$
$k_r$	empirical proportionality constant in the rate $-k_r h_n$ of deposit removal
$L$	length of the nozzle channel
$M_d$	molar mass of the deposit precursors
$p$	cylinder pressure
$p_0$	standard pressure, 101325 Pa
$\Delta p$	injector pressure
$Q$	volumetric flow rate through the nozzle
$Q_0$	maximal volumetric flow rate through the nozzle
$q^{\text{S}}$	heat flux from the combustion gases to the injector surface
$R$	gas constant
$R_n$	nozzle channel radius (not affected by the deposits)
$r_{\text{W}}$	Wenzel factor (ratio between actual area of a rough surface and projected area)
$s_{\text{H}}$	deposit-bound reactive C-H bond at the interface deposit fuel
$T$	temperature
$T_{90\%}$	$T$ at which 90% of the fuel is evaporated ( $T_{90\%} = T_b$ for single component fuel)
$T_b$	boiling temperature
$T_{b0}$	boiling temperature at standard conditions
$T^{\text{F}}$	film temperature, $\min(T_b, T_{\text{wall}})$
$T_{\text{out}}$	temperature at the outer wall ( $x = -h^{\text{M}}$ ) of the metal layer
$T_{\text{wall}}$	wall temperature
$t$	time
$t_0$	starting time of the accumulation of leaked fuel, $\tau \times \text{CAD}_0 / 720^\circ$
$t_b$	moment of boiling and precipitation, $\tau \times \text{CAD}_b / 720^\circ$
$t_{\text{end}}$	end of the combustion cycle, $\pi/2$
$V$	volume of the leaked droplet
$v$	rate of a reaction
$v_i$	initiation rate [ $\text{mol}/\text{m}^3\text{s}$ ]
$v_n$	rate of formation of nozzle channel deposits, $\Delta h_n / \tau$



$v^S$	rate of a reaction at the interface deposit fuel [mol/m <sup>2</sup> s]
$w\%$	weight part
$wppm$	weigh ppm
$x\%$	molar part
$xppm$	molar ppm
$x_{active}$	the fraction of reactive C-H bonds at the surface among all C-H bonds
$z$	Cartesian coordinate normal to the surface of the injector
$\varepsilon$	mean roughness of the nozzle wall
$\eta(x)$	Heaviside step function, $\eta(x) = 1$ for $x > 0$ and $\eta(x) = 0$ for $x < 0$
$\eta_f$	viscosity of the fuel
$\kappa$	heat conductivity
$\lambda_b$	heat of vaporization
$\nu$	engine speed [rpm]
$\xi$	pair mixing fraction
$\rho$	mass density
$\tau$	period for a full cycle, $2/\nu$
$\chi$	temperature diffusivity, $\kappa/c$
$\omega$	cycle-based angular velocity, $2\pi/\tau$

### **Abbreviations**

BMEP	break mean effective pressure
CAD	crank angle degree
E10	gasoline with 10% ethanolic blend
HC	hydrocarbon
IMEP	indicated mean effective pressure
MFB50	CAD of 50% mass fuel burned
PRF95	95 w% isooctane, 5 w% heptane

### **indices of a quantity X**

$\bar{X}$	time-averaged value and 0 <sup>th</sup> Fourier coefficient of $X(t)$
$X_0$	value at the start of the accumulation of leaked fuel
$X_a$	hydrogen abstraction by $RO_2\cdot$
$X_{aOH}$	hydrogen abstraction by $RO\cdot$
$X_b$	value at the point of boiling and precipitation
$X_{c,n}$	$n^{\text{th}}$ even Fourier coefficient (multiplying $\cos n\omega t$ )
$X^D$	deposit phase
$X^F$	fuel film phase
$X_i$	initiation
$X^M$	metal phase
$X_{NO}$	branching by $\cdot NO + RO_2\cdot \rightarrow \cdot NO_2 + RO\cdot$
$X_n$	nozzle deposit
$X_{OH}$	formation of $RO\cdot$ by $2RO_2\cdot \rightarrow 2RO\cdot + O_2$
$X_o$	oxidation
$X^S$	surface
$X_{s,n}$	$n^{\text{th}}$ odd Fourier coefficient (multiplying $\sin n\omega t$ )
$X_t$	termination
$X_{tip}$	tip deposit